

# Modems: Modulation Waveforms: Past, Present, & Future



29 November – 2 December 2011

fred harris

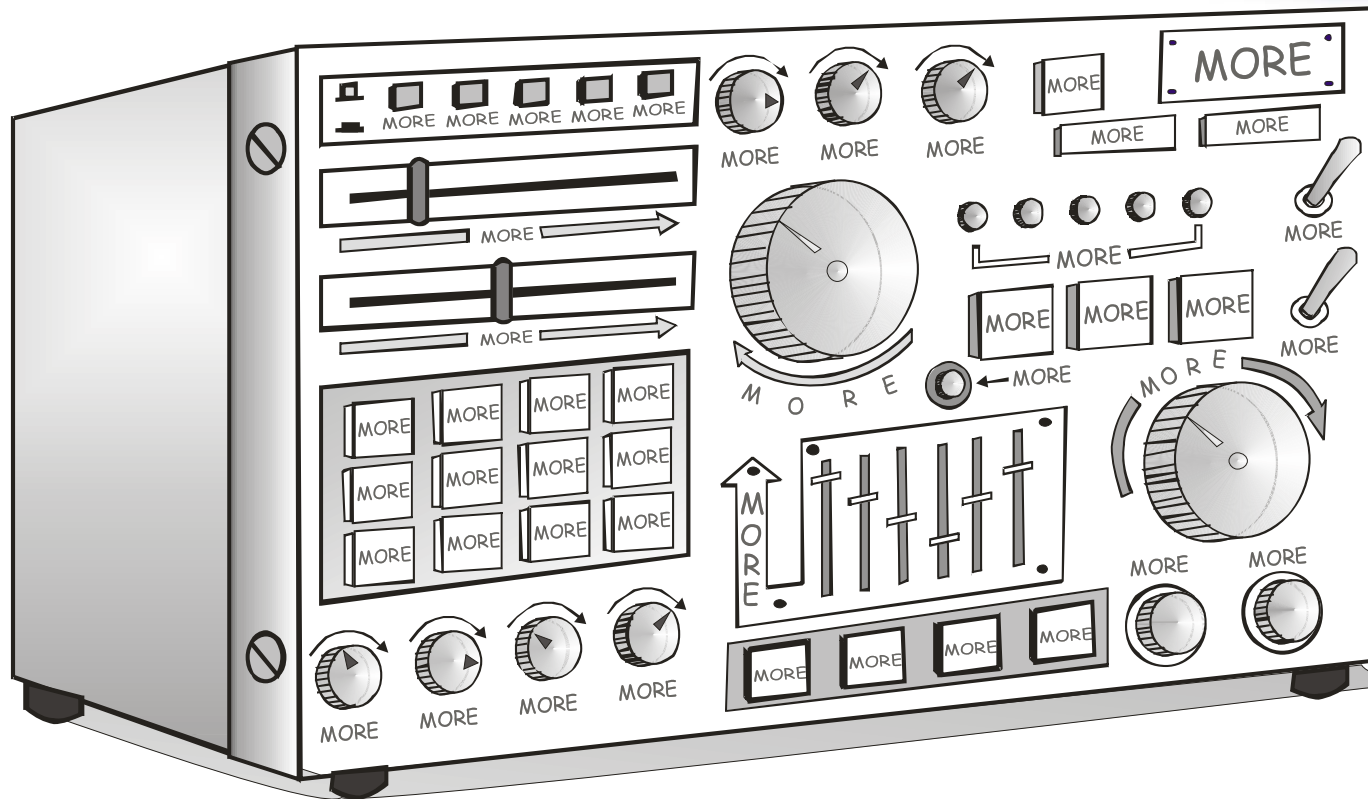


"Wake up! You're the  
next interesting speaker!"



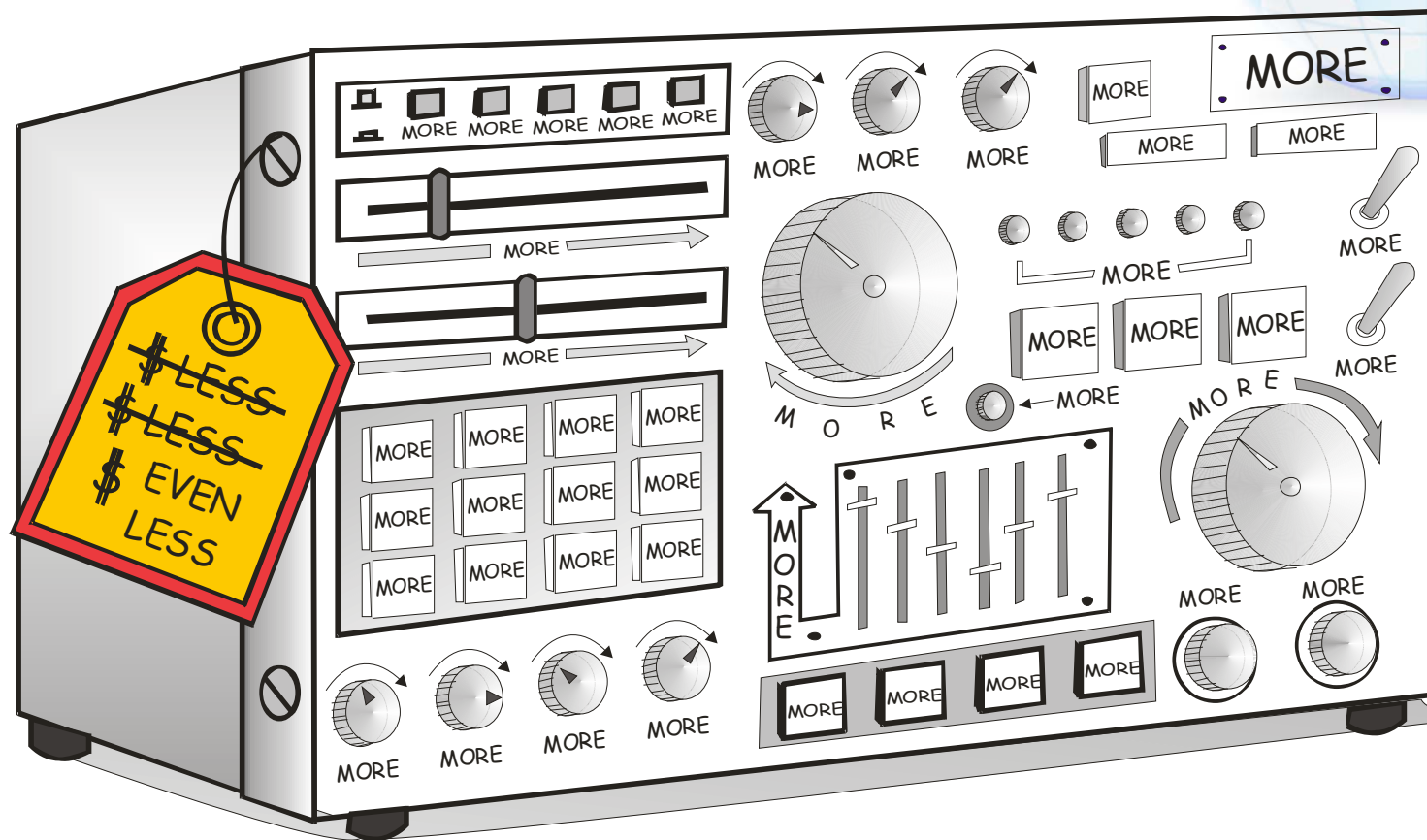
"THE NEW PRODUCTIVITY  
GOALS ARE HERE."

# What the Customer Wants

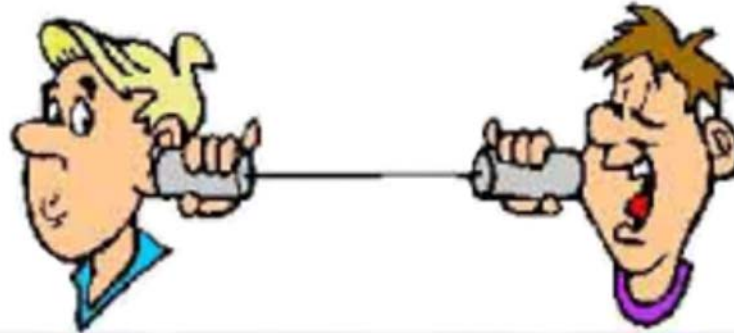


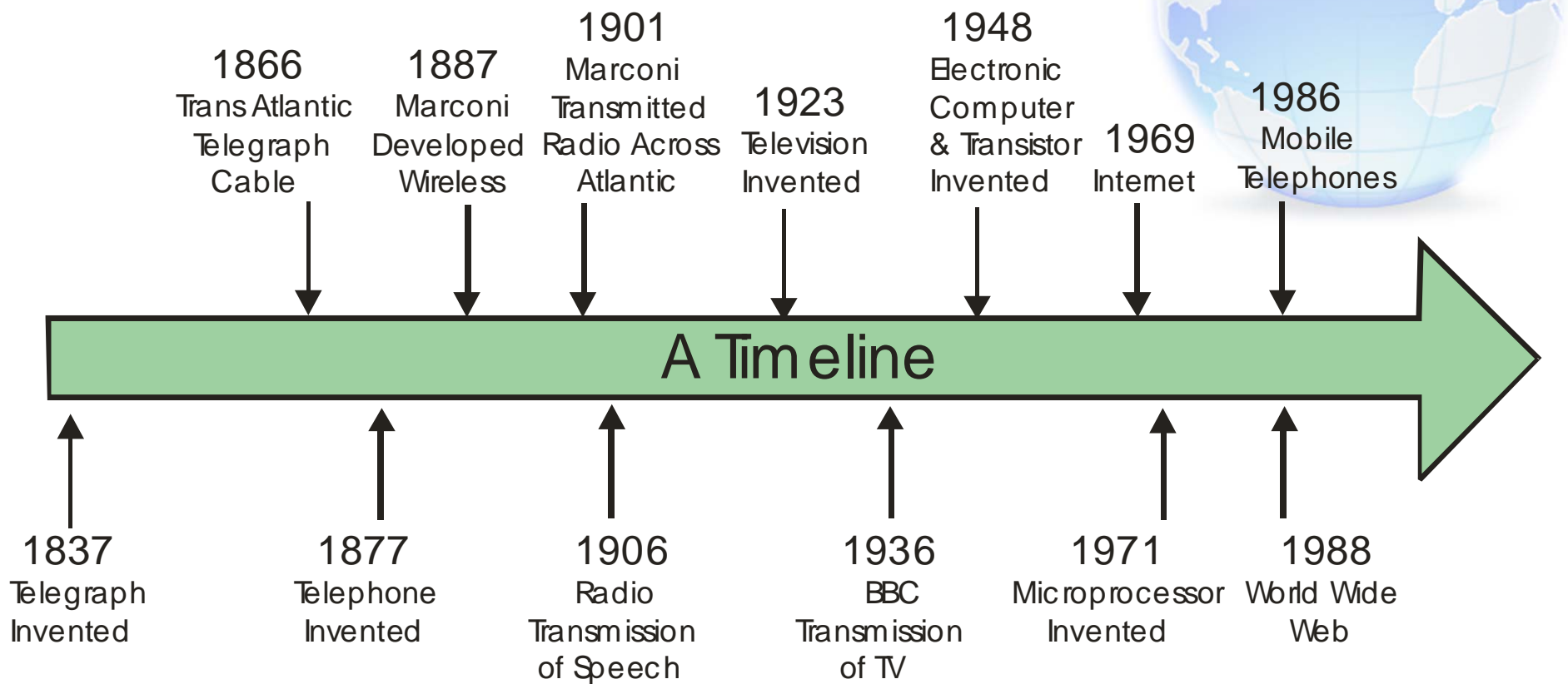


# What The Customer Expects to Pay



## A Short History of Communication Signals And Modem Design





Telegraph → Telephone → Wireless

# Very Early Communications at a Distance: Free Space Acoustic and Optical Channels



Drums, Whistles,  
Cannon Fire



Claude Chappe 1793  
Optical Telegraph



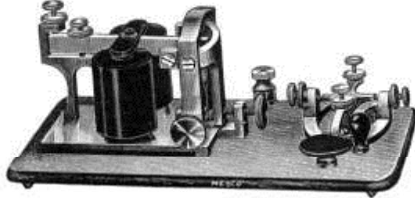
Smoke Signals,  
Semaphore,  
Beacon Fires, Ship Flags,  
Heliograph,  
Signal (Aldis) Lamp



# Disruptive Technology in Communications



The Printing Press: 1450,  
German Inventor Johannes Gutenberg



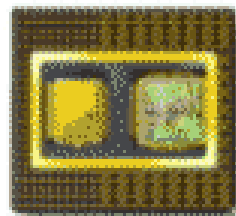
The Long Distance Electric Telegraph: 1843,  
American Inventor Samuel Morse



The Telephone: 1876,  
British Inventor Alexander Graham Bell



Wireless (Radio): 1901,  
Italian Inventor Guglielmo Marconi



The Microprocessor: 1971  
American Inventor Ted Hoff

Preparing Conditions for next Disruption

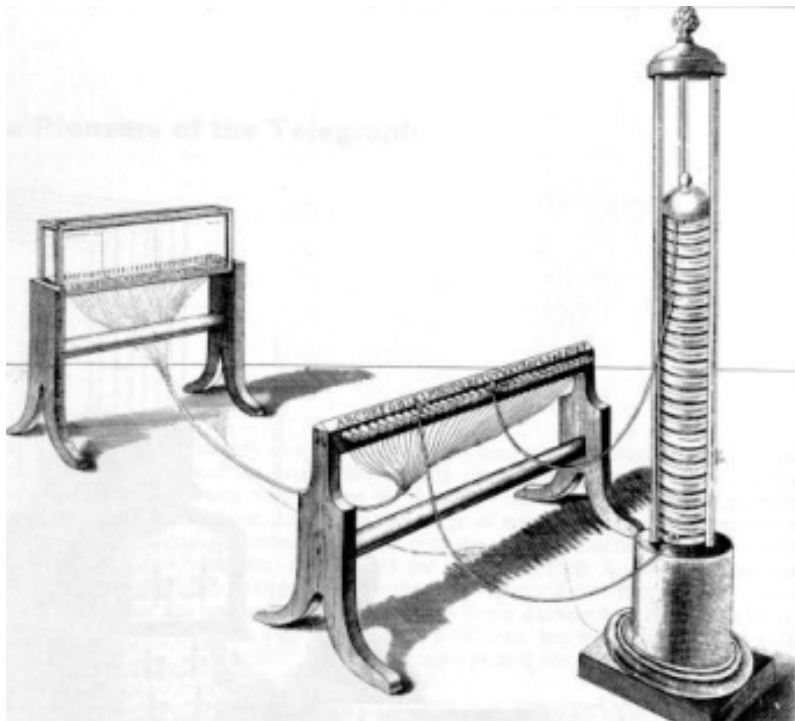


# Disruptive Technology



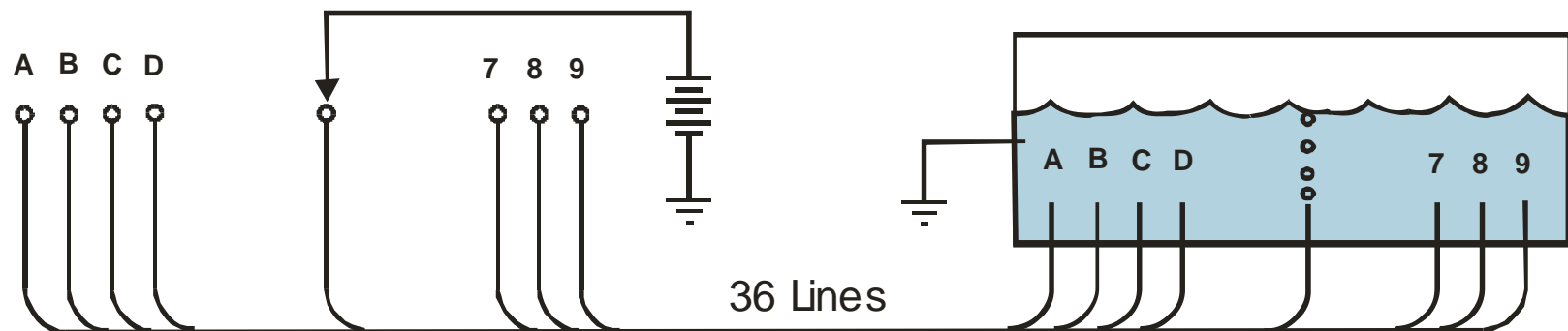
- The electric telegraph arrived in the early 19-th century and redefined communications at a distance.
- It required the confluence of three factors:
  - The science of electromagnetism,
  - The ability to generate and store electricity
  - The Industrial Revolution to build the required infrastructure.

# Converting an Electrical Connection Into a Signal

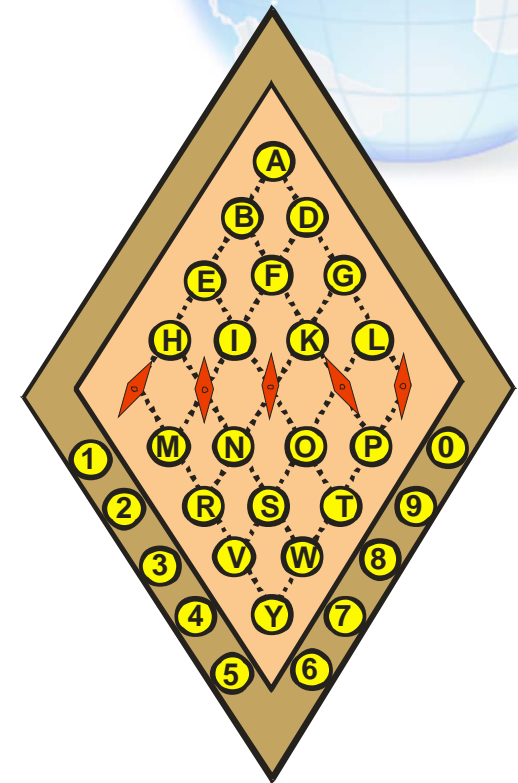
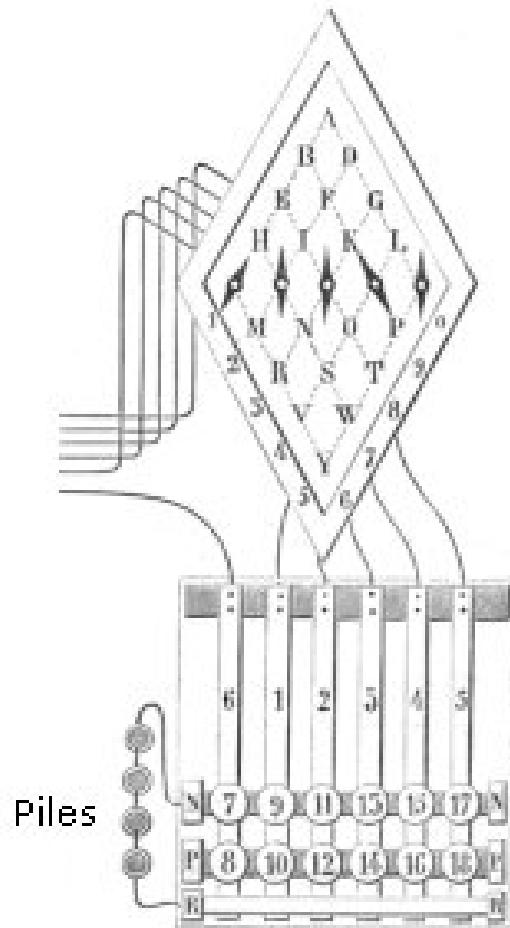
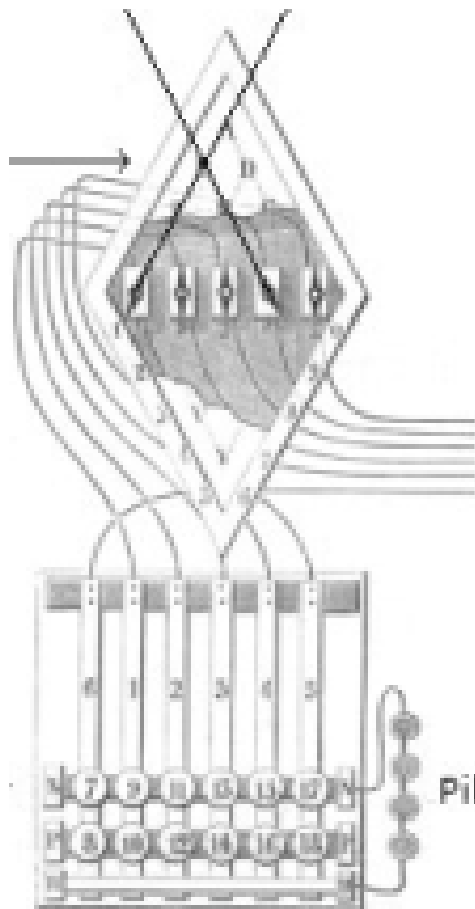


Samuel Thomas von Sömmering's  
(1808-10)

"Space Multiplexed" Electrochemical  
Telegraph



# Cooke and Wheatstone Telegraph



2 out of 5 Coding  
( $5 \times 4 = 20$ )



# Single Needle Telegraph Variable Length Code



## Single Needle (1846)

⌘	\	f	W	m	/	t	///	1	/	6	^
a	W	g	w	n	//	u	w	2	//	7	W
b	W	h	W	o	///	v	w	3	///	8	W
c	W	i	w	p	///	w	w	4	^	9	^
d	v	k	W	r	v	x	W	5	^	0	W
e	W	l	W	s	v	y	W			+	W

⌘ not understand, end of word    E understand  
R wait    W go on, decimal point    H⌘ figures

**Cooke-Wheatstone  
Single Needle Telegraph (c 1850)**

# Communication at a Distance with Electricity and Magnetism

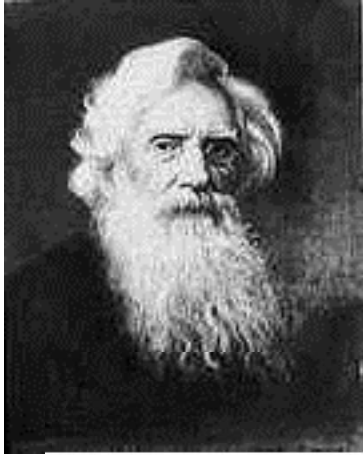


- 1831 Joseph Henry invents the first electric telegraph.
- 1843 Samuel Morse invents the first long distance electric telegraph line.
- **1858 Cyrus Field's Company Lays the Transatlantic Cable.**
- 1876 Alexander Graham Bell patents the electric telephone.
- 1894 Guglielmo Marconi improves wireless telegraphy.
- 1902 Guglielmo Marconi transmits radio signals across the Atlantic Ocean.



Brunel's Great Eastern

**Telegraph -> Telephone -> Wireless**



## ***THE TELEPHONE***

***1876 - Alexander Graham Bell invents the Telephone. He offers the patent to Western Union for \$100,000.***

***The President of the Telegraph Company, appointed a committee to investigate the offer. The report reads in part:***

***The Telephone purports to transmit the speaking voice over telegraph wires. We found that the voice is very weak and indistinct, and grows even weaker when long wires are used between the transmitter and receiver.***

***Technically, we do not see that this device will be ever capable of sending recognizable speech over a distance of several miles.***

***Bell wants to install a "telephone device" in every city. The idea is idiotic on the face of it.***

***"We do not recommend its purchase."***



# Early Telephone Instruments

**Ericsson "Eiffel Tower"  
Telephone, 1885**



**11 digit Potbelly  
Dial Candlestick  
Strowger 1905**



**Dial Candlestick  
Automatic Electric  
1921**



**Footnote: Western Electric  
Engineers were  
Wrong! Very Wrong!**

<b>1877:</b>	<b>5 Phones</b>
<b>1894:</b>	<b>250,000 Phones</b>
<b>1906:</b>	<b>7,500,000 Phones</b>

# Electrical Communication at a Distance!

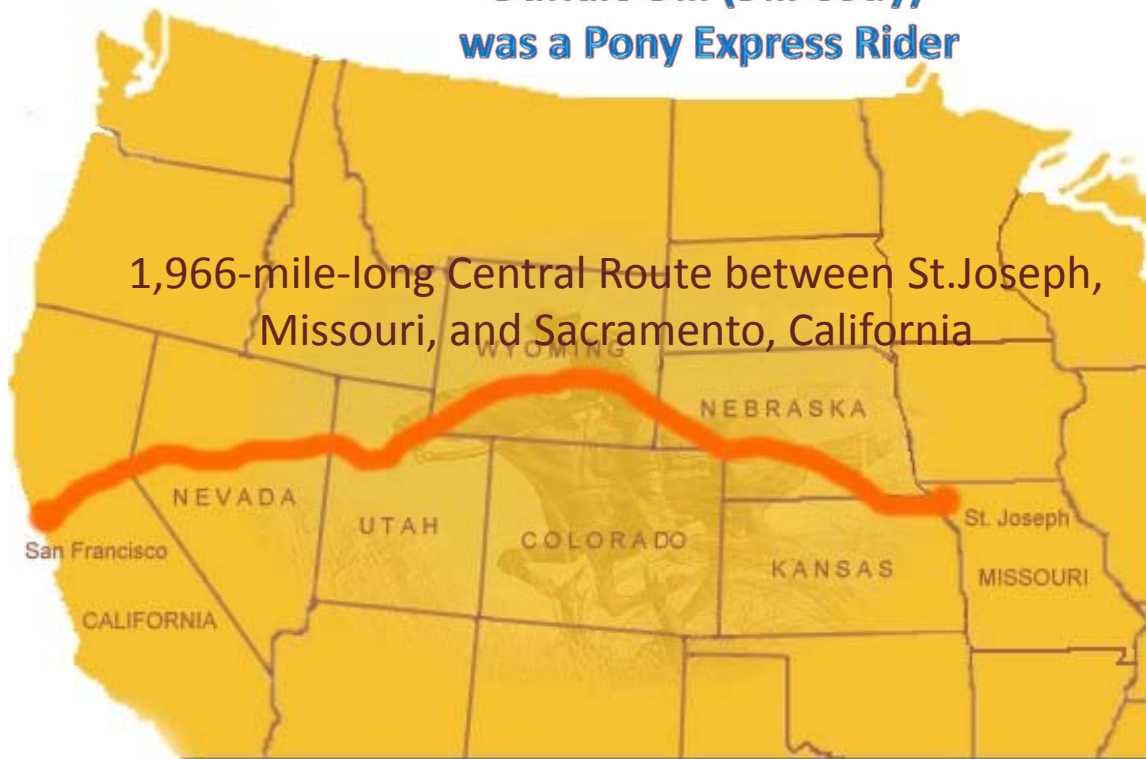
## It All Started with the Telegraph!

1837	Cooke and Wheatstone patent telegraph in England.
1838	Morse's <b>Electro-Magnetic Telegraph patent</b> approved.
1843	<b>First telegraph message</b> sent between Washington and Baltimore.
1846	First commercial telegraph line completed. Lines ran from New York to Washington.
1851	New York and Mississippi Valley <b>Printing Telegraph Company</b> . Became Western Union.
1851	Telegraph first used to coordinate train departures.
1859	<b>Transatlantic cable</b> is laid from Newfoundland to Ireland. Fails after 23 days.
1861	Transcontinental telegraph completed. <b>Pony Express Disbanded 2-days Later!</b>
1867	Stock <b>ticker tape</b> service inaugurated.
1870	Western Union introduces the money order service.
1876	Alexander Graham Bell patents the telephone. Upcoming Competition for Telegraph
1924	AT&T offers <b>Teletype</b> system.
1926	Inauguration of direct stock ticker circuit from New York to San Francisco.
1930	High-speed <b>ticker tape</b> can print 500 words per minute.
1962	Western Union offers <b>Telex</b> for international teleprinting (Teleprinter Exchange).
1974	Western Union places Westar satellite in operation.
2006	Western Union <b>discontinues all Telegram</b> and Commercial Messaging services.

# Pony Express Route: 10.5 Days of Hard Riding 21 Days by Overland Stage Coach

Riders were paid \$25 per week.  
Unskilled labor wages at the time  
was about \$1 per week.

Buffalo Bill (Bill Cody)  
was a Pony Express Rider





# The Pony Express



- In March 1860, William H. Russell newspapers advertisements announced:  
**"Wanted: Young, skinny, wiry fellows not over 18. Must be expert pony riders willing to risk death daily. Orphans preferred."** Riders had to swear not to cuss, fight, or abuse their animals.
- Starting on April 3, 1860, the Pony Express ran through parts of Missouri, Kansas, Nebraska, Colorado, Wyoming, Utah, Nevada, and California. On an average day, a rider covered 75 to 100 miles. He changed horses at relay stations 10 or 15 miles apart, transferring himself and his mail pouch to the new mount, all in one leap.
- **The first mail by Pony Express from St. Joseph to Sacramento took 10 1/2 days,** cutting the Overland Stage time by more than half. The fastest delivery was in March 1861, when President Abraham Lincoln's inaugural address was carried in 7 days and 17 hours.
- **The Pony Express operated from April 3, 1860 through October 24, 1861, when the transcontinental telegraph line was completed.**  
The Pony Express survives as a legend in the history of the West.

# The Telegraph Network: Late 19-th and Early 20-th Century Enabling Engine of Finance, Commerce, and Transportation

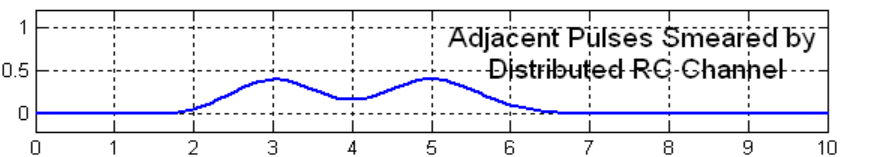
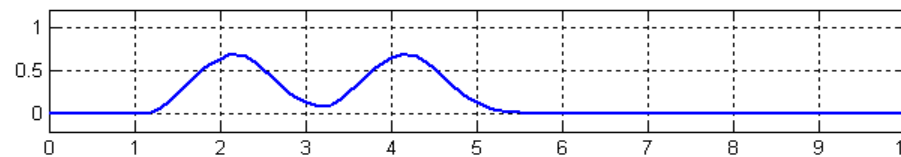
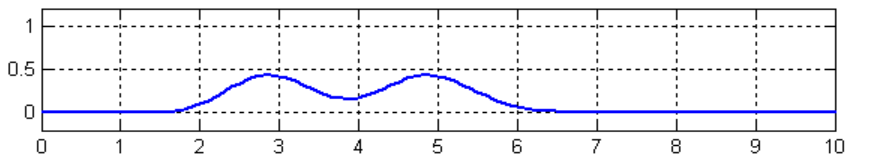
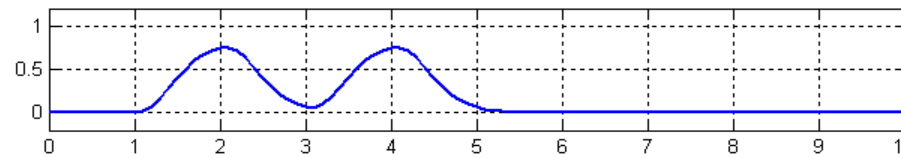
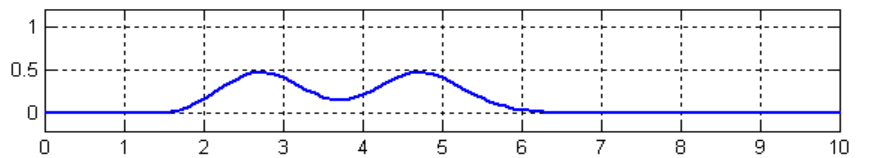
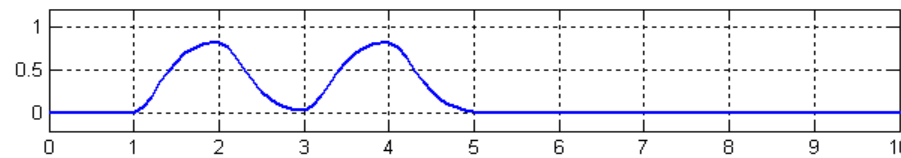
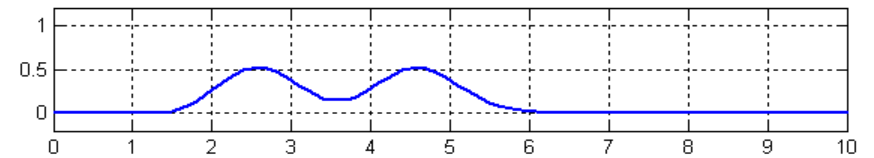
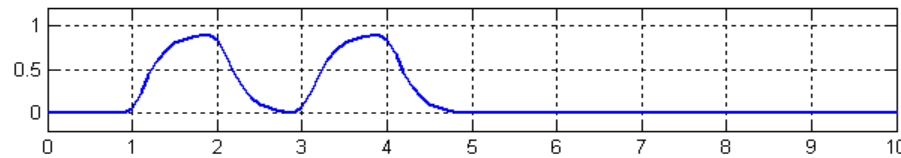
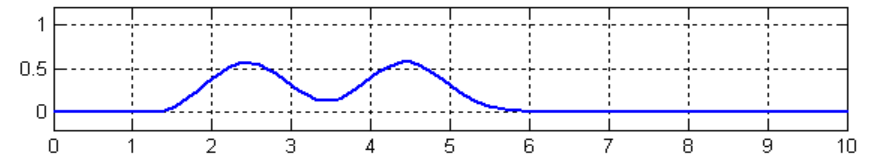
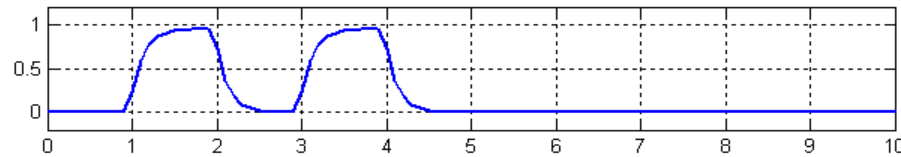
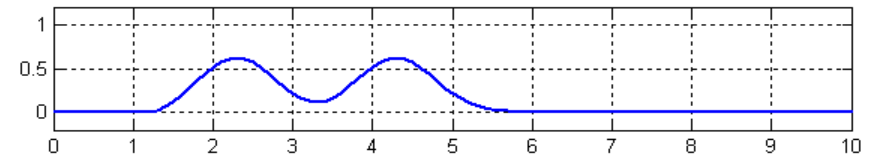
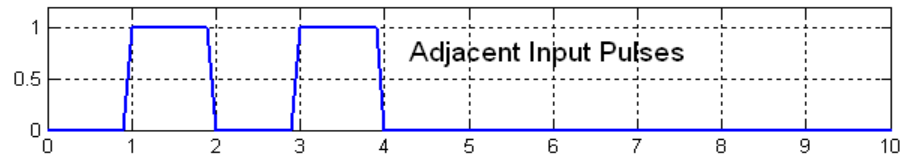
Messages Handled by the Telegraph Network: 1870-1970

Date	Messages Handled	Date	Messages Handled
1870	9,158,000	1930	211,971,000
1880	29,216,000	1940	191,645,000
1890	55,879,000	1945	236,169,000
1900	63,168,000	1950	178,904,000
1910	75,135,000	1960	124,319,000
1920	155,884,000	1970	69,679,000

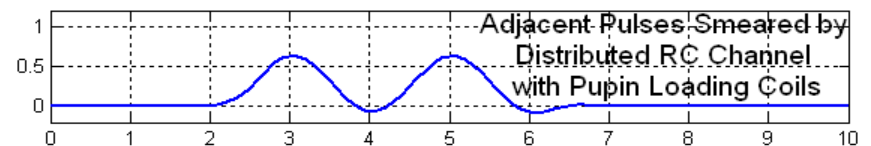
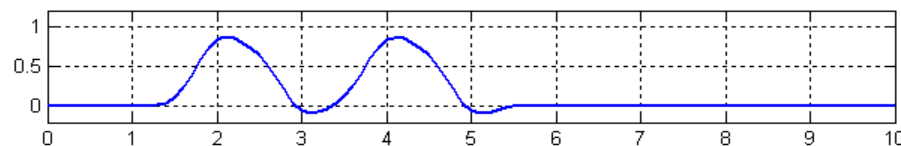
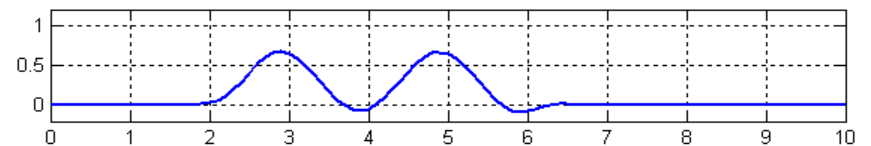
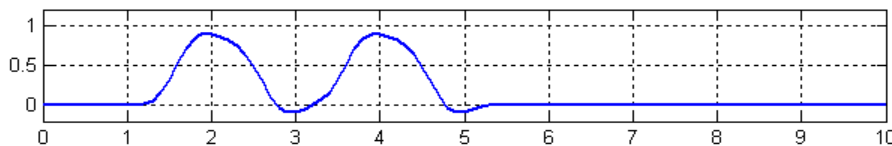
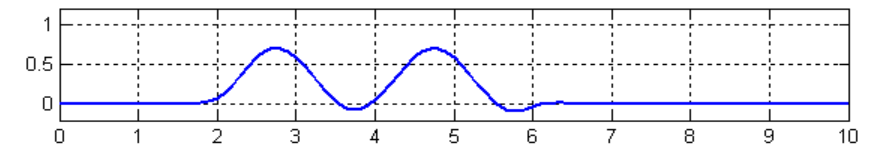
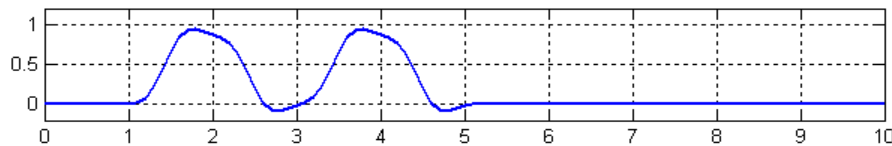
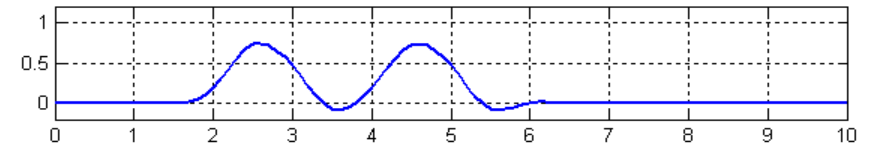
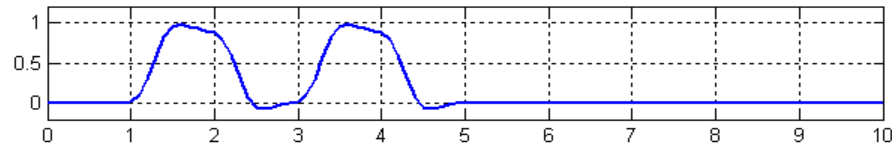
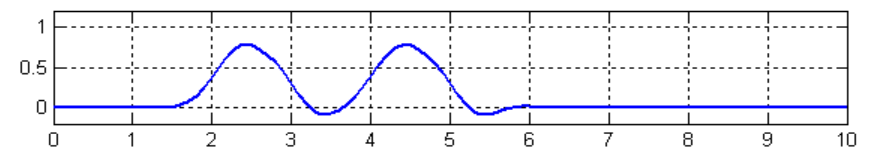
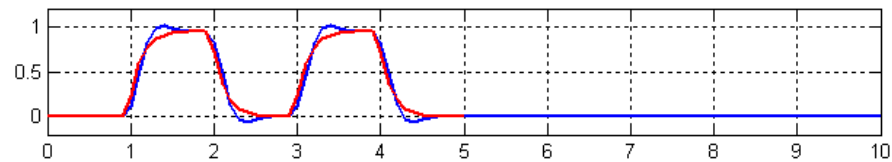
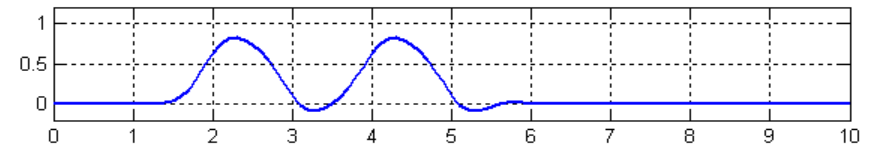
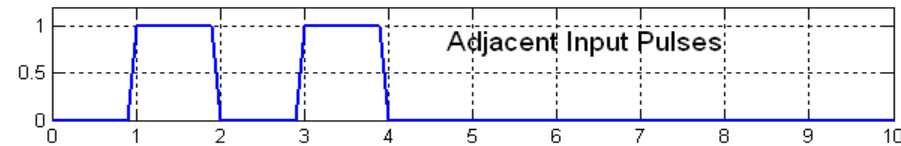
Teletype, Telegraph, Telex, Stock Ticker-Tape  
**Printed Records** of Communication



# Smearing Of Telegraph Pulses Due to Impulse Response of Distributed RC Cable Channel



# Smearing Of Telegraph Pulses Due to Impulse Response of Distributed RC Cable Channel Compensated by Pupin Loading Coils



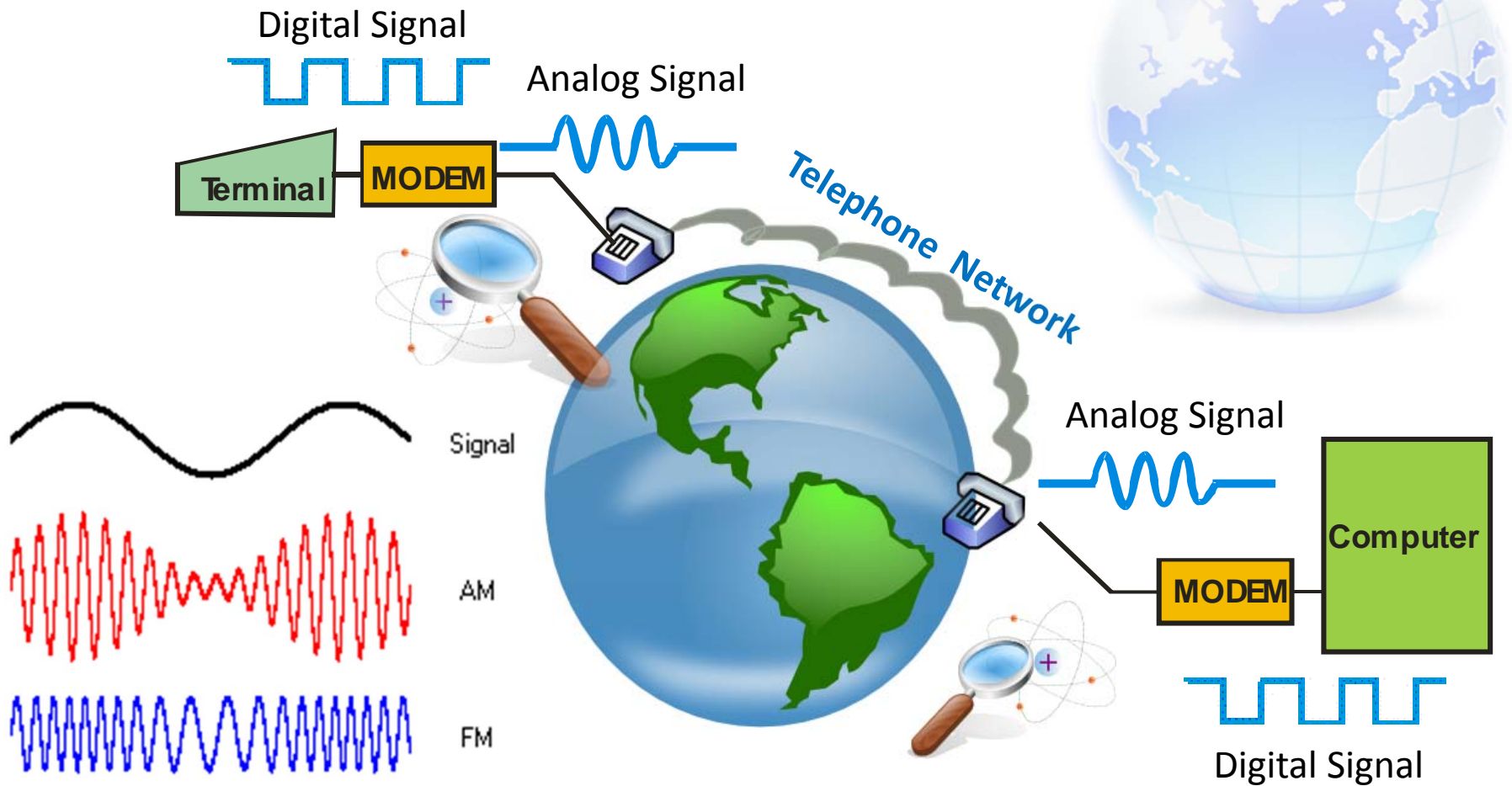
# History & Birth of Modems



- Modems grew out of the need to connect teletype machines over ordinary phone lines instead of more expensive leased lines which had previously been used for current loop-based **teleprinters** and **automated telegraphs**.
- Mass-produced modems in the United States began as part of NORAD's SAGE air-defense system in 1958, **connecting terminals** at various airbases, radar sites, and command-and-control centers in the U.S. and Canada.
- SAGE modems were essentially commercial acoustically coupled Bell 101, 110 baud modems.
- Modem: Acronym formed from two words. Modulator and Demodulator  
Modulator and Demodulator ☺    Mod Dem ☺    Modem

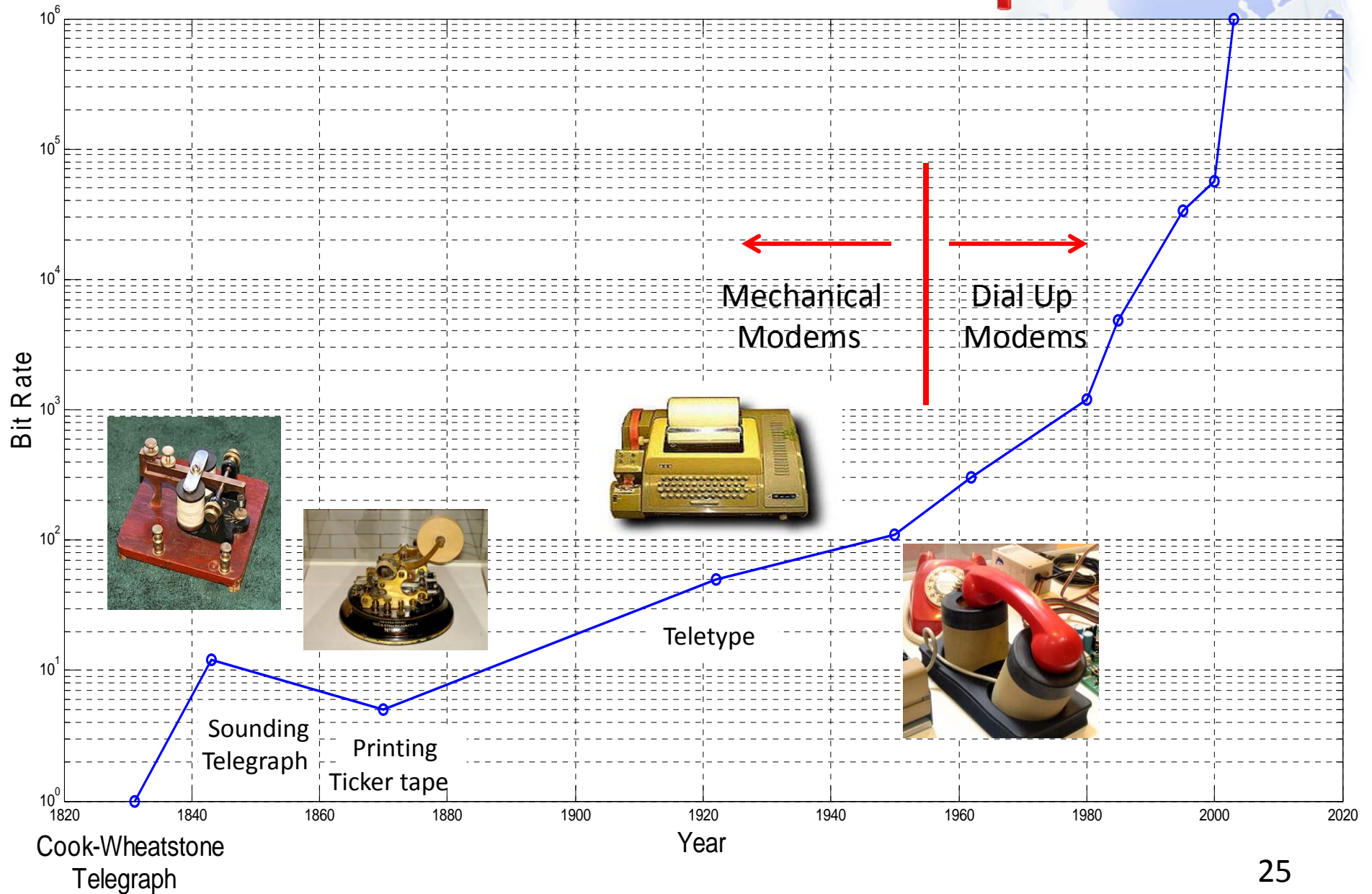
Norad: North American Aerospace Defense Command  
SAGE: Semi-Automatic Ground Environment

# Modems



Modems are the **interface**  
between a computer and the **telephone line**.

# Wire-Line Modem Speeds



# **Communication at a Distance by Electromagnetic Radiation, (Radio or Wireless)**

**1894 Guglielmo Marconi  
improves wireless  
telegraphy.**

**1902 Guglielmo Marconi  
transmits radio signals  
across the Atlantic Ocean.**

**1914 First cross continental  
telephone call made.**

**1916 First radios with tuners  
to select different stations.**

**1930 First television broadcasts  
in the United States.**



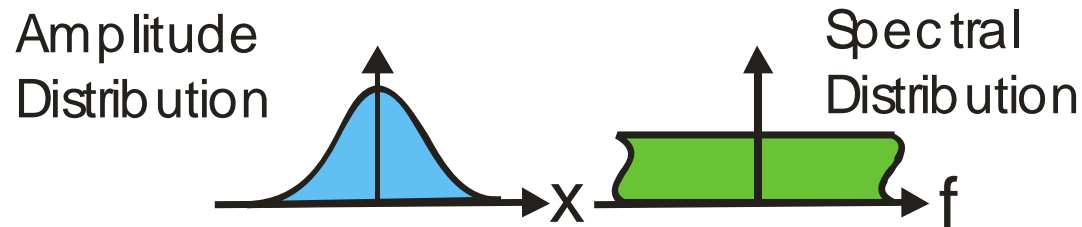


## **Russian Astrophysicist Iosif Shklovski Commented:**

**"For a few decades after invention of the first radio-amplifier the total level of radio-emission from earth increased millions of times in comparison with the normal level of emission of a 300 Kelvin-degree planet. For the shortest time the Earth became #1 source of the radio-emission in the solar system "**

**It means that, if someone is looking through a radio-telescope at the Solar system from another part of our galaxy, he would register the radio explosion that looks like the birth of a new star on the Earth planet.**

# The Basic Communication System





# The Wireless Channel



**The Wireless Channel Propagates Wave Shape Energy Between Remote Locations**

**Radio Waves are Not Constrained in Space and Share the Medium with Others**

**Our First Model of the Channel is:**

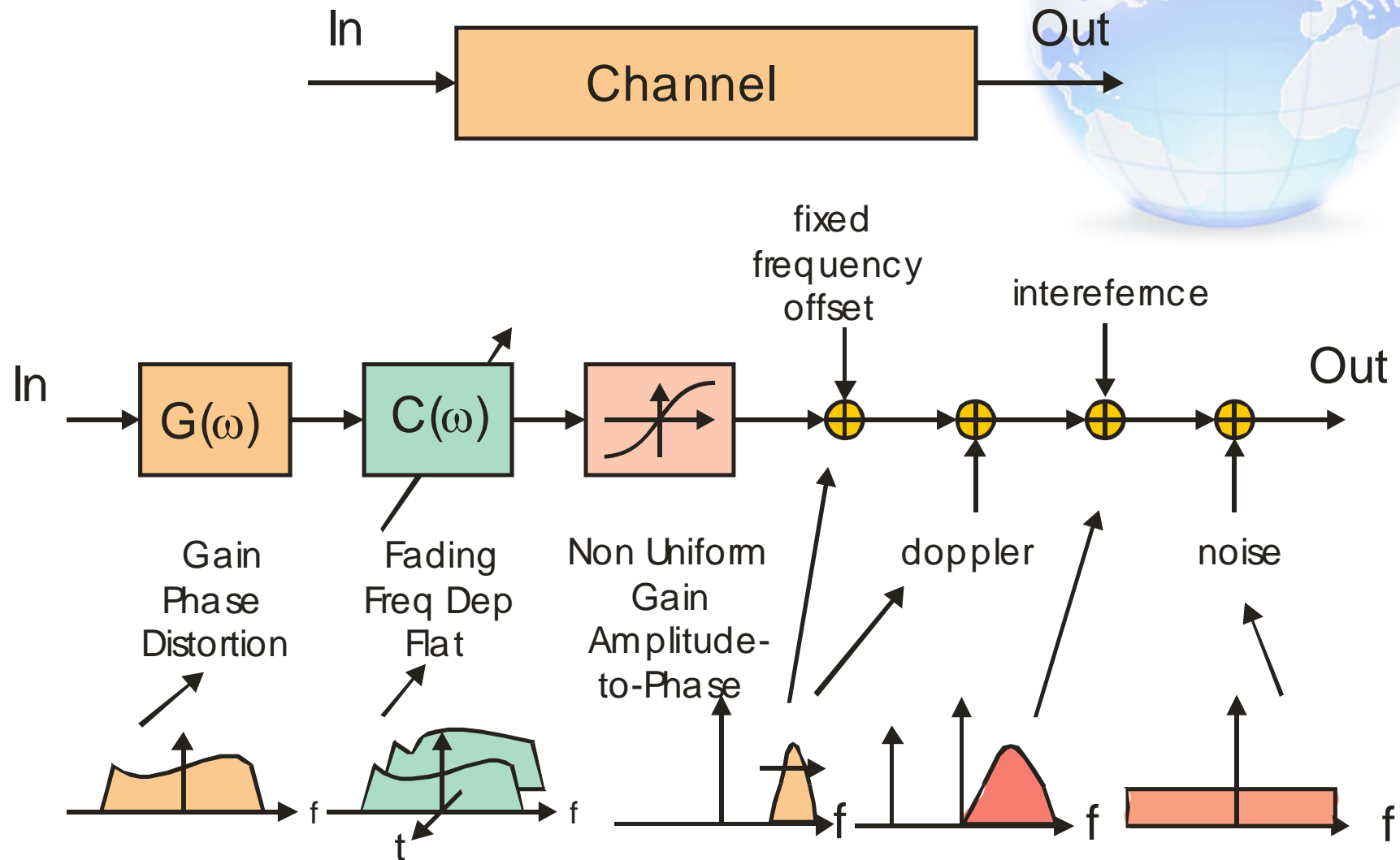
**Linear, Time Invariant, with White, Gaussian, Additive Noise**

**If we Include Transmitter and Receiver in the Channel Model we find**

**Our Second Model of the Channel is:**

**Non Linear, Time Varying, with Non White, Non Gaussian, Additive Noise**

# More Inclusive Channel Impairments



# Modern Physical Layer Modem Recipe:

Add these Ingredients, Stir, Bake for 20 Minutes at 300°. Let Cool! Enjoy your Modem!

## ➤ First Tier Processing: Modulation and Demodulation

- Shaping Filters
- Interpolation
- Spectral Translation
- Signal Conversion



DSP Genie-1

## ➤ Second Tier Processing: Parameter Estimation

- Carrier Frequency and Phase Synchronization
- Timing Frequency and Phase Synchronization
- Automatic Gain Control
- SNR Estimate



DSP Genie-2



DSP Genie-3

## ➤ Third Tier Processing: Channel and Hardware (Dirty RF)

- Equalization
- I-Q Balance
- DC-Cancel
- Peak-to-Average Ratio (PAPR) Control
- Predistortion
- Interference Suppression
- Intrusion Suppression
- Power Amplifier Linearization



DSP Genie-4



DSP Genie-5





# Modem Ingredients



- Signal Strength Indicator
- Log Amplifier
- Signal Presence (Squelch)
- Overdrive Protection
- Automatic Gain Control (AGC)
- Logarithm and Exponentiation
- Amplitude Demodulation
- Frequency Demodulation
- Phase Demodulation
- Carrier Frequency & Phase Recovery Phase Locked Loop
- Symbol Timing Frequency & Phase Recovery Phase Locked Loop
- ATAN (Nobody Does This!)
- Comparator
- Delay
- DC Cancel
- I-Q Gain and Phase Balance
- Interleaved ADC Gain and Timing Balance
- Predistortion
- Peak-to-Average Power Ratio Control
- Interference Suppression
- Intrusion Suppression
- Power Amplifier Linearization
- Signal-to-Noise Ratio Estimate (Nobody Does This! ) (I'm Shocked!)
- Analog-to-Digital Converter (ADC)
- Digital-to-Analog Converter (DAC)
- Fast Fourier Transform (FFT)
- Interpolator (Sample Rate Change)
- Direct Digital Synthesizer (DDS)
- Channelize

# Important Technology Developments



- **Pupin Loading Coils**
- **Echo Cancellers**
- **Fixed Equalizers**
- **Adaptive Equalizers**
- **Phase Locked Loops**
- **$\mu$ -Processors**
- **A-to-D Converters**
- **D-to-A Converters**



# Why Are There So Many Modulation Options?



## •Analog Modulation

- AM, Amplitude Modulation
- SSB, Single Sideband Modulation
- VSB, Vestigial Sideband Modulation
- QAM, Quadrature AM
- FM, Frequency Modulation
- PM, Phase Modulation
- Space Modulation  
(ILS Instrument Landing System)

## • Spread Spectrum Modulation (SS)

- CSS, Chirp Spread Spectrum
- DSSS, Direct-Sequence Spread Spectrum
- FHSS, Frequency-Hopping Spread Spectrum
- PWM, Pulse-Width Modulation
- PCM, Pulse-Code Modulation

## •Digital Modulation

- OOK, On-Off Keying
- FSK, Frequency Shift Keying
- DTMF, Dual-Tone Multi-Frequency
- MFSK, Multiple Frequency Shift Keying
- ASK, Amplitude Shift Keying
- PSK, Phase Shift Keying
- BPSK, Binary PSK
- QPSK, Quadrature PSK
- OQPSK, Offset PSK
- $\pi/4$ -QPSK,
- DQPSK, Differential QPSK
- DPSK, Differential PSK
- QAM, Quadrature Amplitude Modulation
- MSK, Minimum (Phase) Shift Keying
- GMSK, Gaussian MSK
- CPM, Continuous Phase Modulation
- PPM, Pulse Position Modulation
- TCM, Trellis Coded Modulation
- OFDM, Orthogonal Frequency Division Multiplex
- SC-OFDM, Single Carrier OFDM

# Reasonable Goals

- Maximize transmission Bit Rate
- Minimize probability of bit error
- Minimize system Bandwidth
- Minimize Size, Weight, & Power
- Maximize system utilization
- Minimize system complexity
- Minimize cost

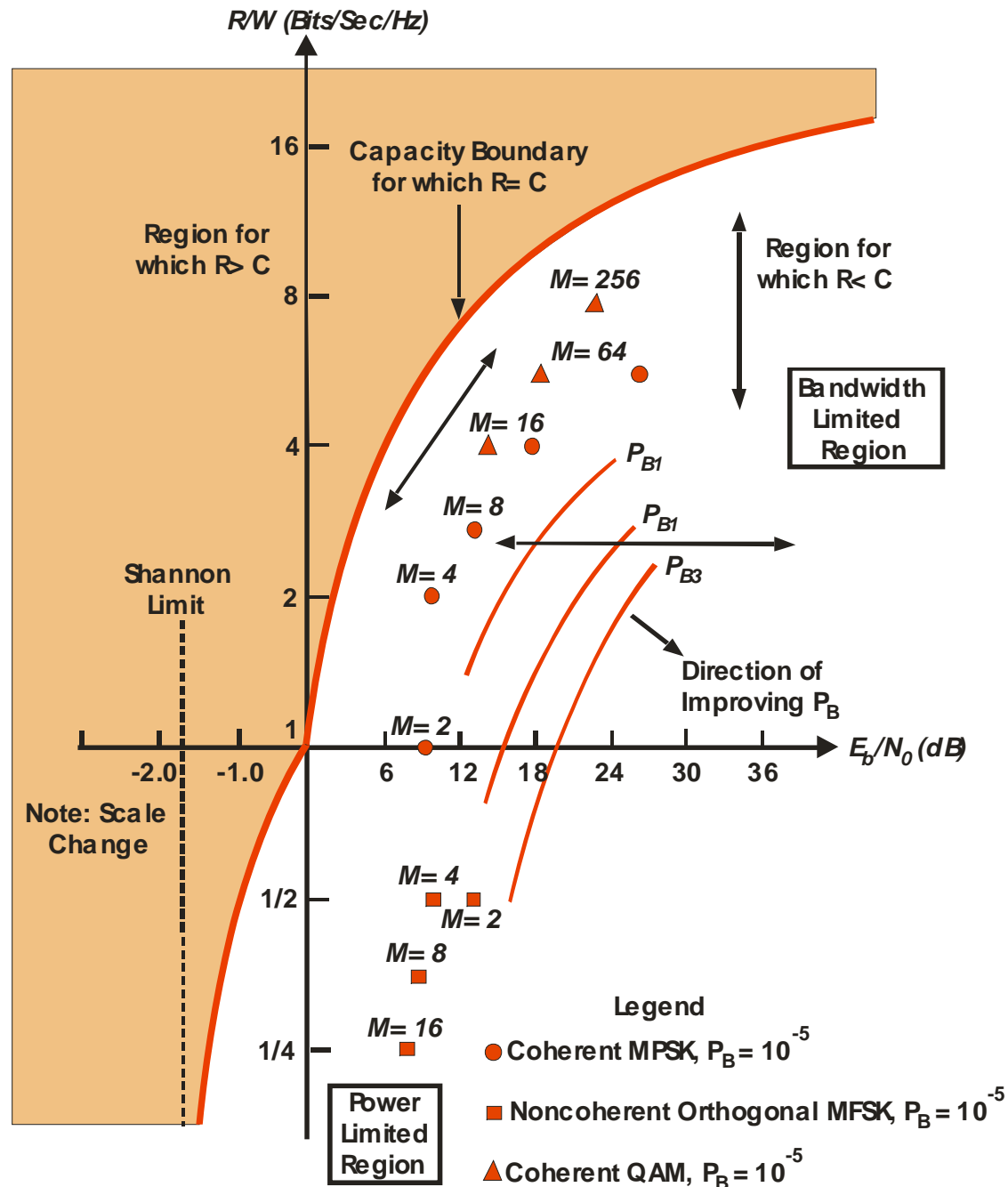


# Boundary Conditions



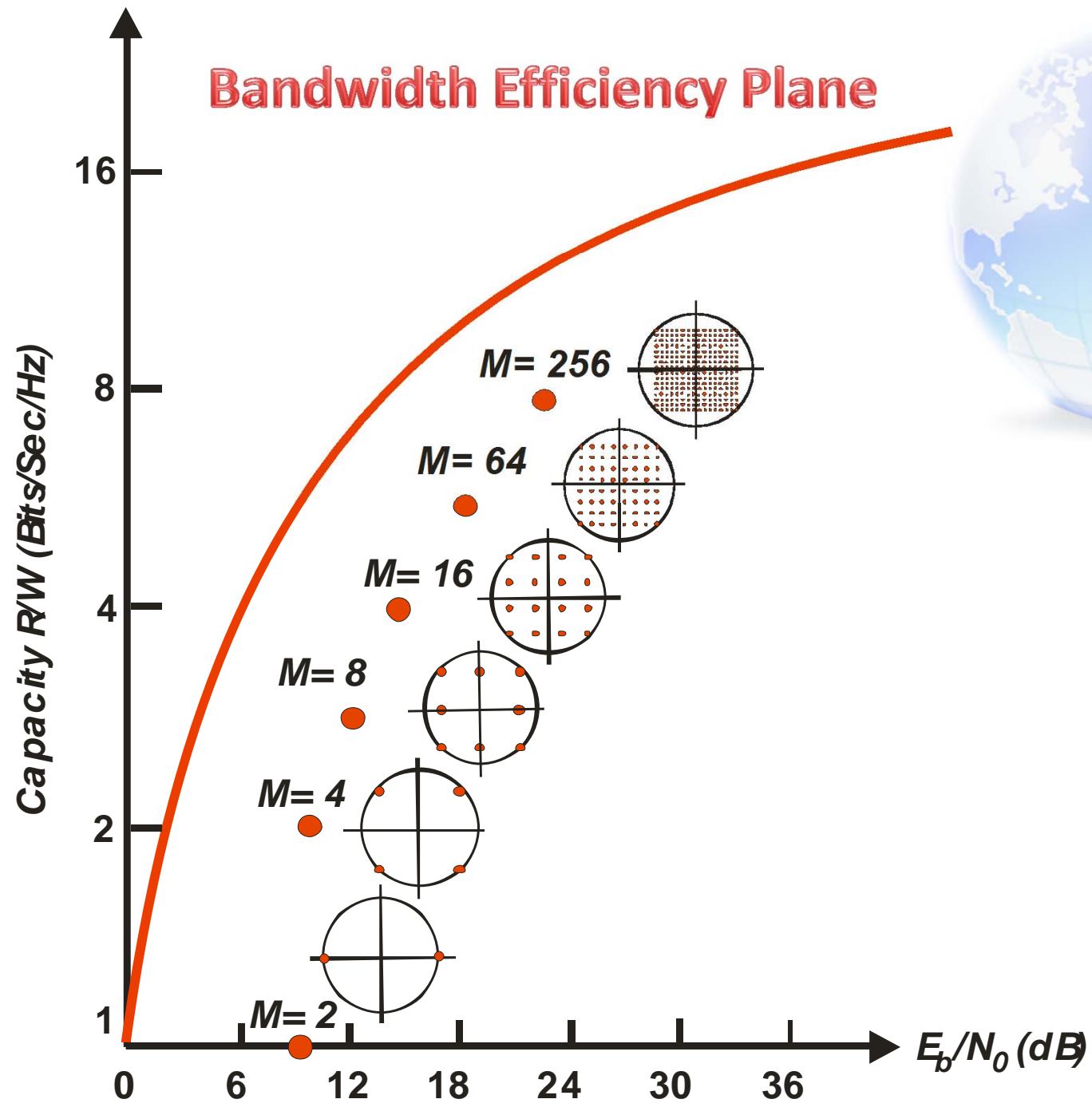
- Nyquist Bandwidth Requirement
  - Shannon-Hartley Capacity Theorem
  - Technology Limitations
  - Regulatory and Treaty Limitations
  - Deployment Restrictions
- (Laws of Physics, Antenna Placement,  
Satellite orbits, Etc.)



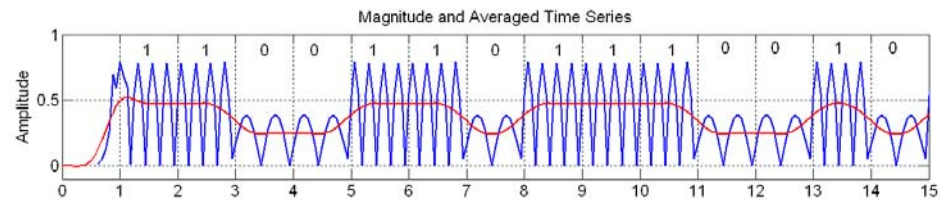
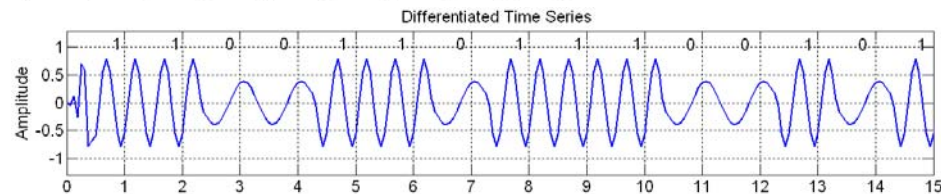
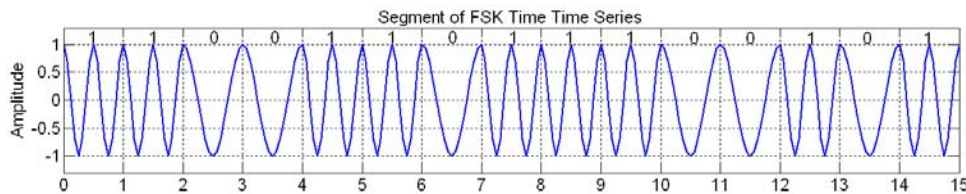
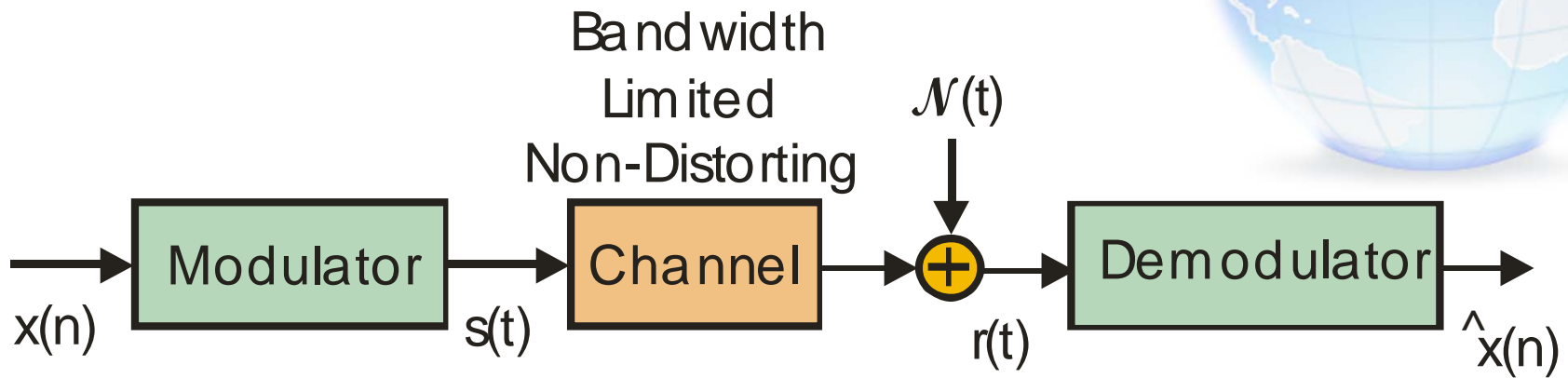


## Bandwidth Efficiency Plane

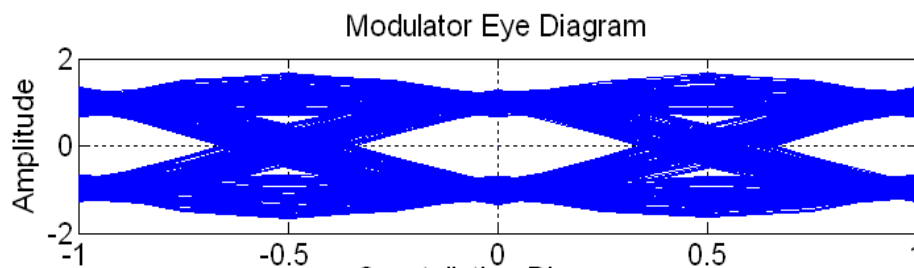
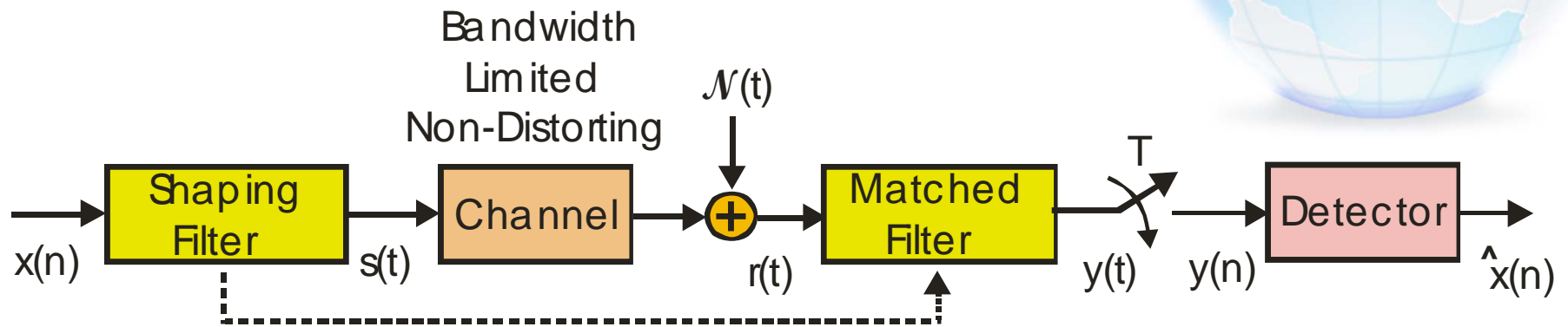
Complements of Bernard Sklar



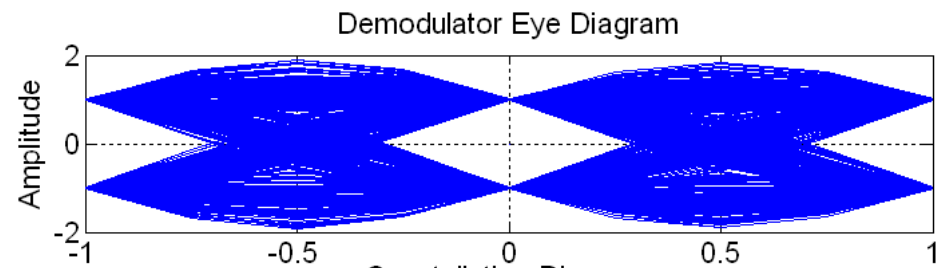
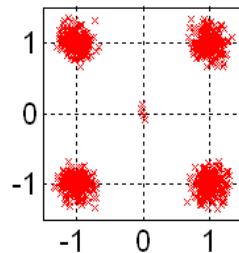
# FSK Modulator-Channel-AWGN-Demodulator



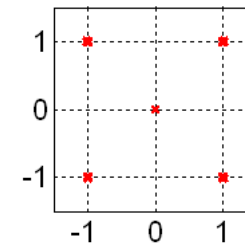
# Shaping Filter in Modulator, Matched Filter in Demodulator



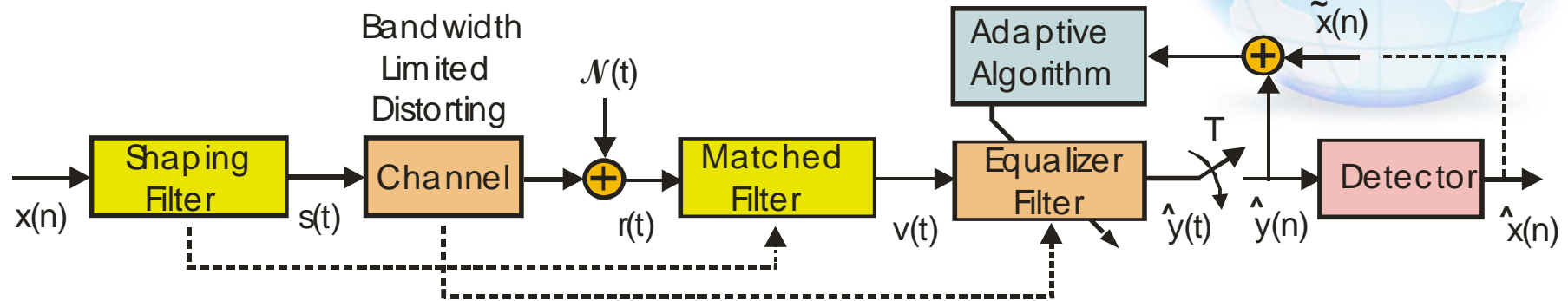
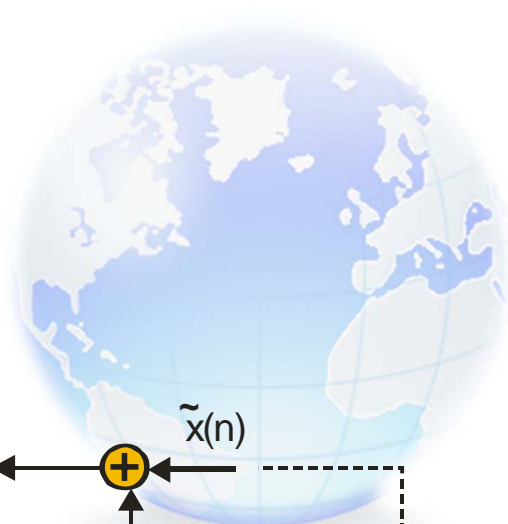
Constellation Diagram



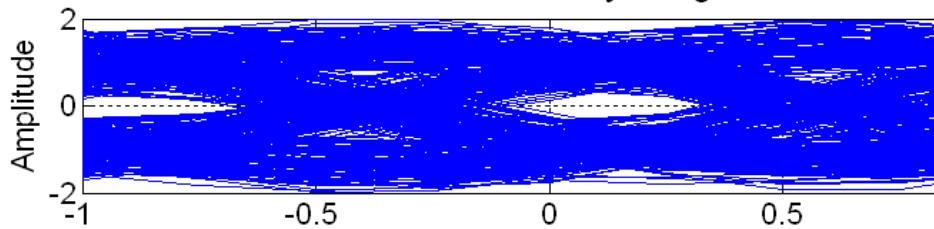
Constellation Diagram



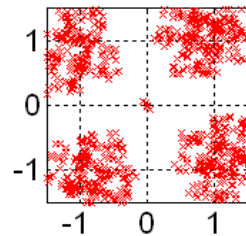
# Distorted Output of Channel and Output of Channel Equalizer



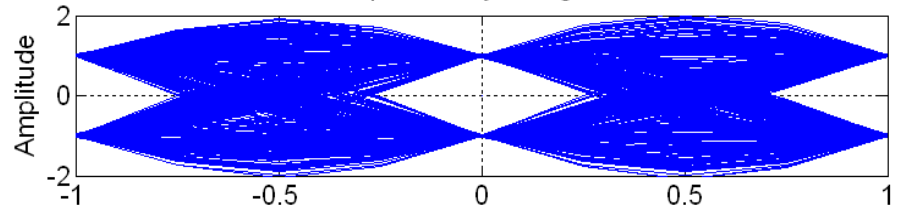
Channel Distorted Eye Diagram



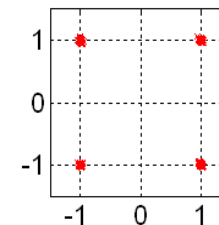
Channel Distorted Constellation



Equalized Eye Diagram

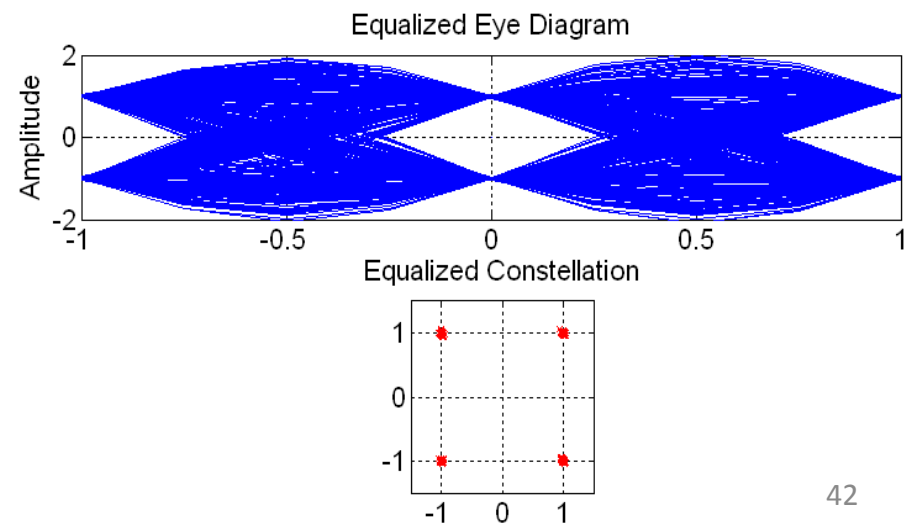
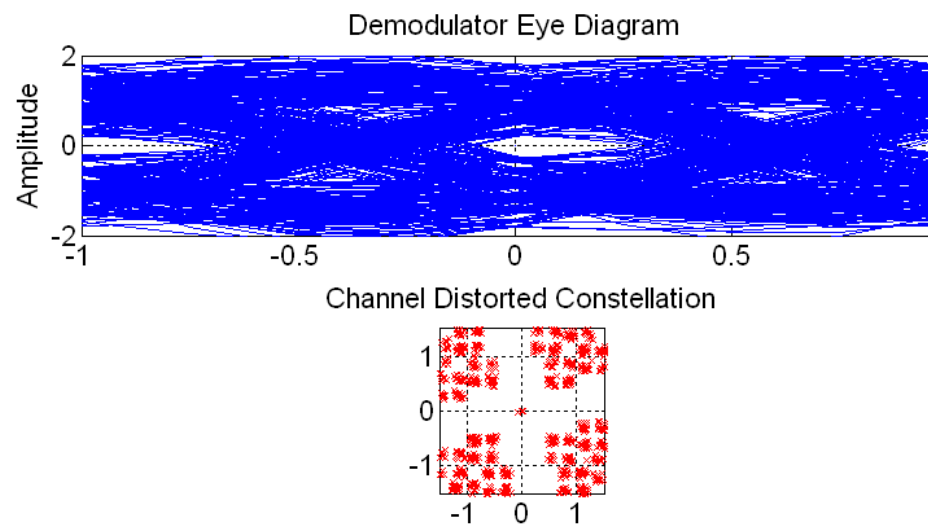
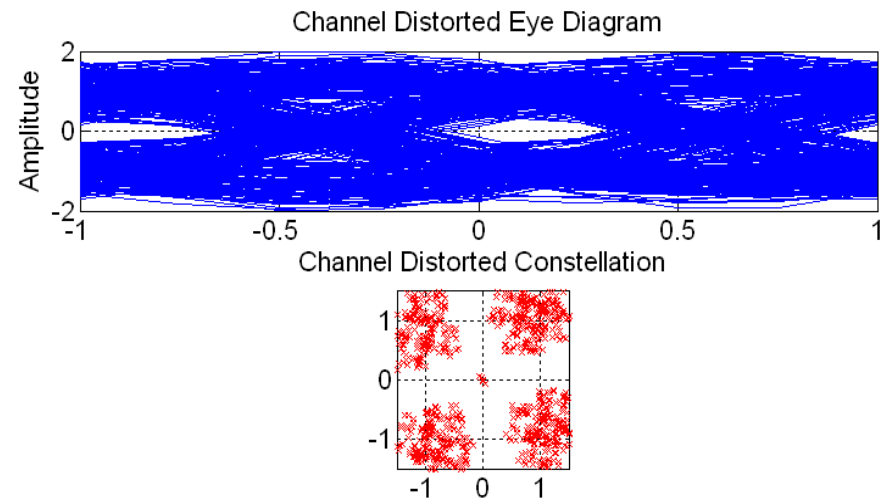
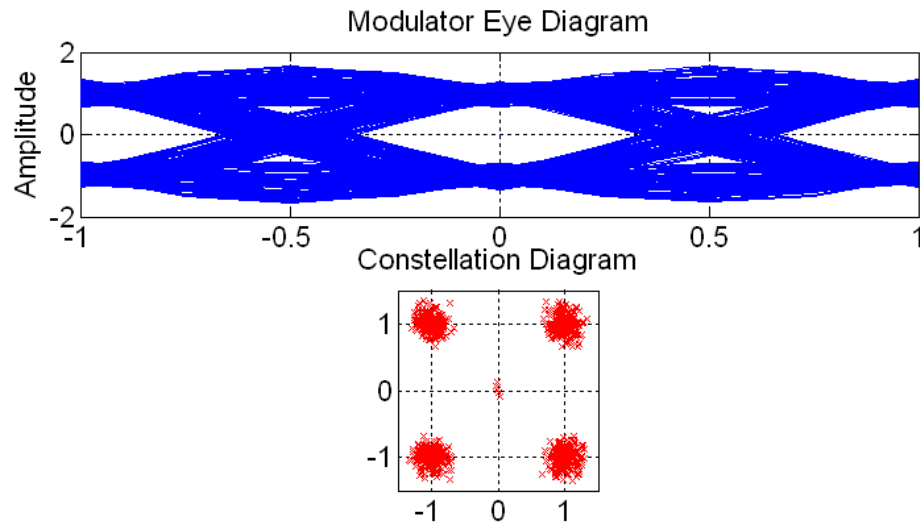


Equalized Constellation



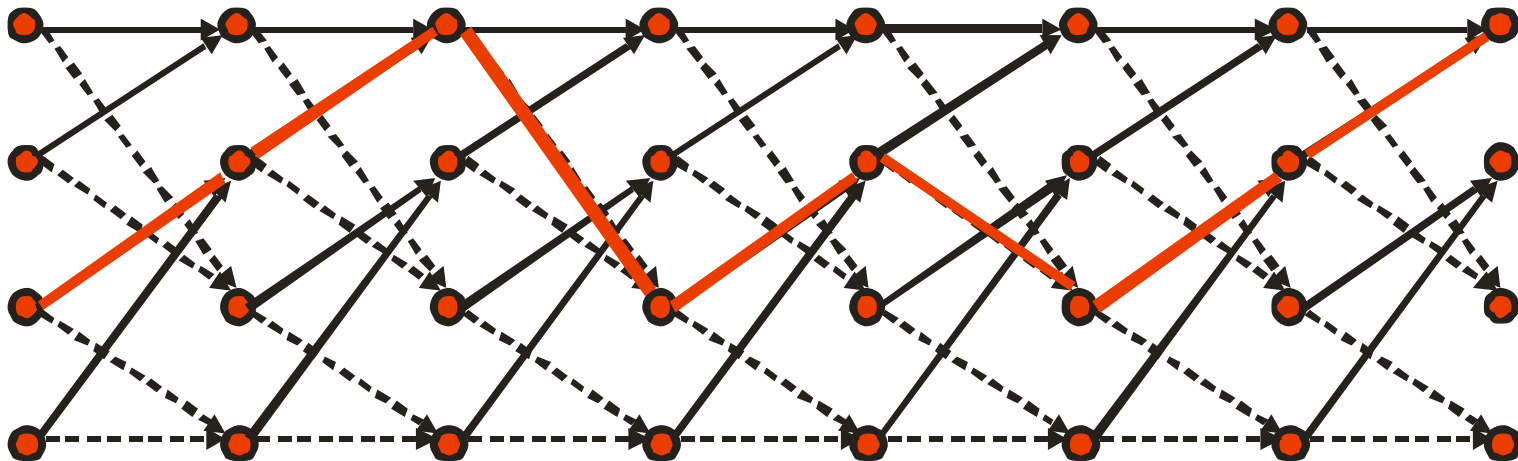
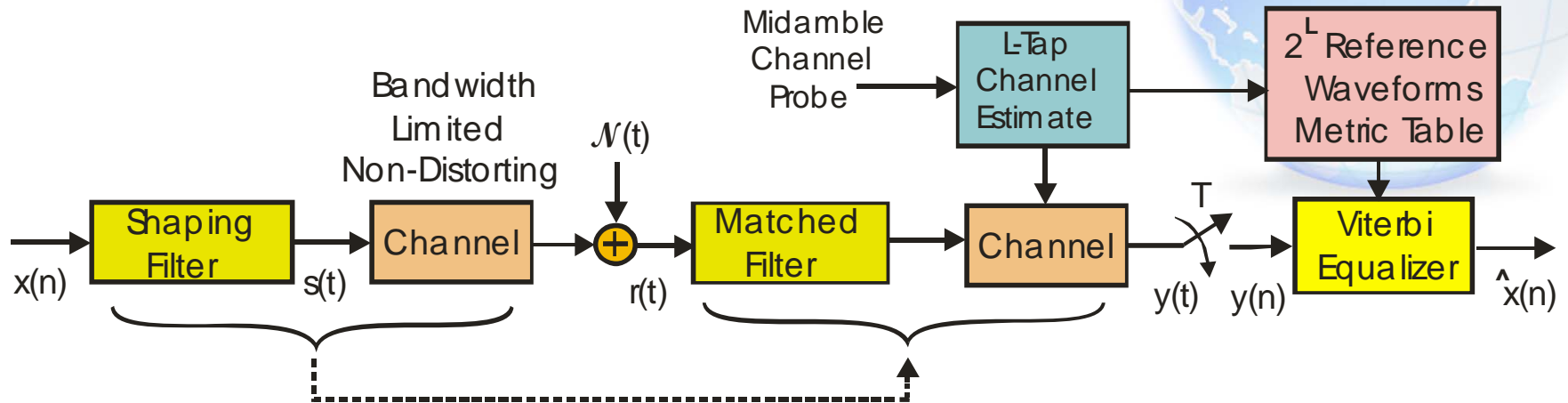


# Eye Diagrams: Channel Input and Output Matched Filter and Equalizer Outputs

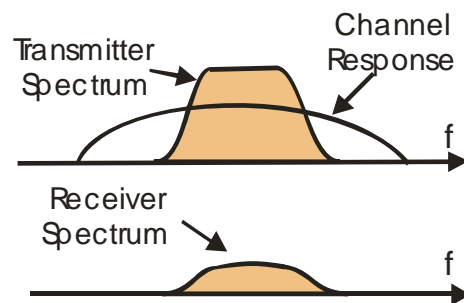
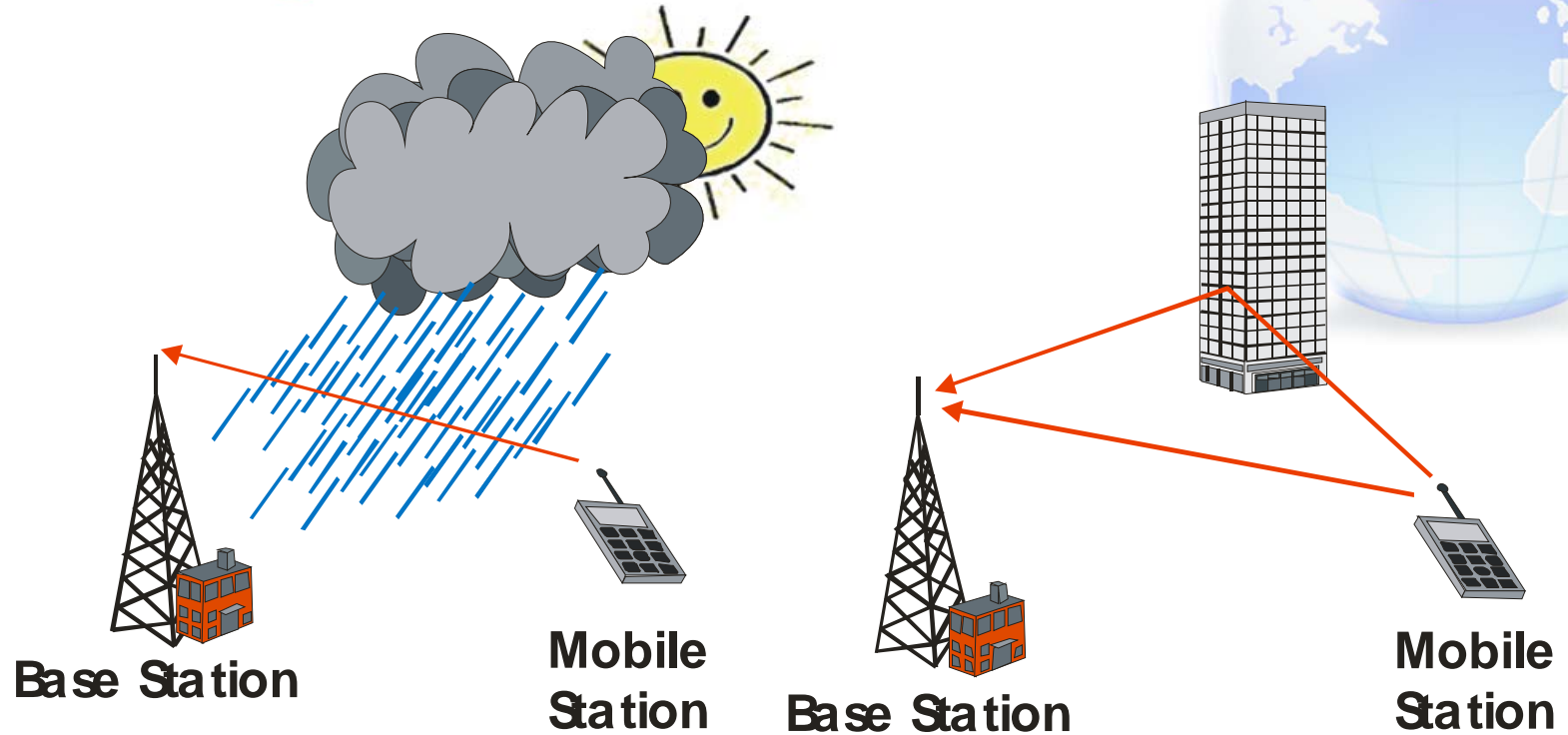


# Viterbi Equalizer

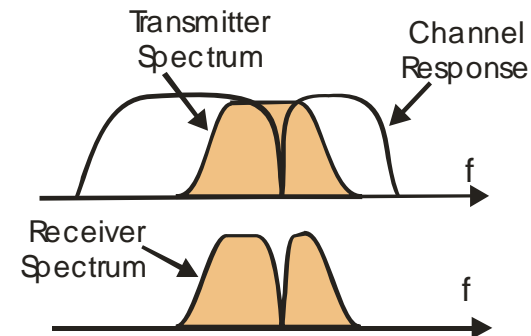
## Maximum Likelihood Estimate of Data Sequence



# Flat Fading and Frequency Selective Fading

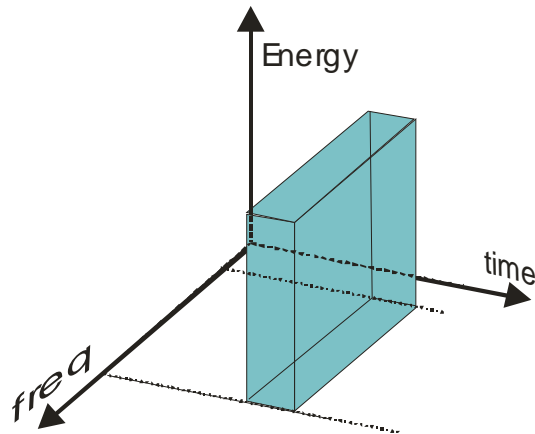


Flat Fading

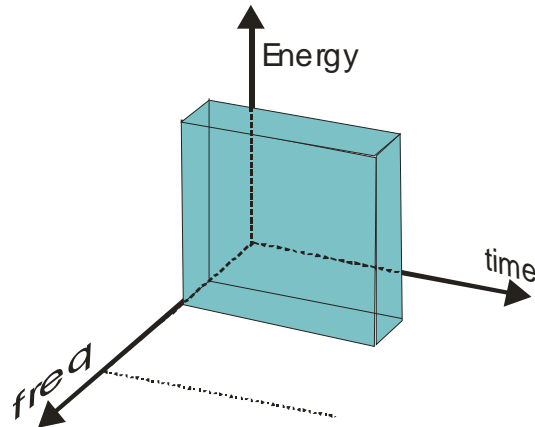


Frequency Selective Fading

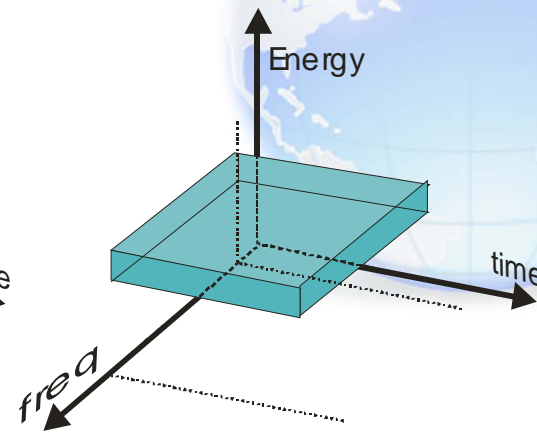
# Share Time-Bandwidth Resources Among Multiple Users



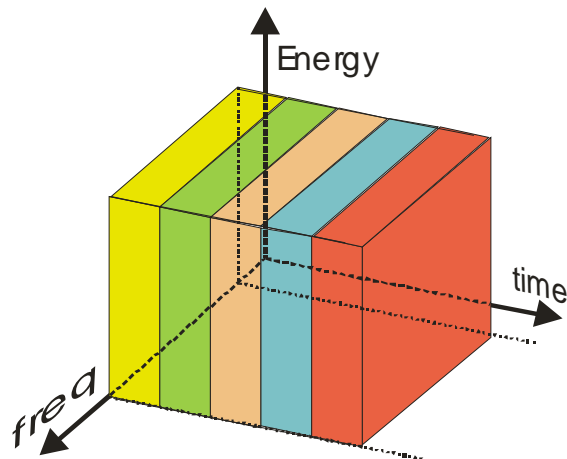
TDMA



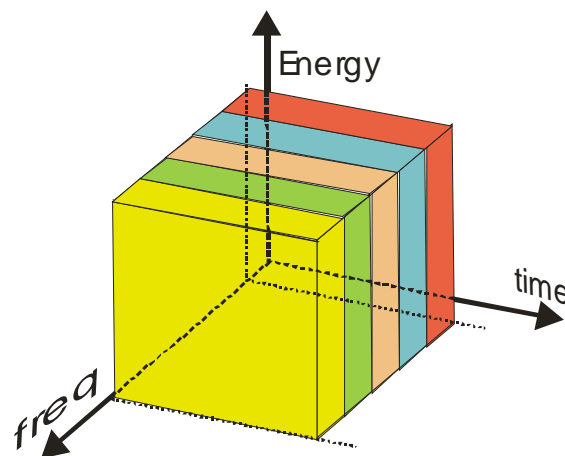
FDMA



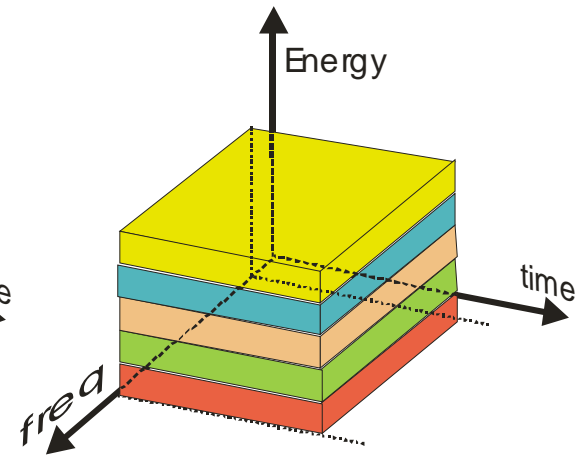
CDMA



TDMA

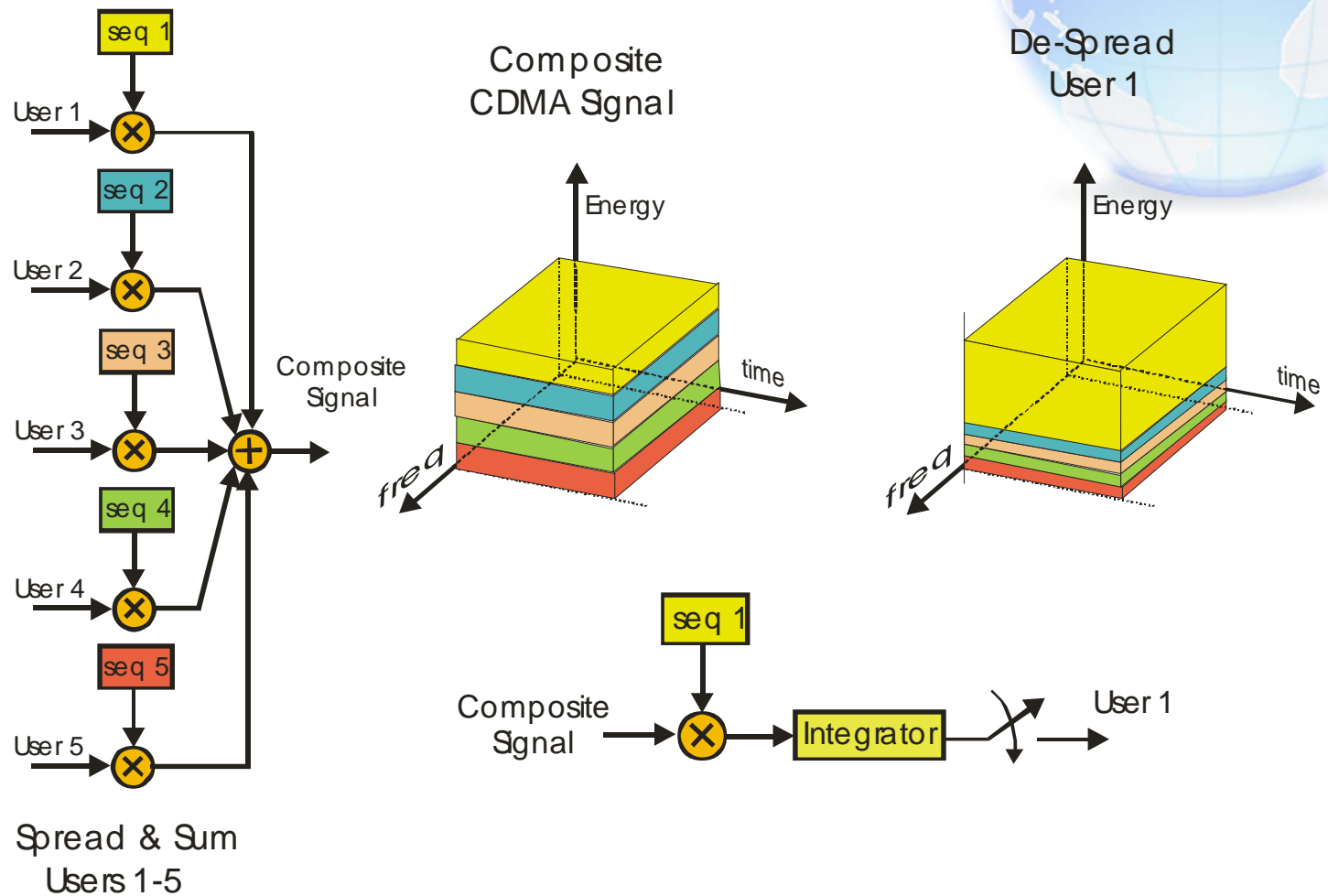


FDMA



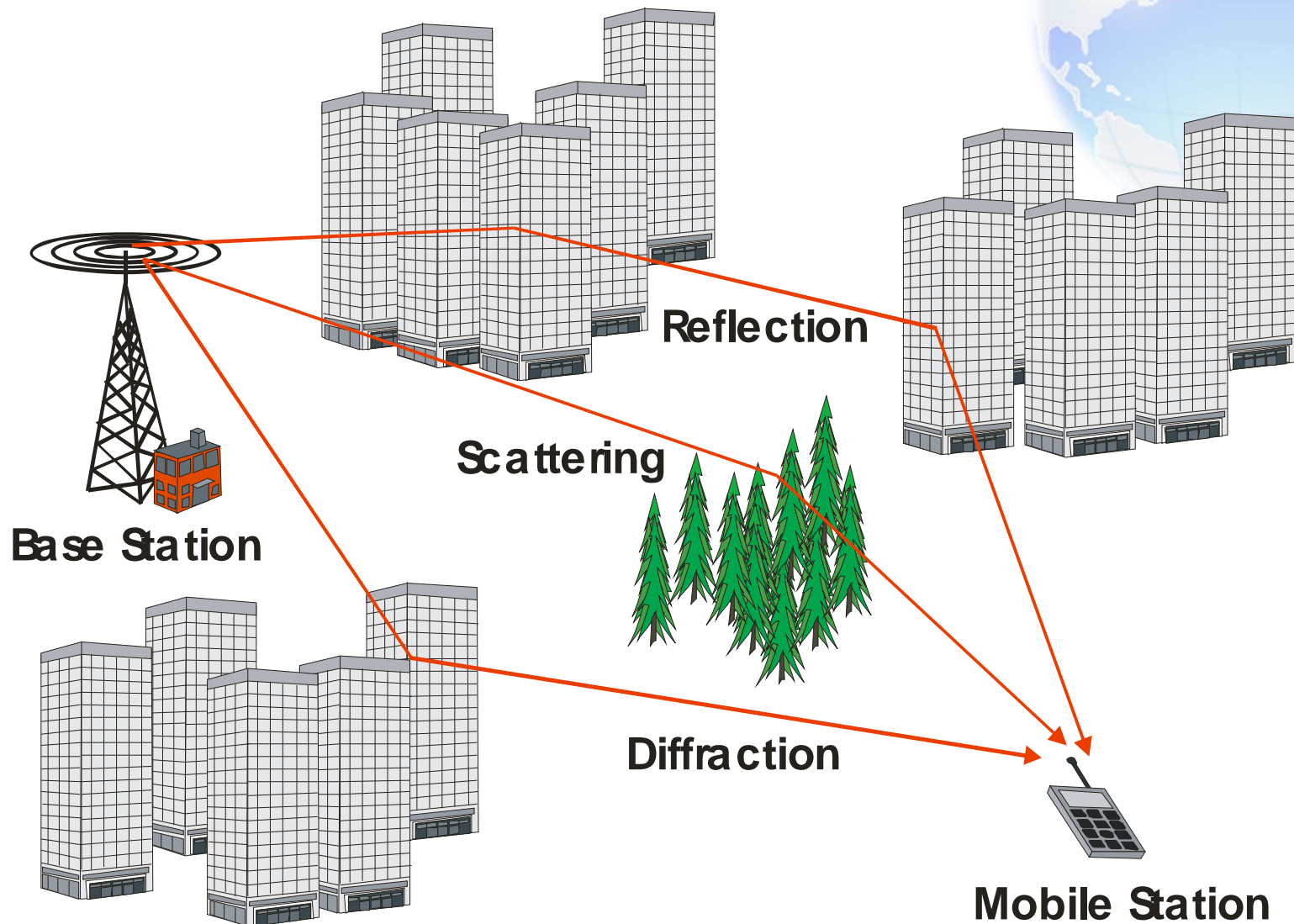
CDMA

# CDMA: Direct Sequence Spread Spectrum, DS-SS



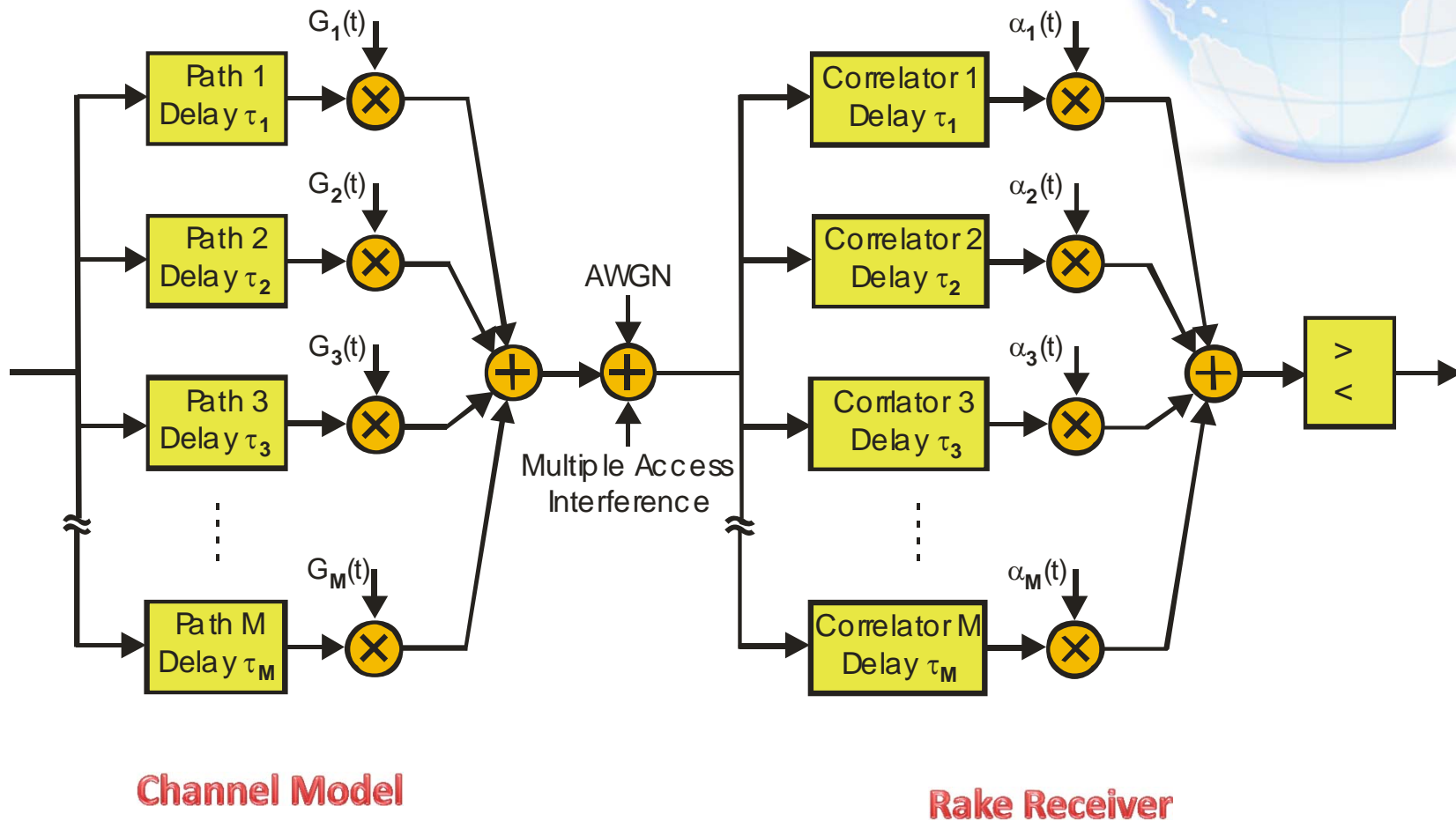


# Propagating Signal Through Multipath Environment



# Multipath Channel Model and Rake Receiver

## Correlators aligned with Multipath Signals



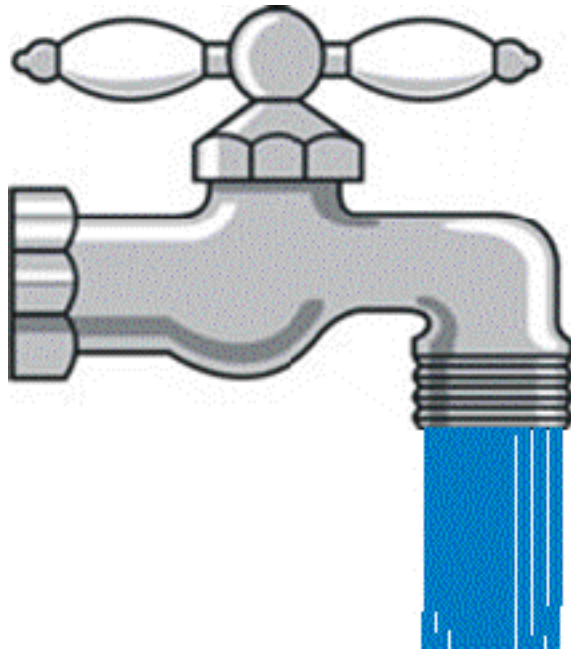
# Modulation Evolution

- **QAM** Shaping Filters Minimize Bandwidth to Share Channel Resource
- Channel Distortion, Combated by Channel Inversion by **Tapped Delay Line Filter**
- **GSM** Probe Channel, Learn T-Tap Impulse Response, Fold Impulse Response into MF
- Form List of  $2^L$  Possible Sequences from Channel Impulse Response and MF
- Build Metric Table and Determine Maximum Likelihood Sequence with **Viterbi Decoder**
- **CDMA** Increased Modulation Bandwidth Offers Frequency Diversity
- Wide Bandwidth Signals have Narrow Main Lobe Correlation Width
- Narrow Correlation Width Permits Temporal Resolution of Multipath Components
- Multipath Spreading Combated in **Rake Receiver**:  
Channel Inversion by Time Aligned and Phase Coherent Sum of Multiple Correlator Outputs
- **OFDM** Increased Bandwidth for Higher Data Rate (Without Spreading)
- Wider BW Channels Offer More Channel Distortion
- Rather than Increase Bandwidth, Reduce Bandwidth by Partitioning Available Bandwidth into Multiple Narrowband, Extended Time Duration, Sub-Channels
- Discrete Fourier Transform (DFT) Modulation and Demodulation  
Channel Inversion by **Frequency Domain Equalizer**



# QAM One Wide Band Pipe

## OFDM Many Parallel Narrow Band Pipes



Complements of Charan Langton  
Loral Space Systems,  
[www.complxtoreal.com](http://www.complxtoreal.com)

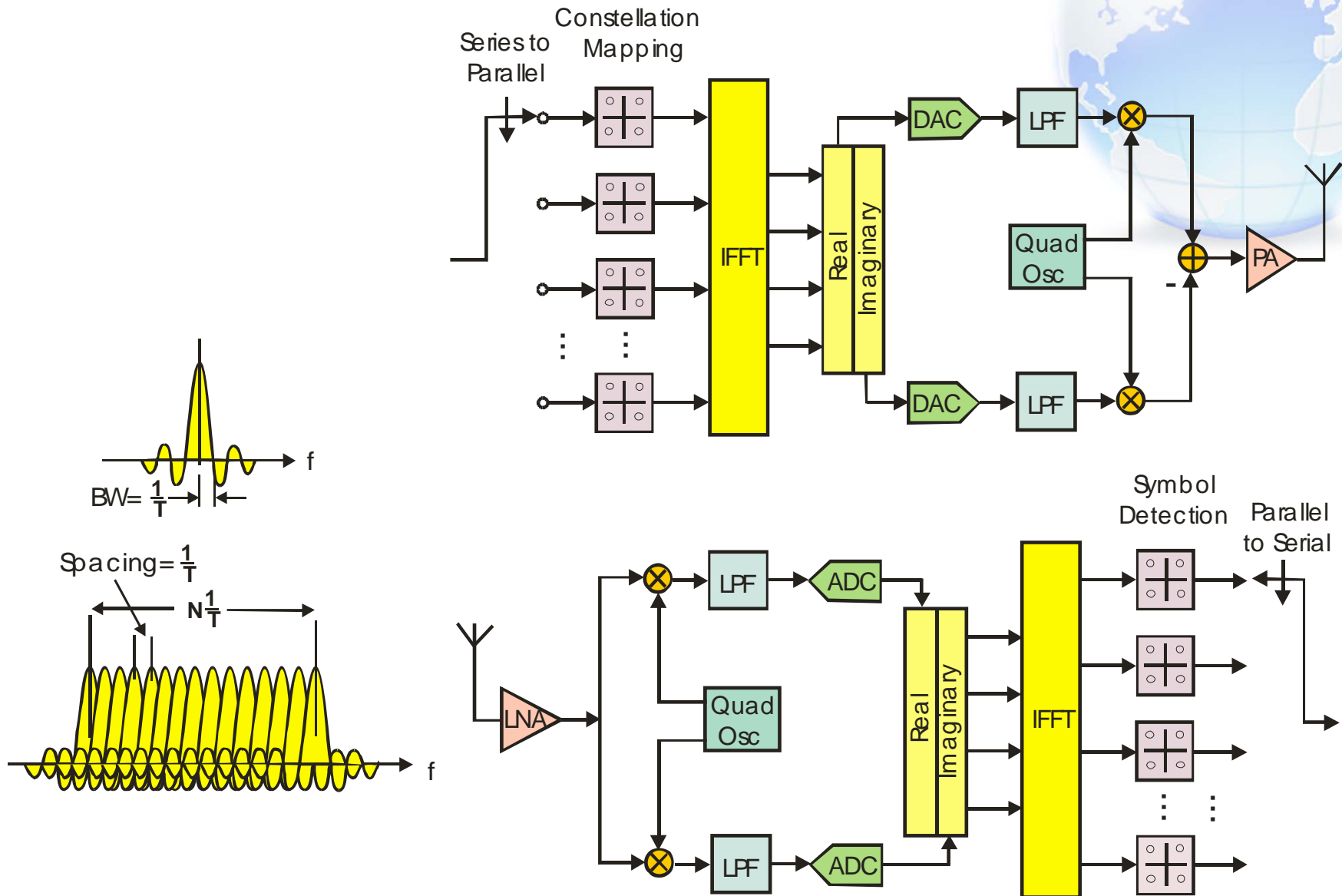


# QAM: One Big Delivery Vehicle

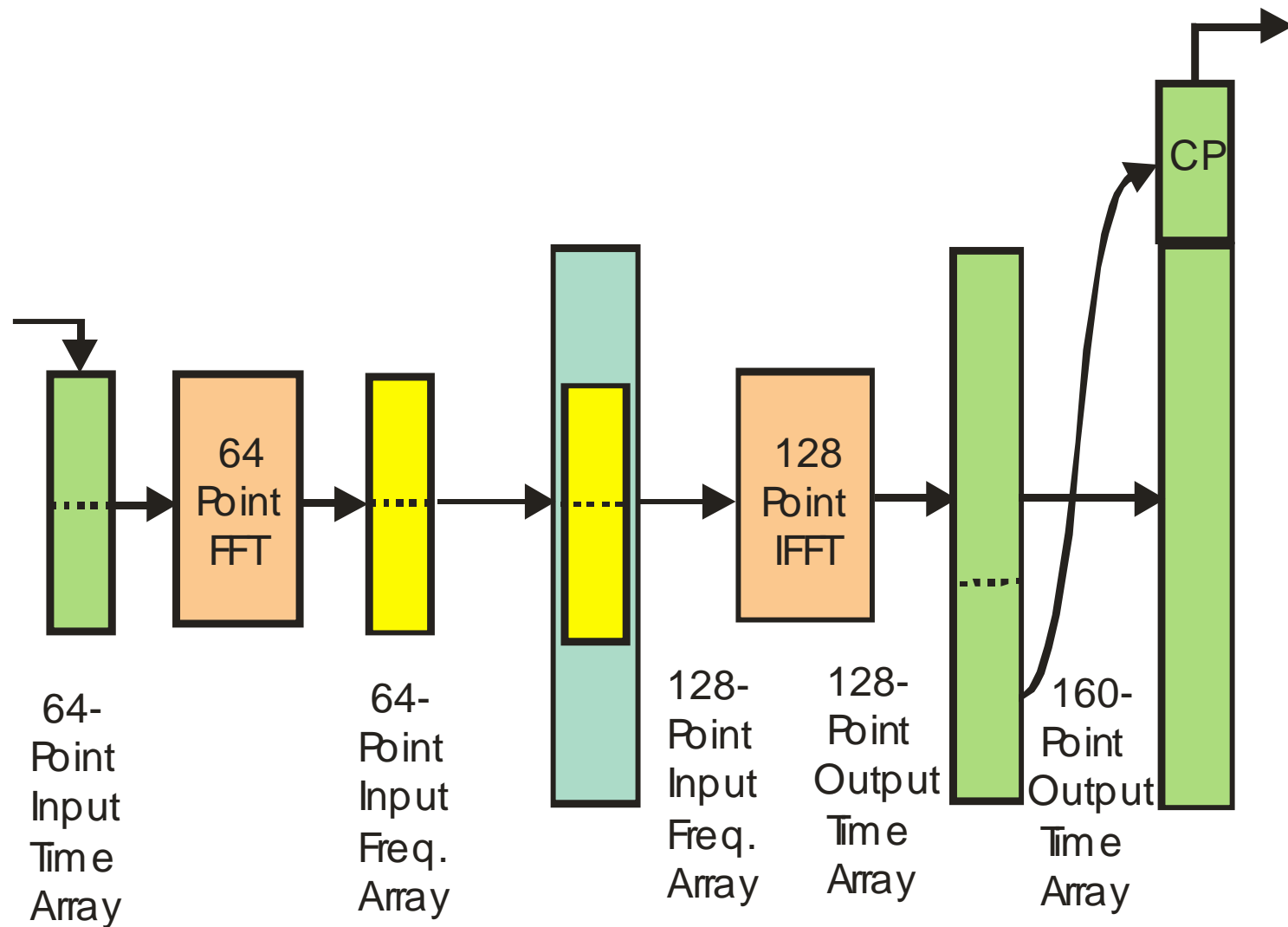
## OFDM: Many Small Delivery Vehicles



# OFDM Modulator and Demodulator

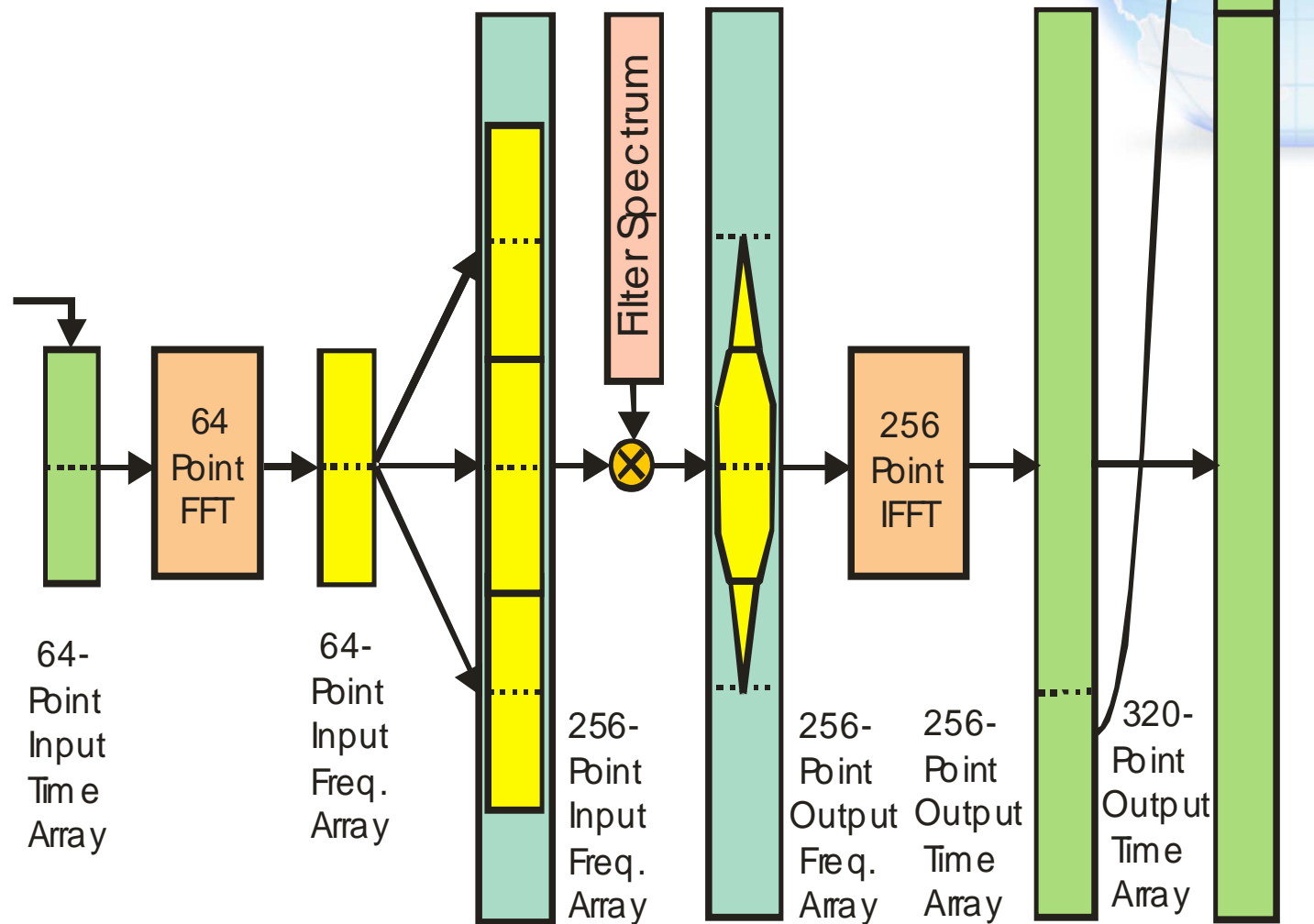


## Unshaped SC-OFDM Dirichlet Kernel Modulator



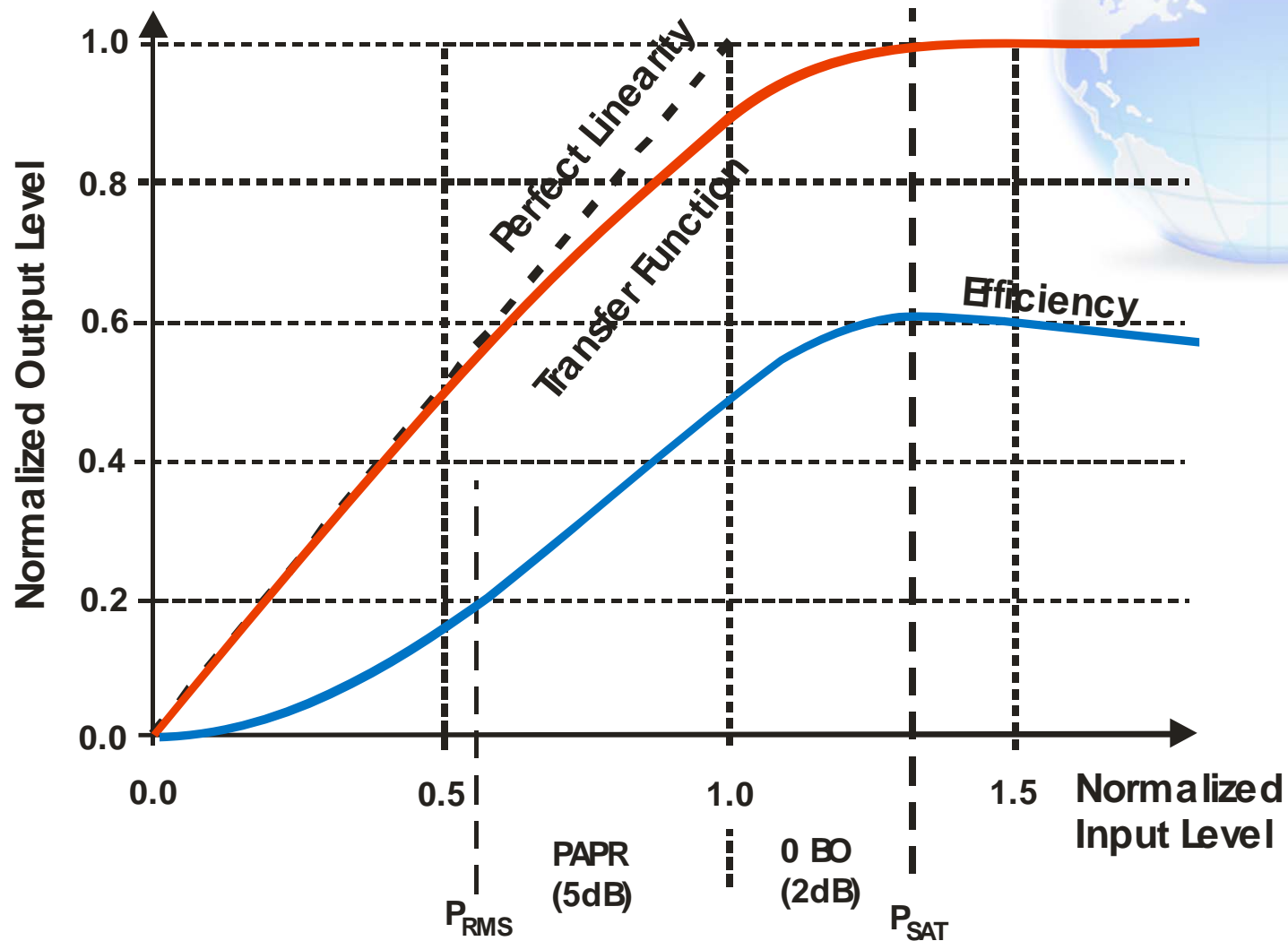
# Shaped SC-OFDM

## Dirichlet Kernel Modulator

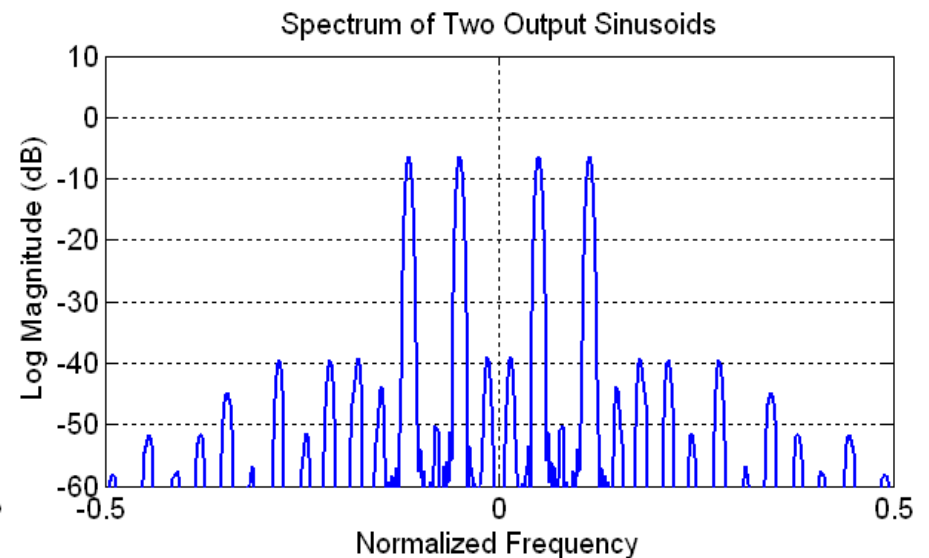
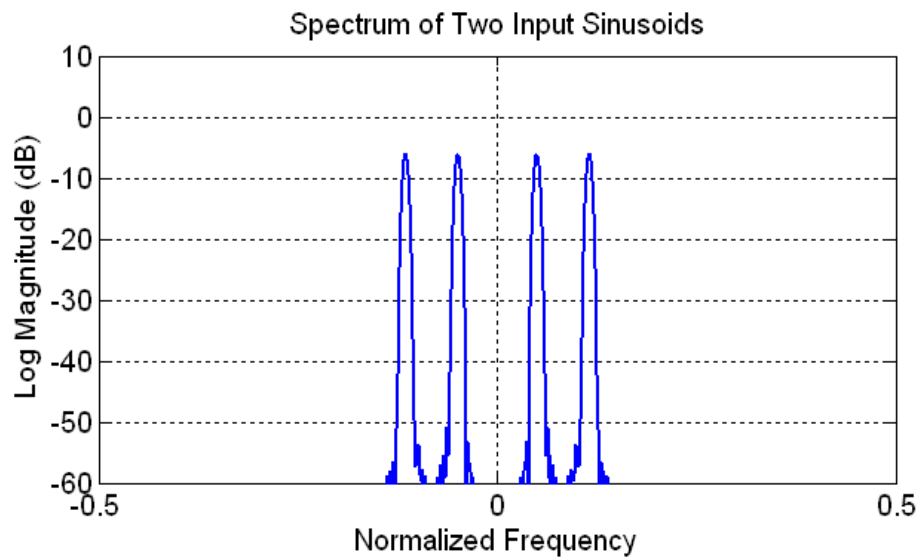
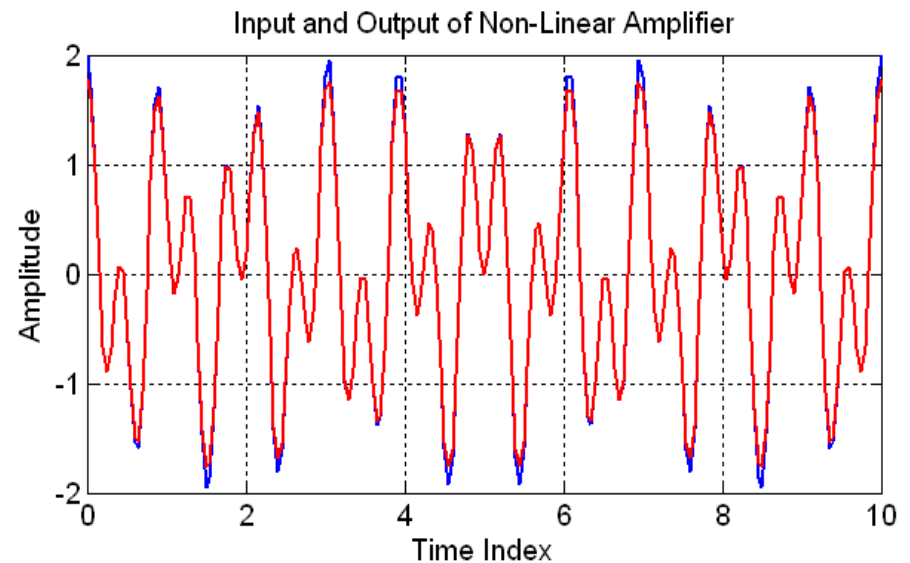
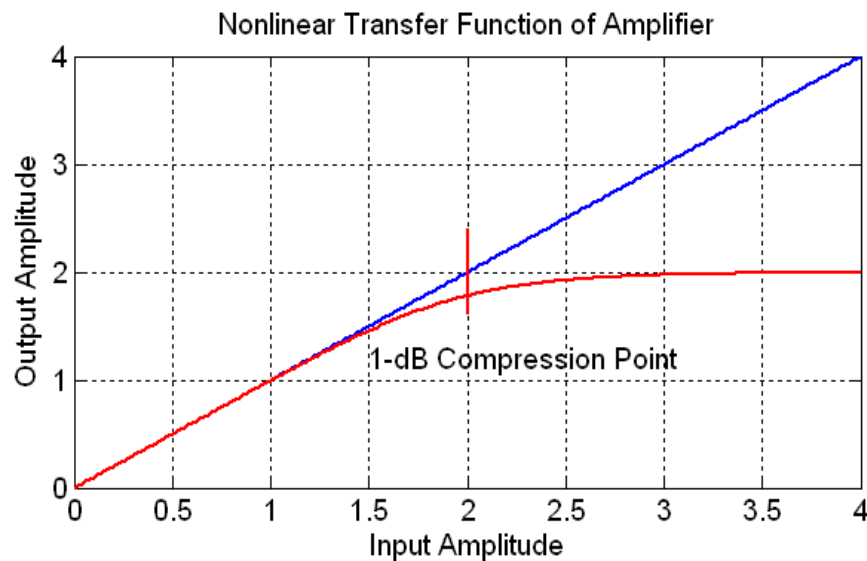




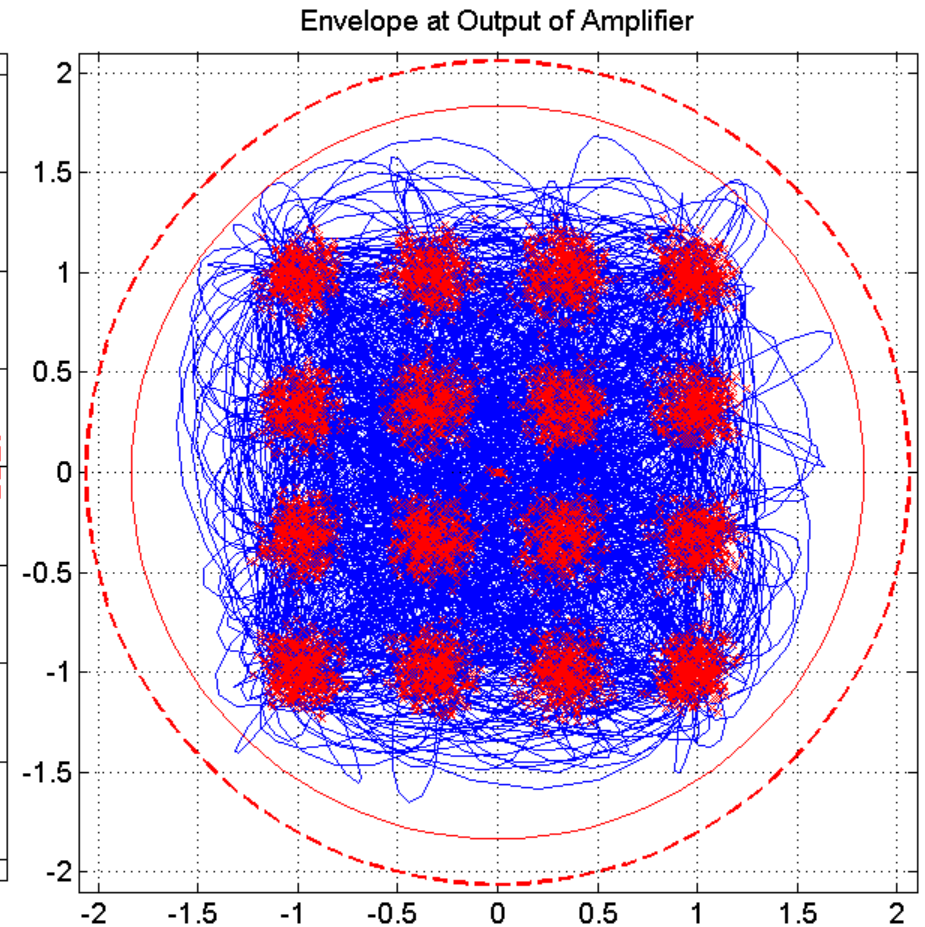
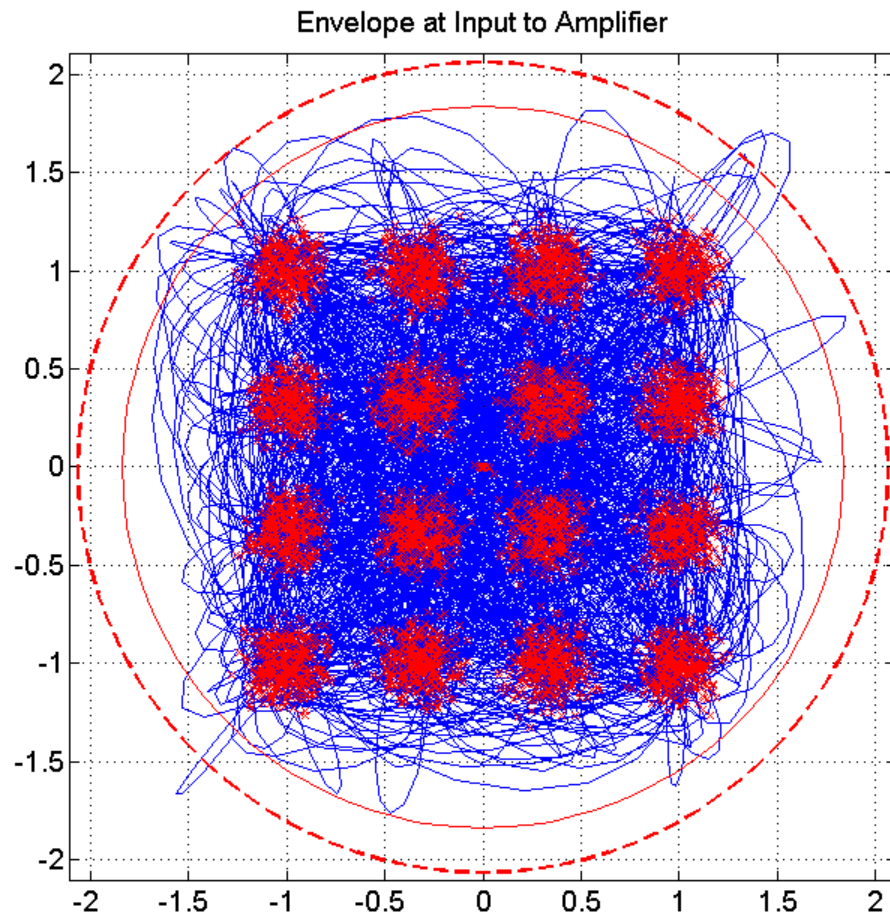
# Power Amplifier Efficiency



# Spectral Re-Growth Due to Power Amplifier Non-Linearity In-band and Out-of-Band Contributions



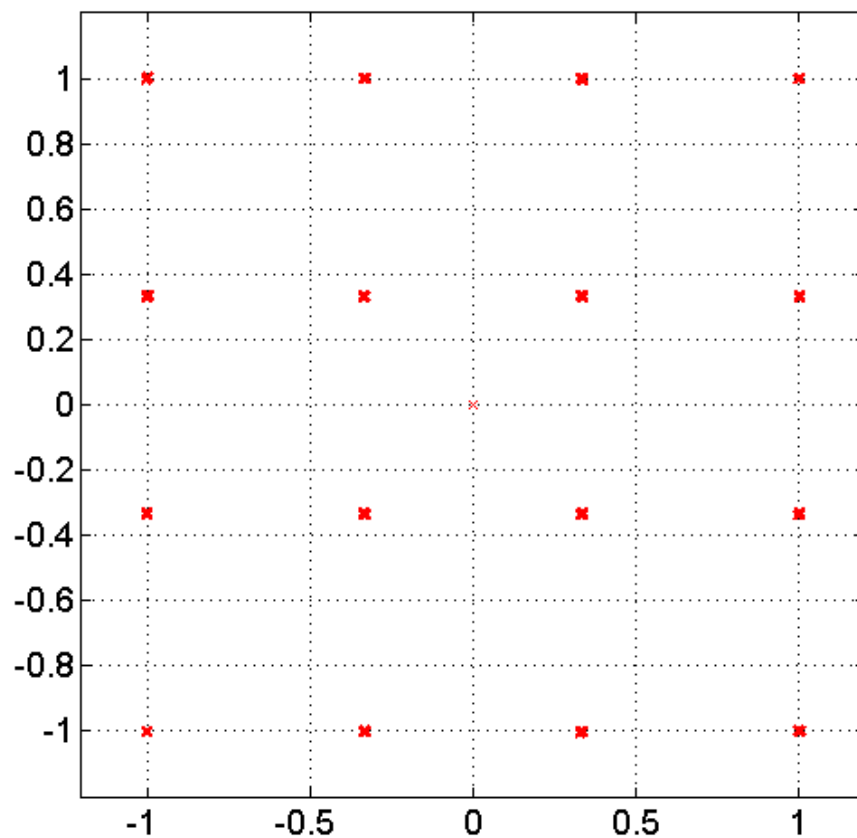
## 16-QAM Input and Output Envelopes. Saturation and 1-dB Compression Circles



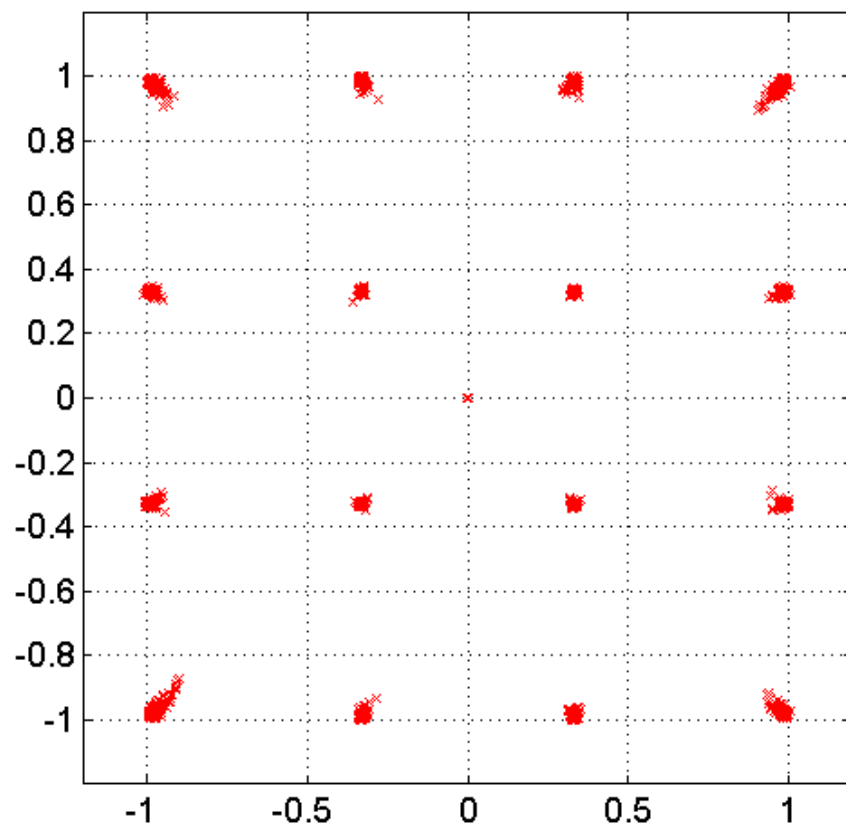
## Limiting Amplifier Effect on Received QAM Constellation



Matched Filter Applied to Input of Amplifier

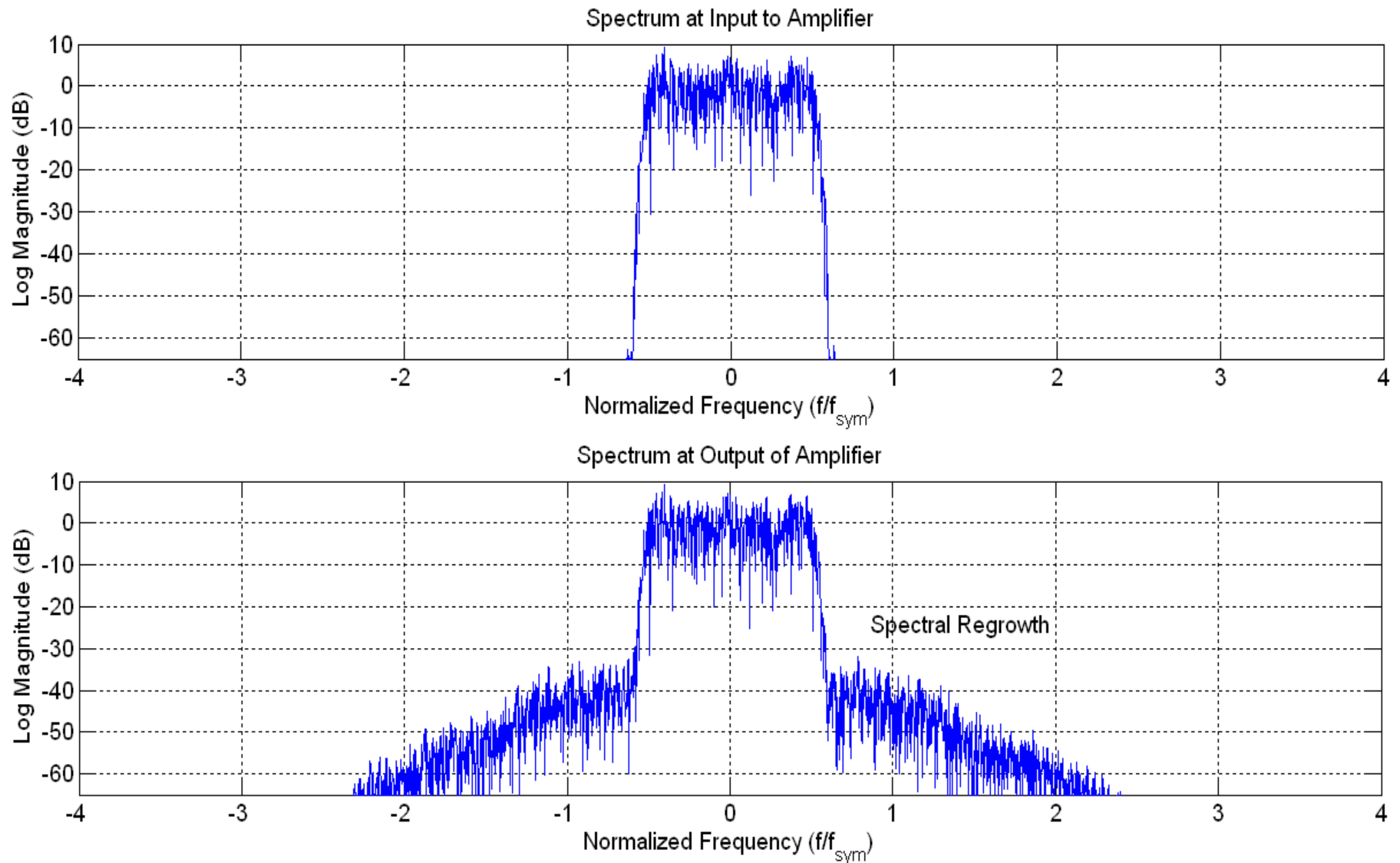


Matched Filter Applied to Output of Amplifier

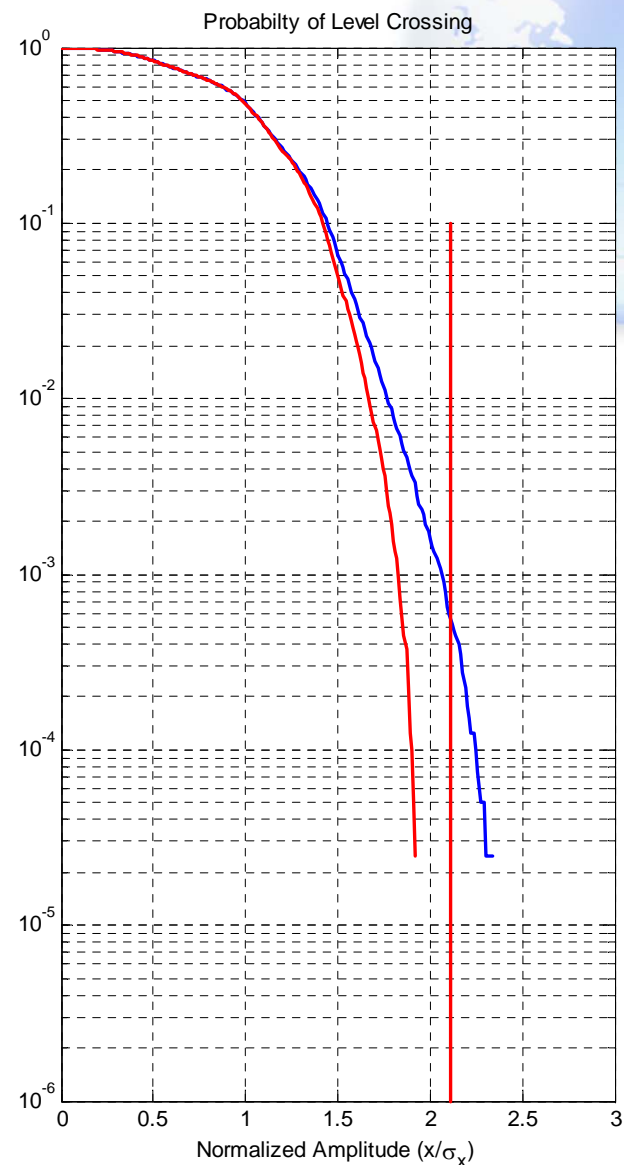
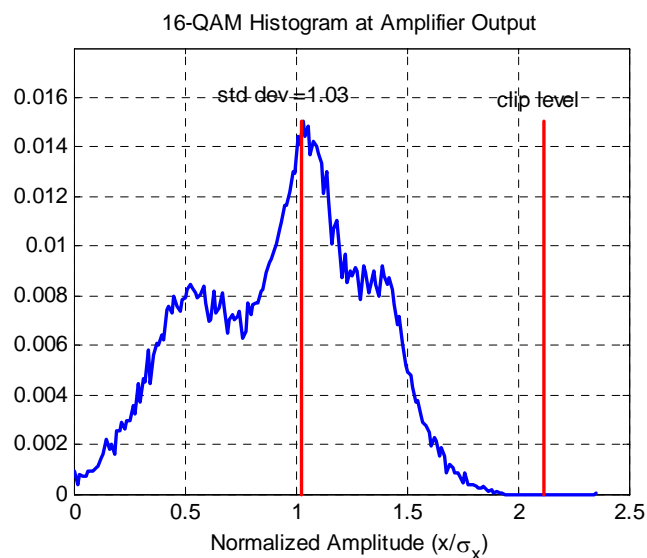
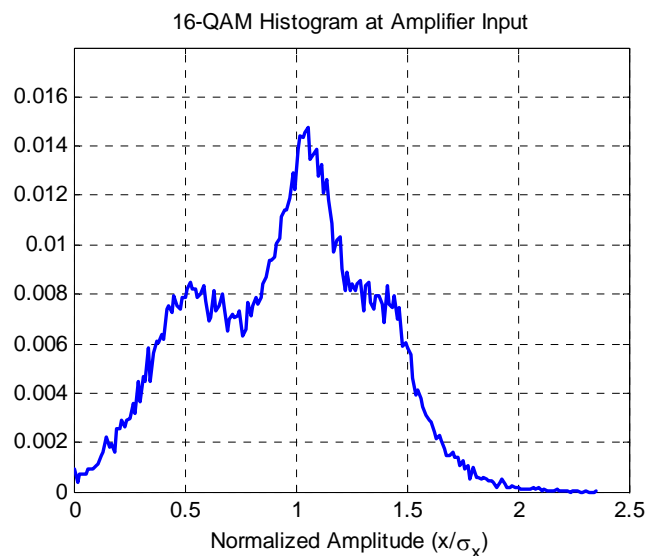




# Limiting Amplifier Effect on Signal Spectra



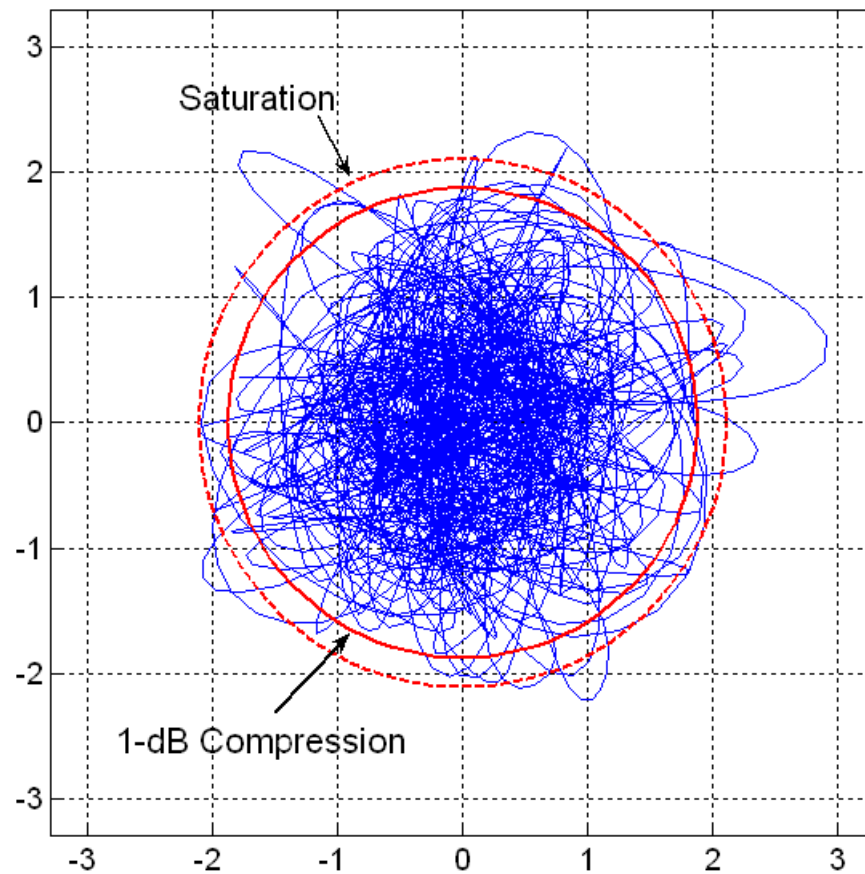
## 16-QAM ( $\alpha=0.2$ ) Envelope Statistics



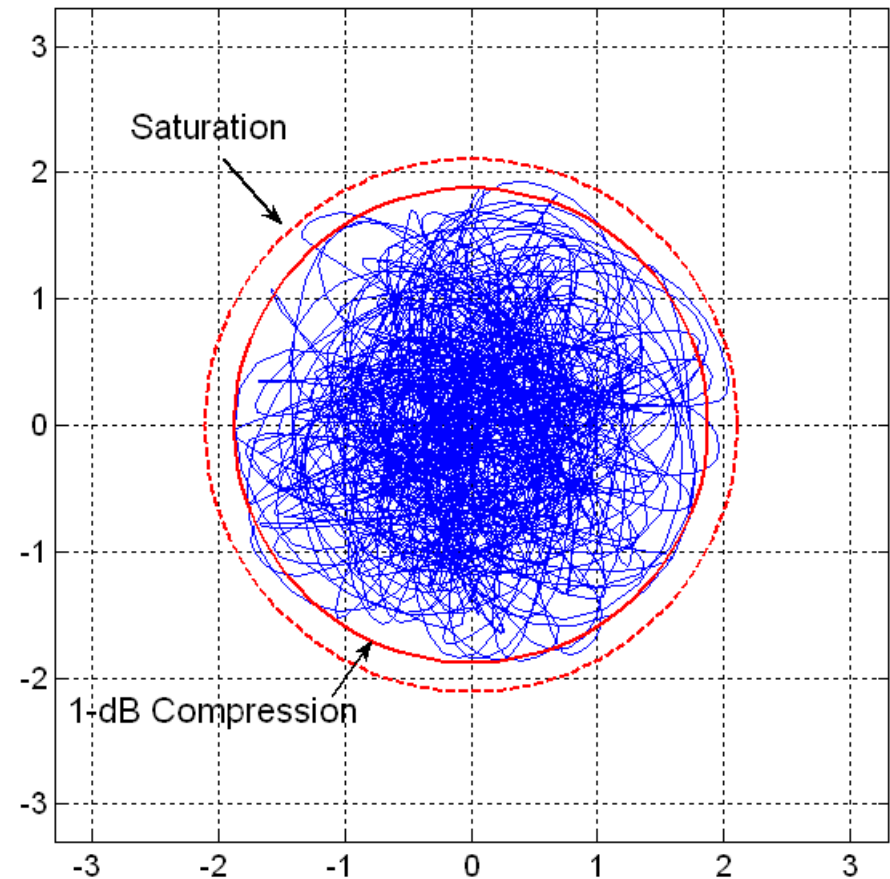
## OFDM Input and Output Envelopes: Saturation and 1-dB Compression Circles



Envelope at Input to Amplifier



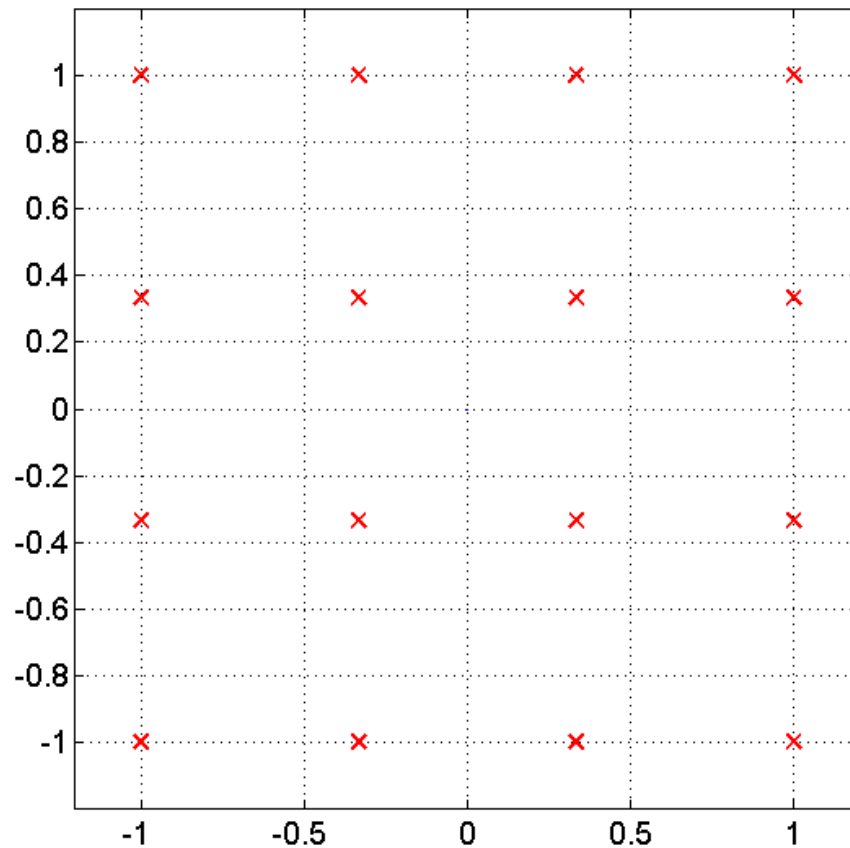
Envelope at Output of Amplifier



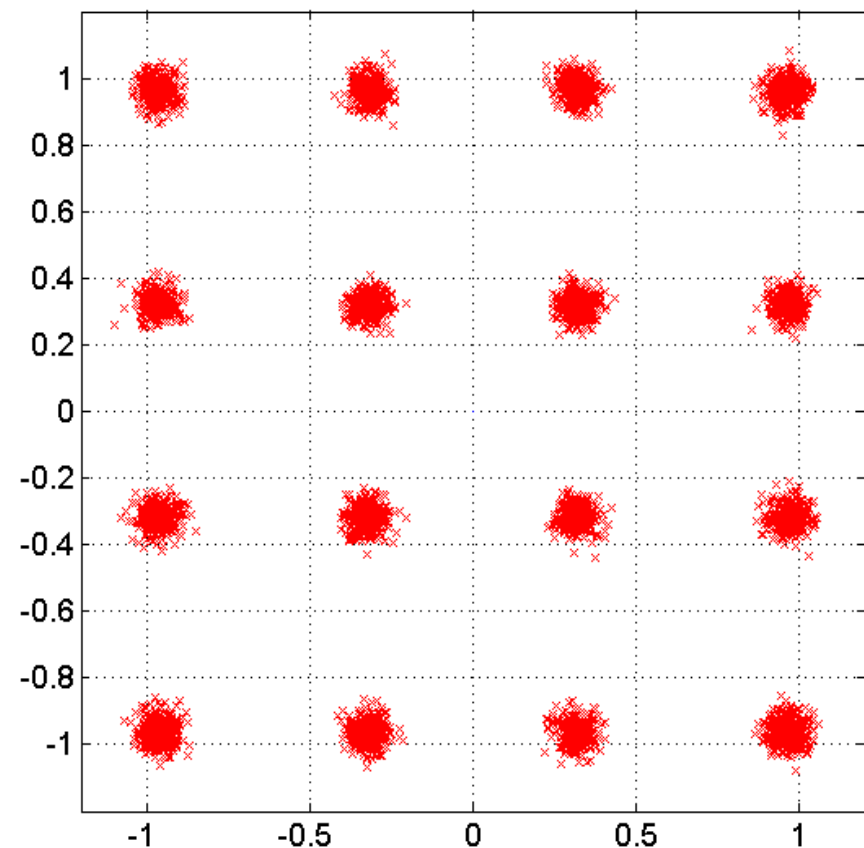
# Limiting Amplifier Effect on OFDM Constellation



OFDM Constellation at Input to Amplifier



OFDM Constellation at Output of Amplifier

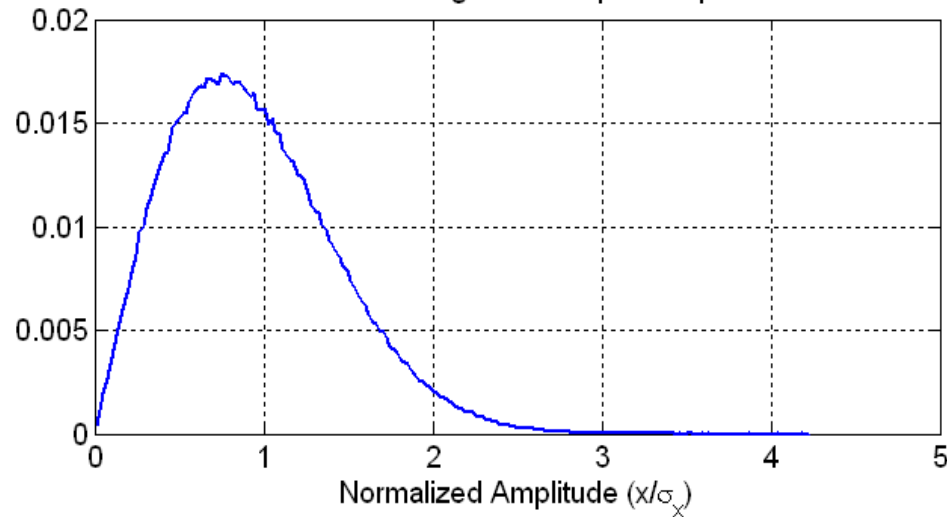




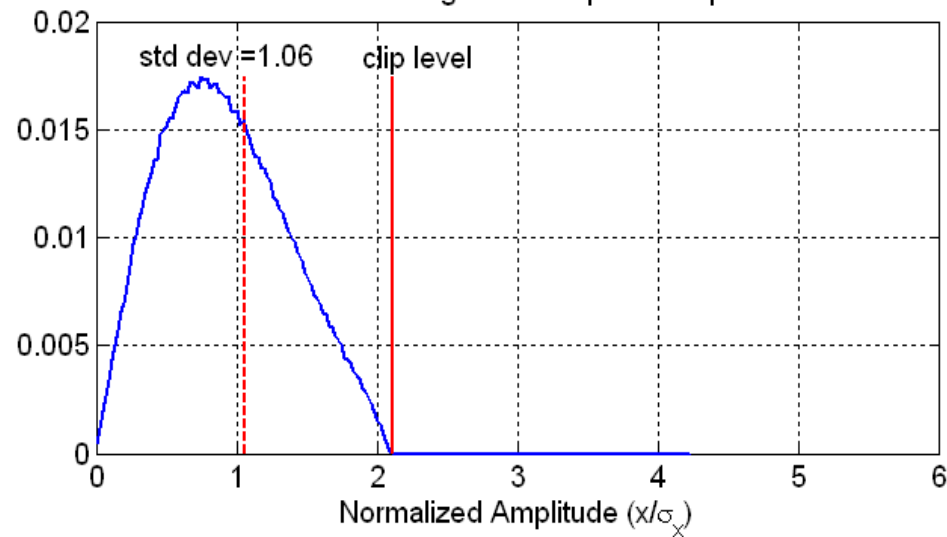
# OFDM Envelope Statistics



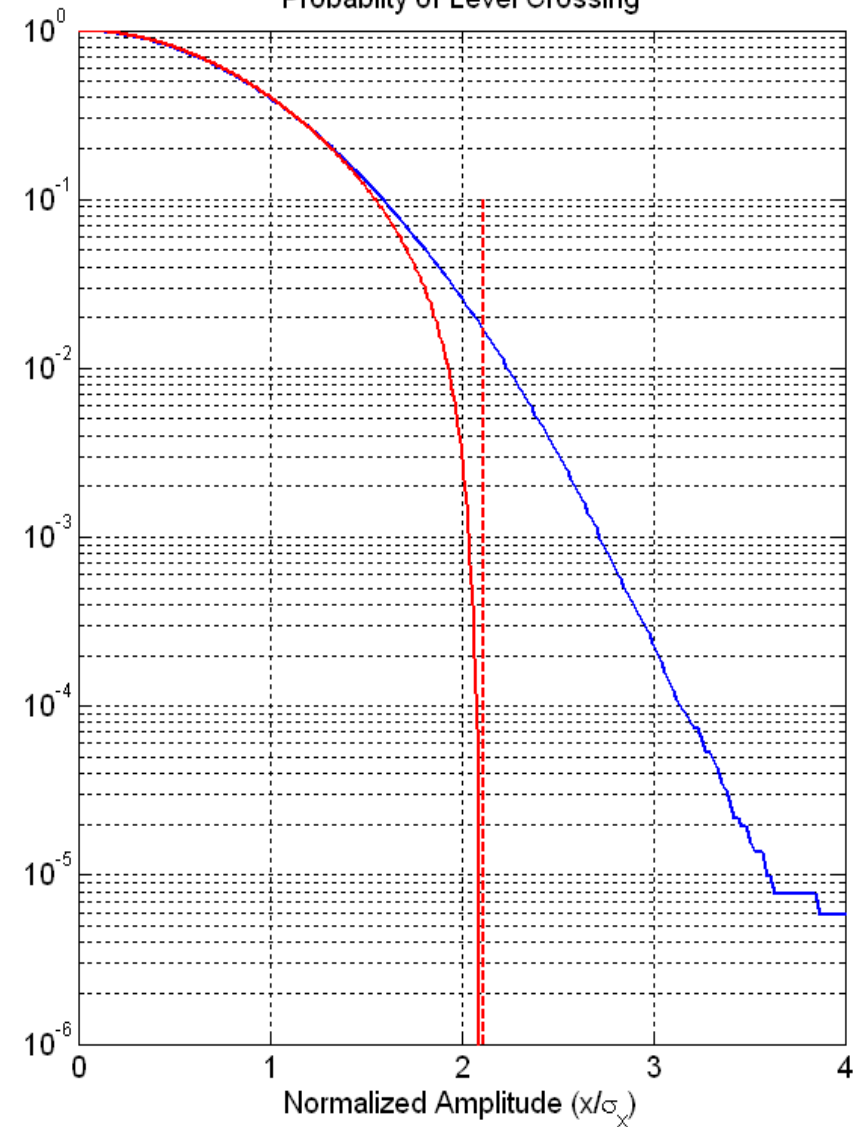
OFDM Histogram at Amplifier Input



OFDM Histogram at Amplifier Output

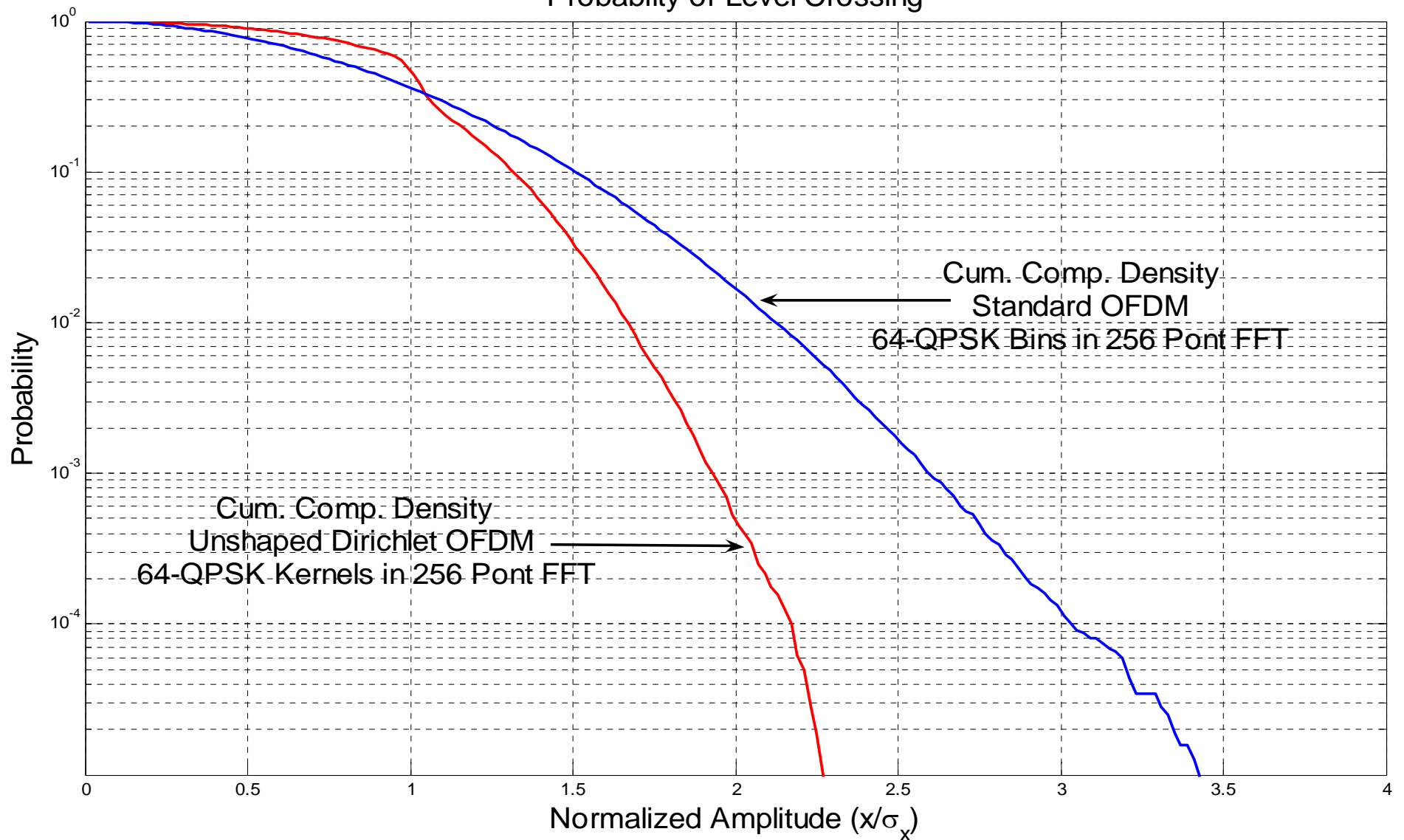


Probability of Level Crossing



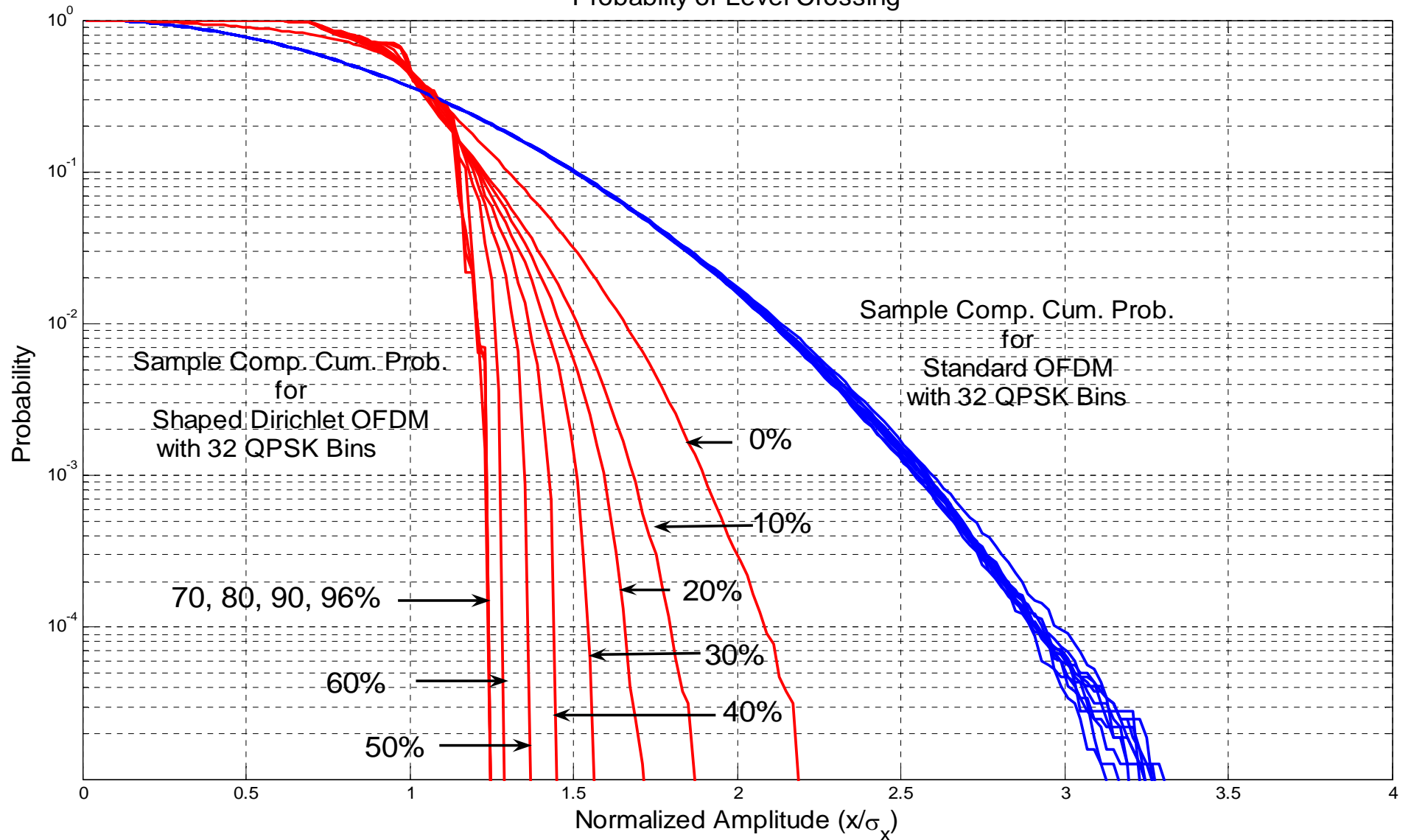
# Complementary Cumulative Density Functions for Standard OFDM and SC-OFDM

Probability of Level Crossing

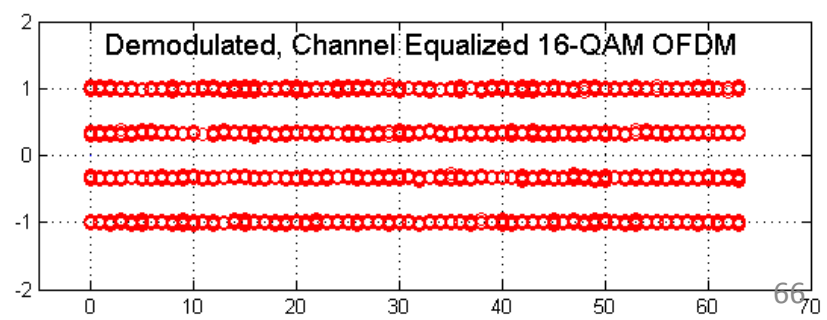
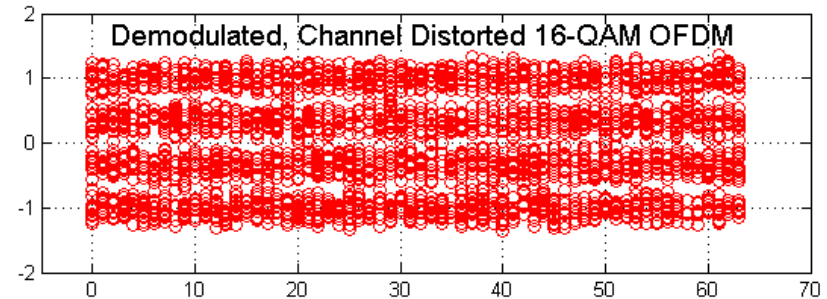
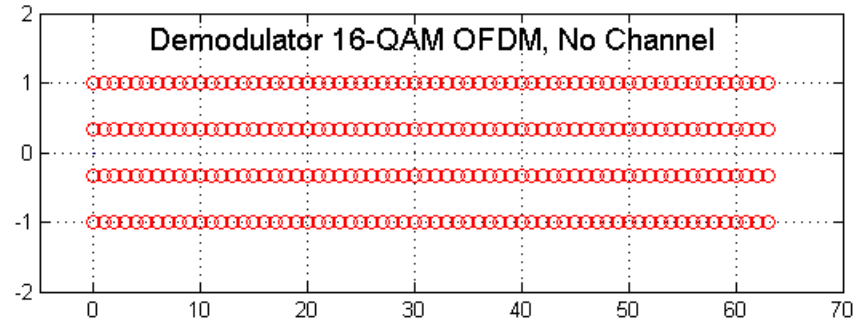
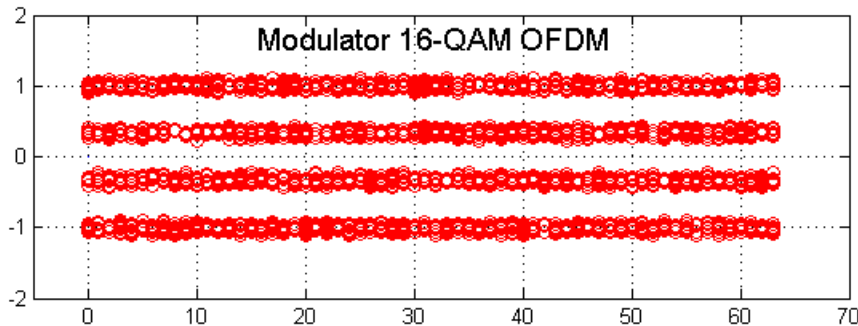
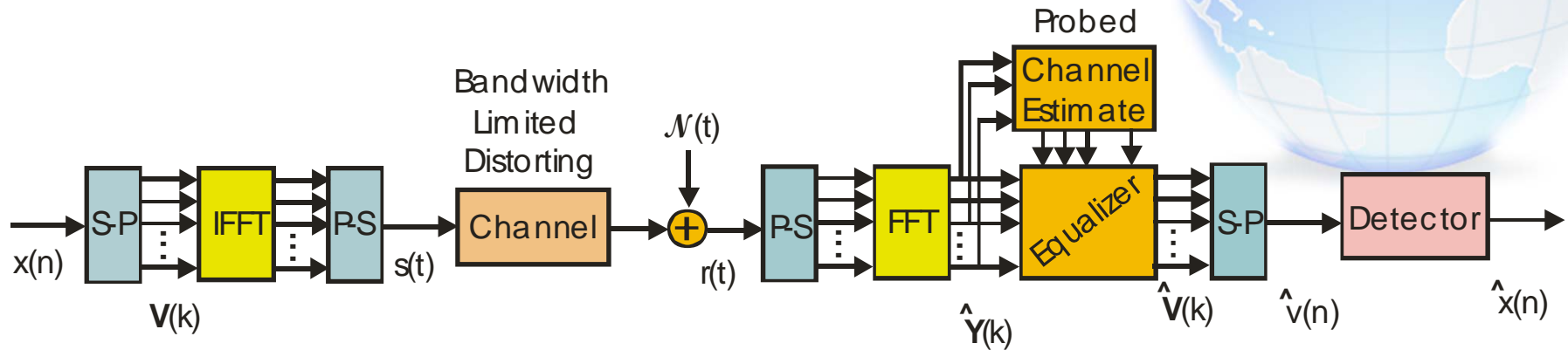


# PAPR: OFDM, SC-OFDM, Shaped SC-OFDM

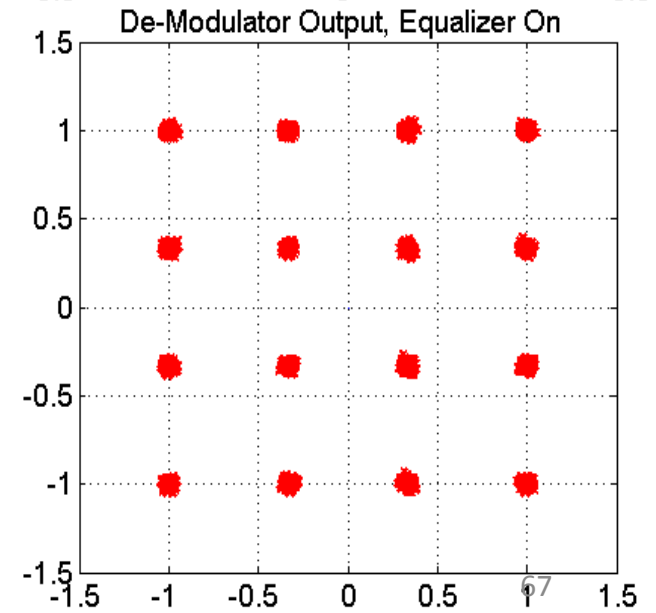
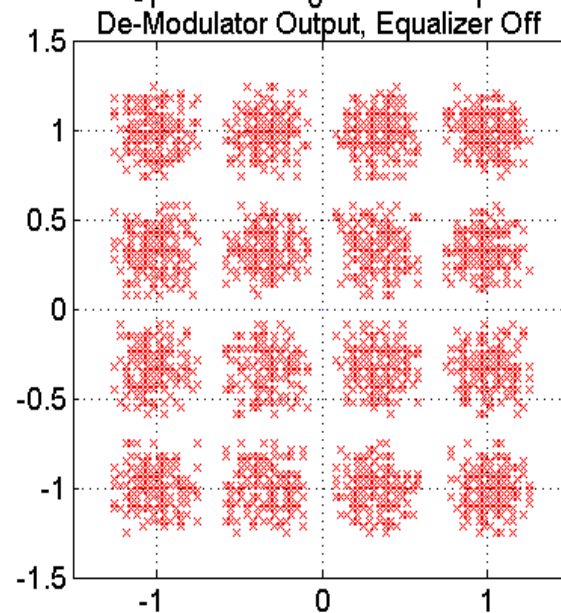
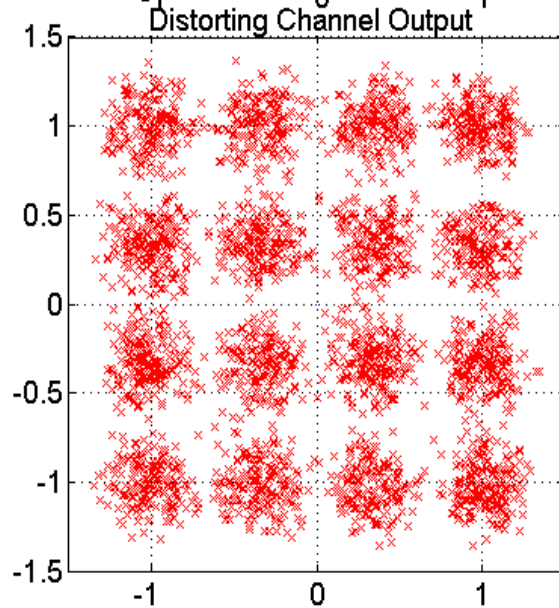
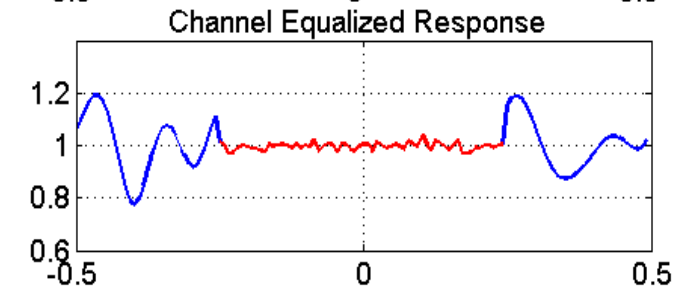
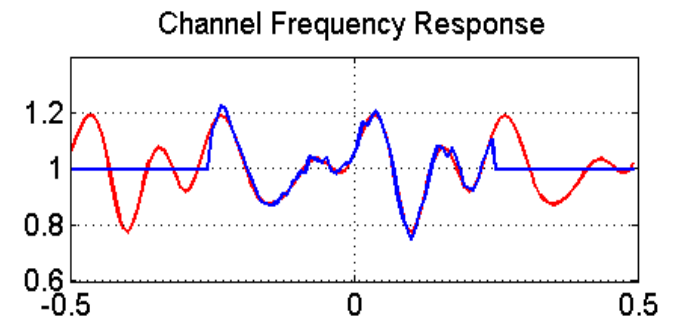
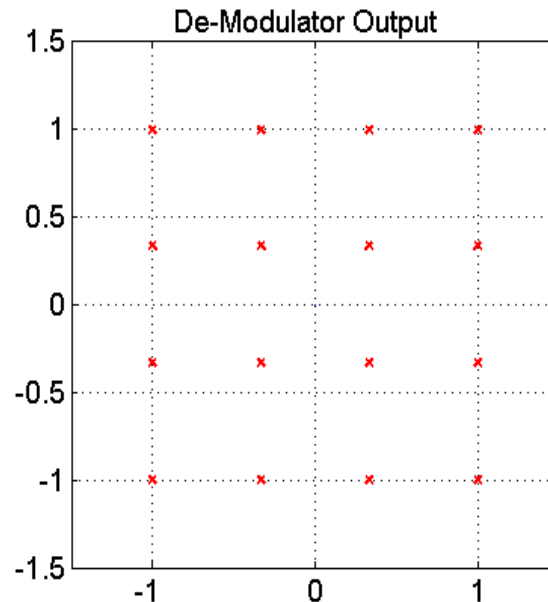
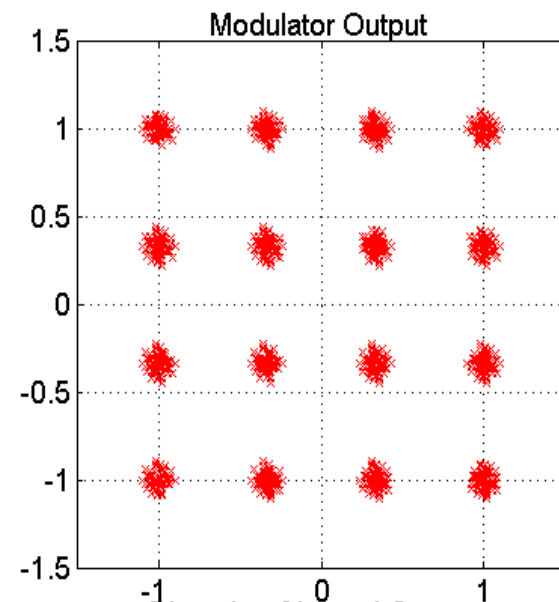
Probability of Level Crossing



# Orthogonal Frequency Division Multiplexing Frequency Domain Equalization



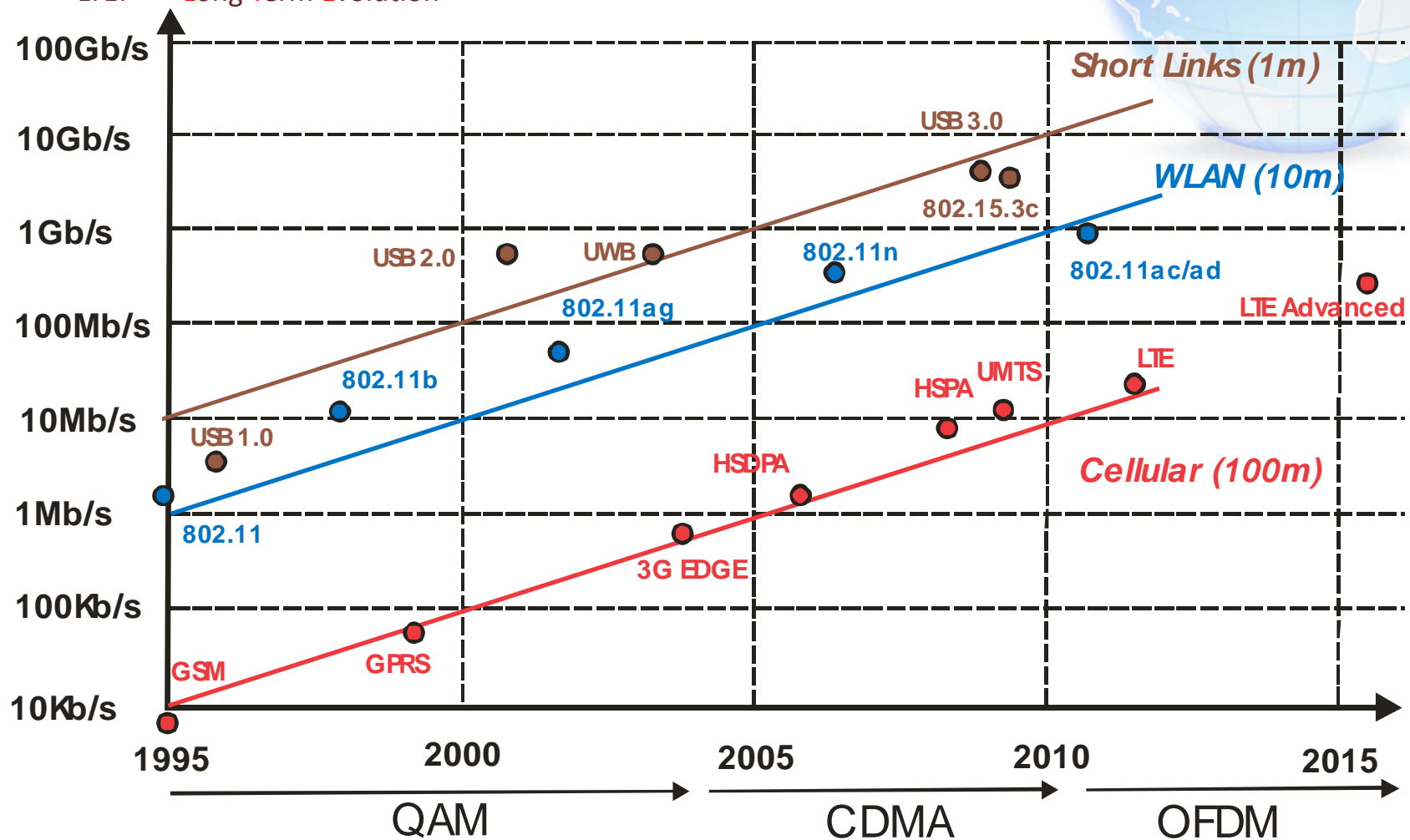
# OFDM Frequency Domain Equalization



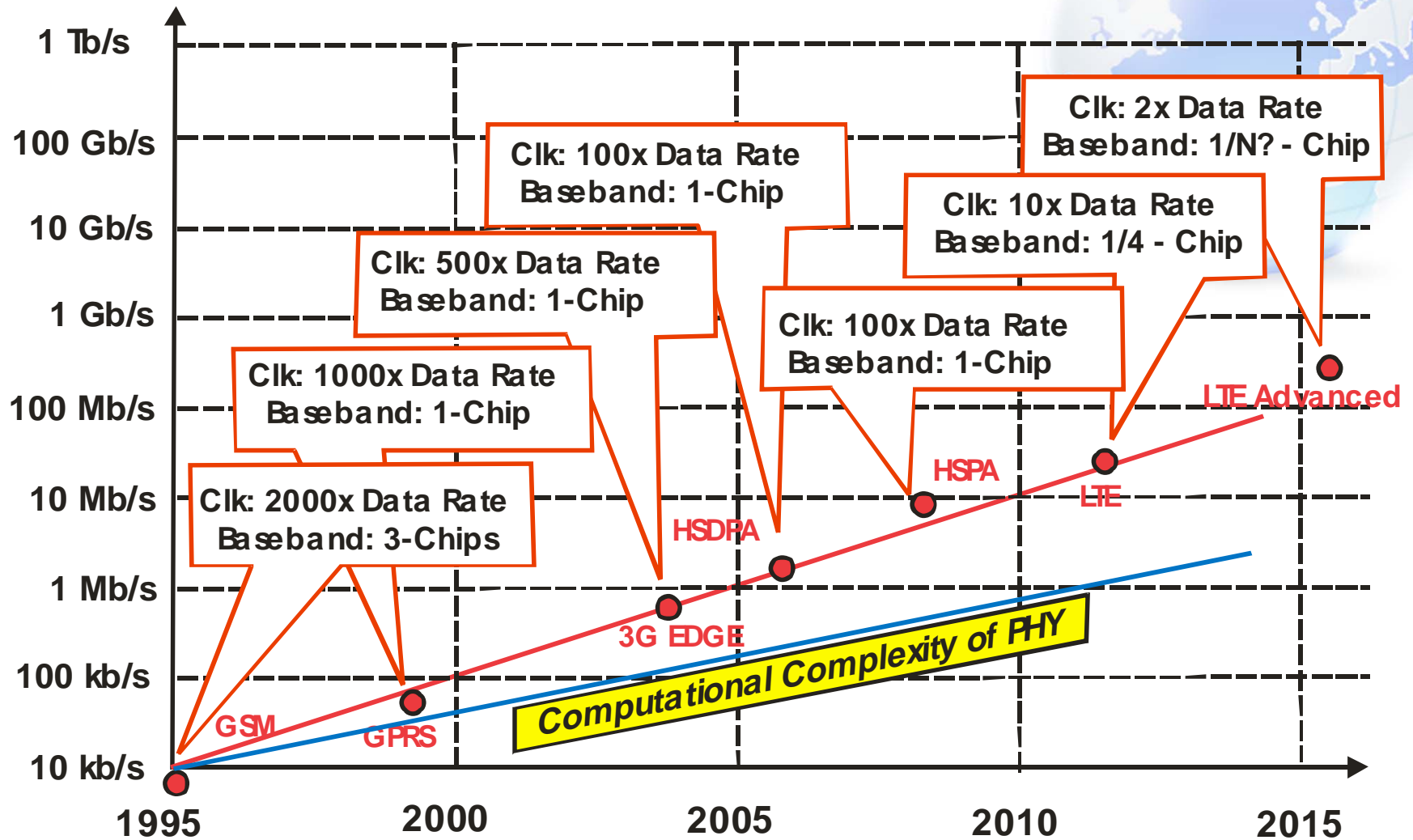


GSM: **G**roupe **S**écial **M**obile  
 GPRS: **G**eneral **P**acket **R**adio **S**ervice  
 EDGE: **E**nhanced **D**ata **R**ates for **G**SM **E**volution  
 HSDPA: **H**igh **S**peed **D**ownlink **P**acket **A**ccess  
 HSPA: **H**igh **S**peed **P**acket **A**ccess  
 UMTS: **U**niversal **M**obile **T**elecommunications **S**ystem  
 LTE: **L**ong **T**erm **E**volution

## Evolving Data Rates



# Physical Layer Complexity



# Receiver Complexity Reduction



## **2G: MLSE**

Equalizer Complexity  
Grows Exponentially  
With Length of Echoes!!



## **3G: RAKE**

Receiver Complexity  
Grows Linearly  
With Number of Echoes!!

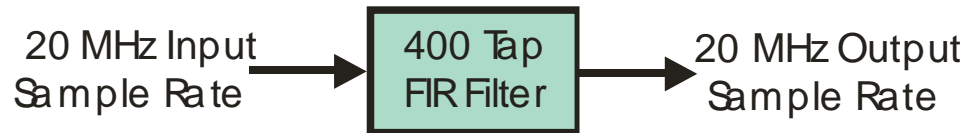
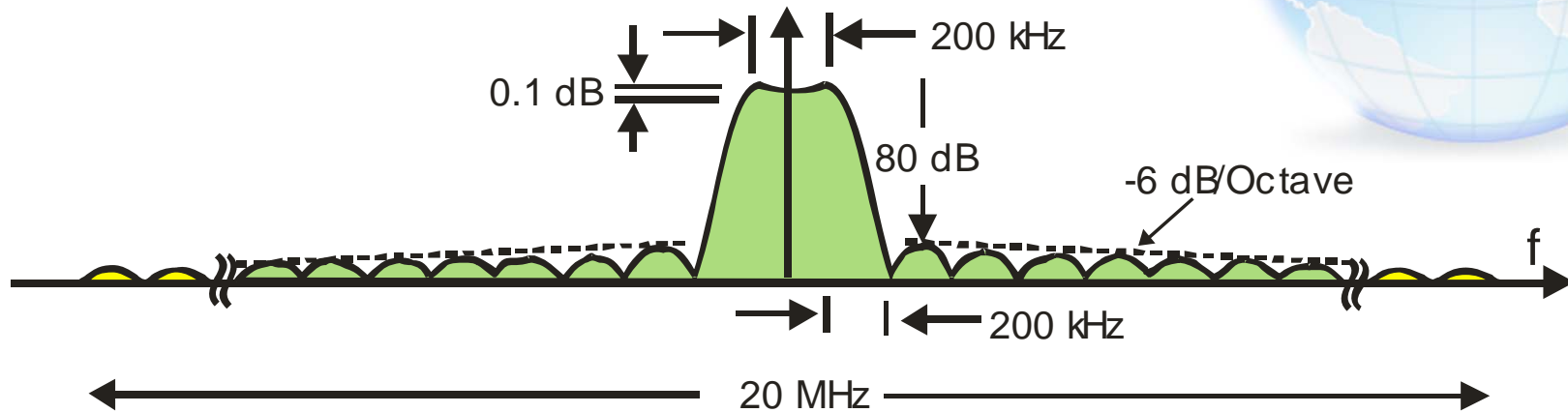


## **4G/LTE: OFDM**

Receiver Complexity  
Grows Logarithmically  
With Length of Echoes!!



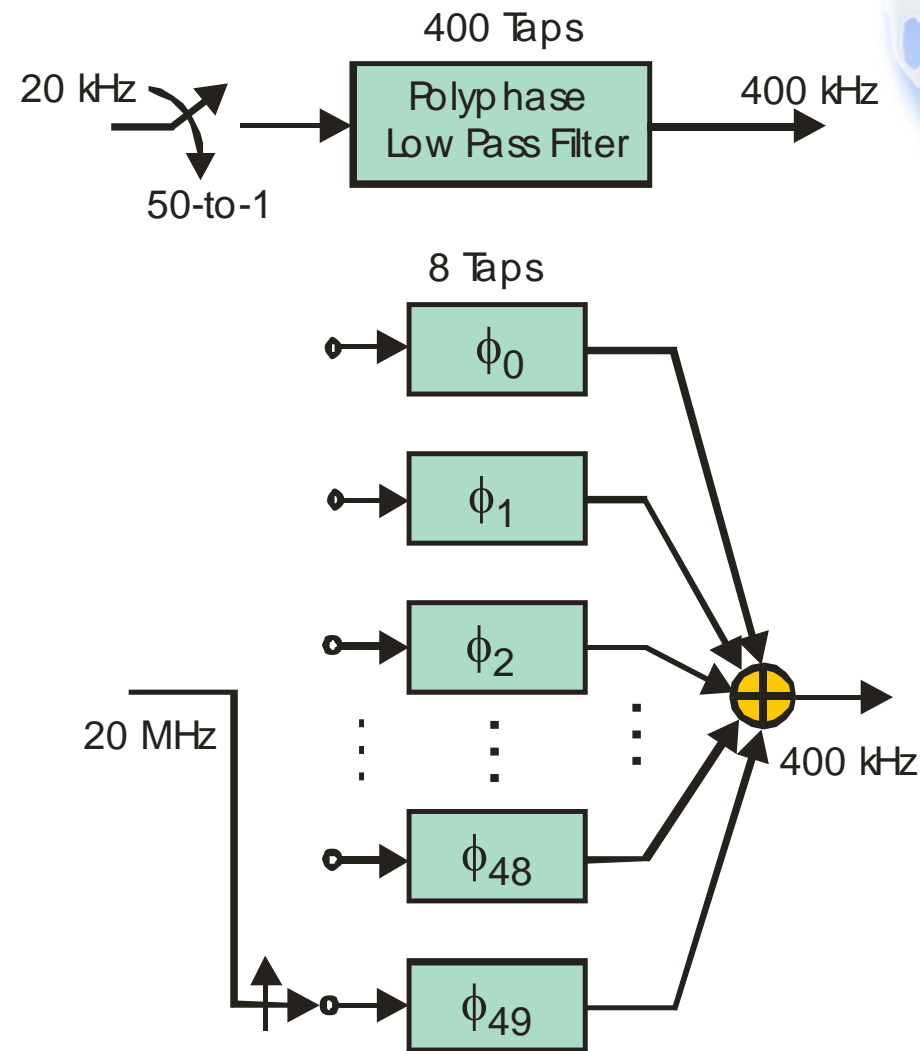
## Bad Mismatch: Sample Rate Large Compared to Transition Bandwidth



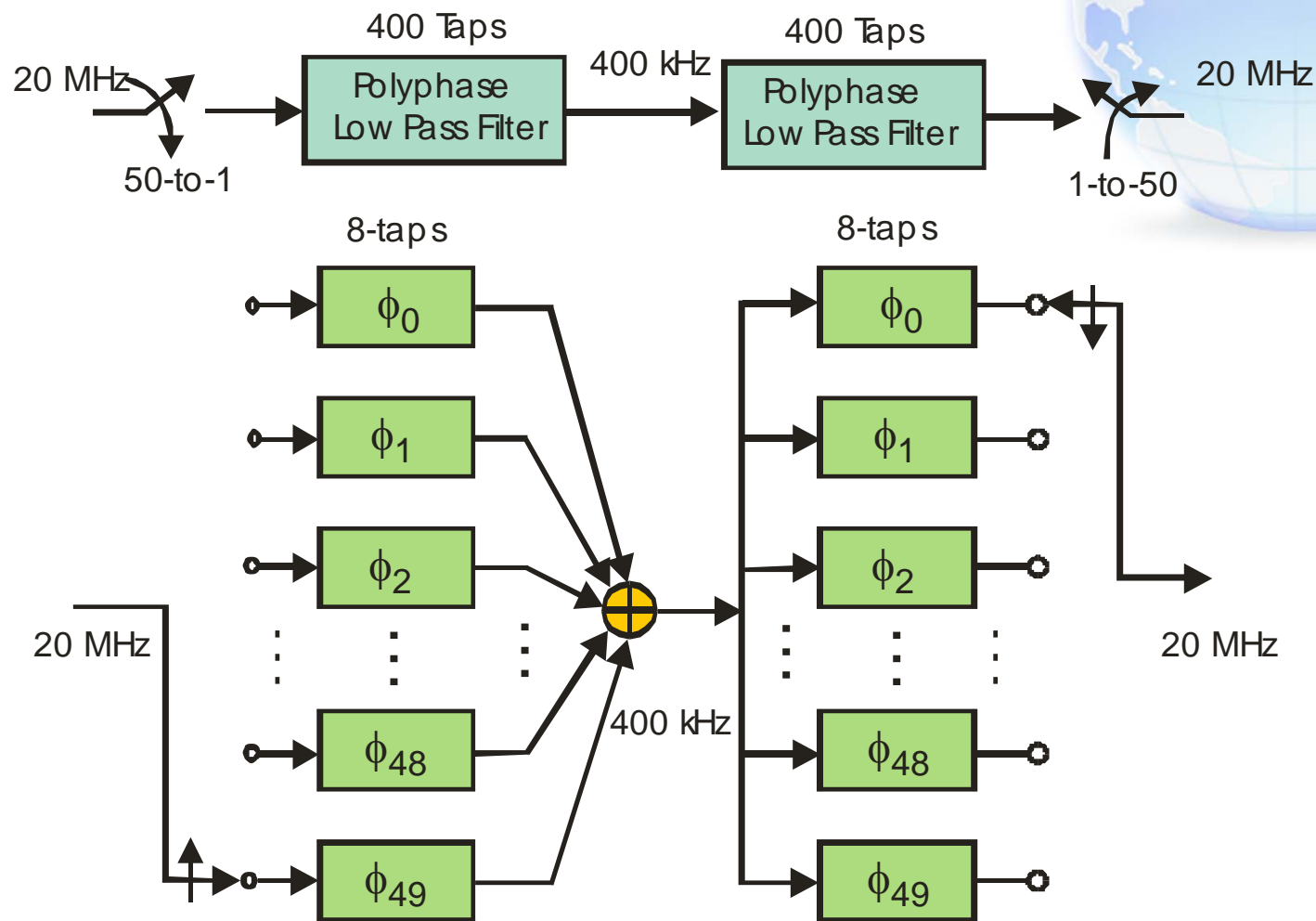
**Nyquist Rate for Filter is  
 $200 \text{ kHz} + 200 \text{ kHz} = 400 \text{ kHz}$  or  $f_s/50$**



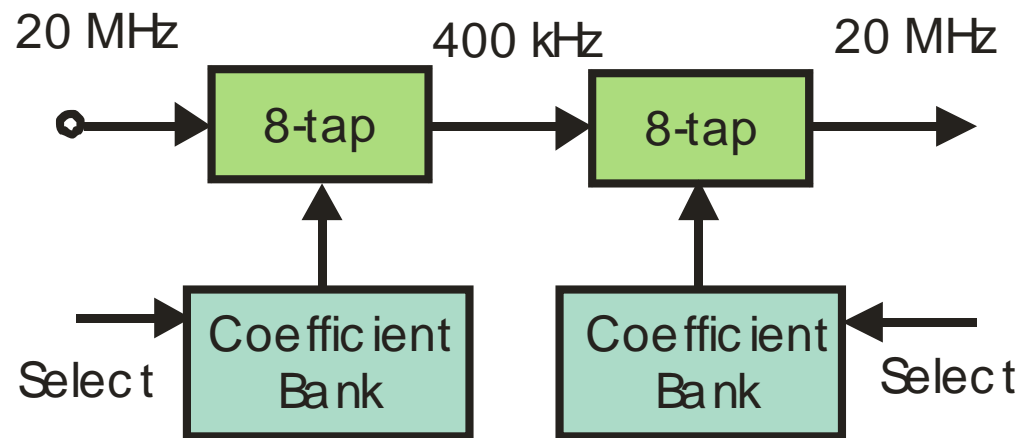
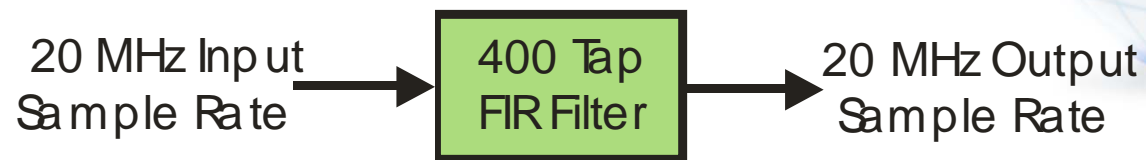
## Polyphase Partition of Low-Pass Filter



# Cascade Polyphase Filter Down-Sampling and Up-Sampling

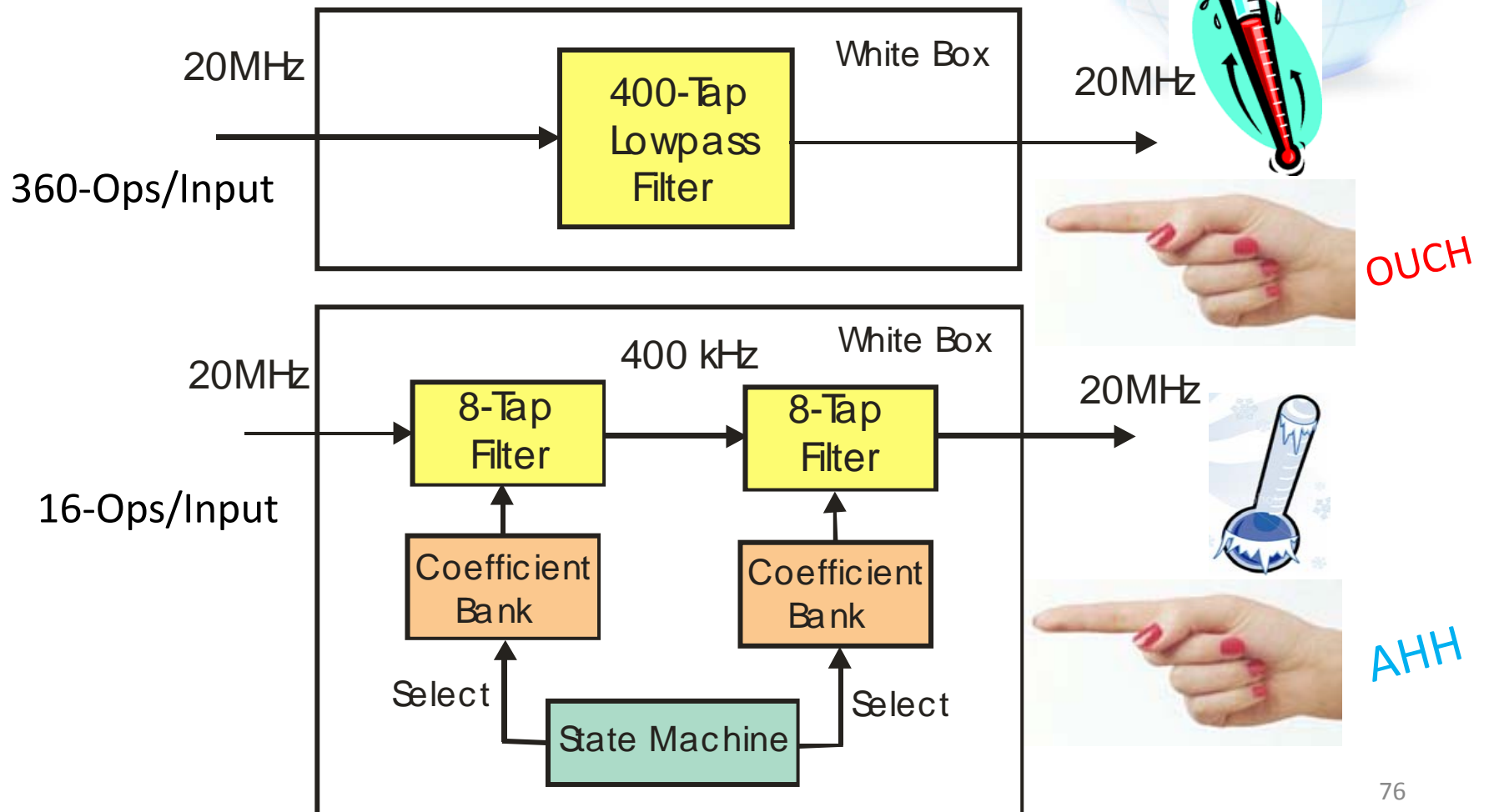


# Efficient Polyphase Filter Implementation

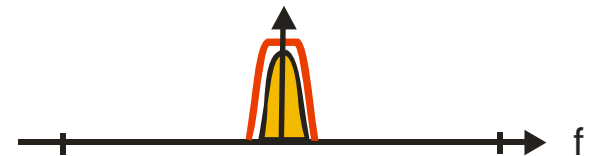
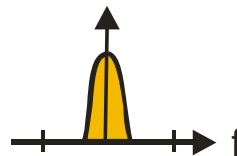
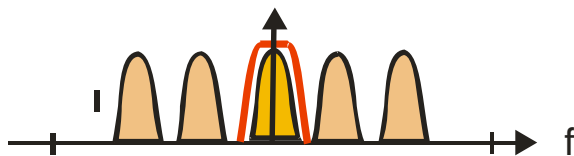
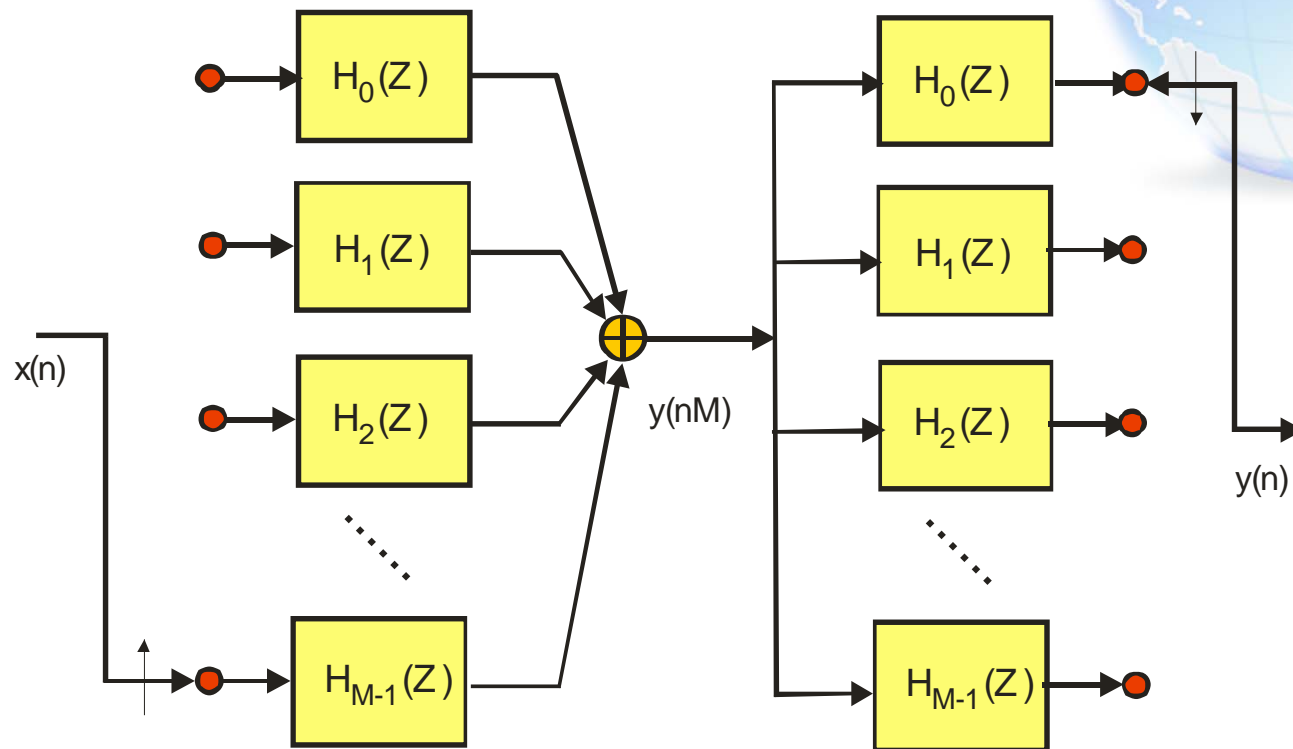


# Two Processing in Boxes: How can you tell which is which from outside box?

(The Wet Finger Test)

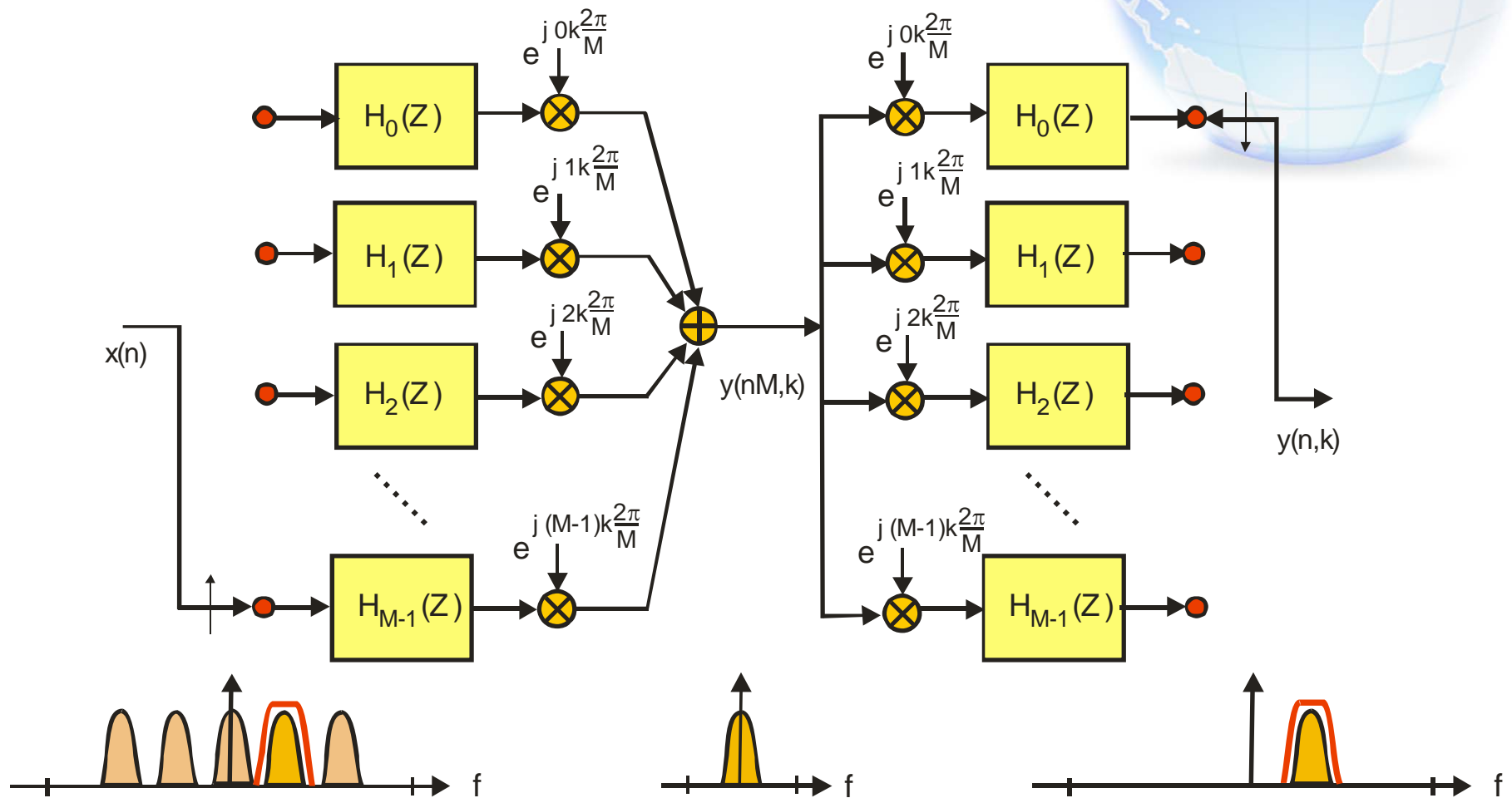


# Polyphase Partition of Low-Pass Filter

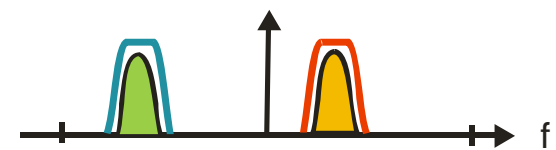
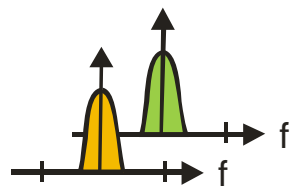
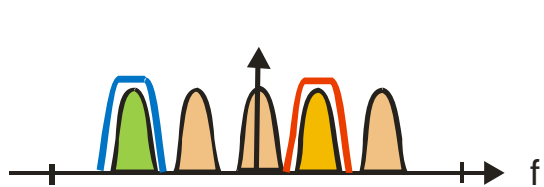
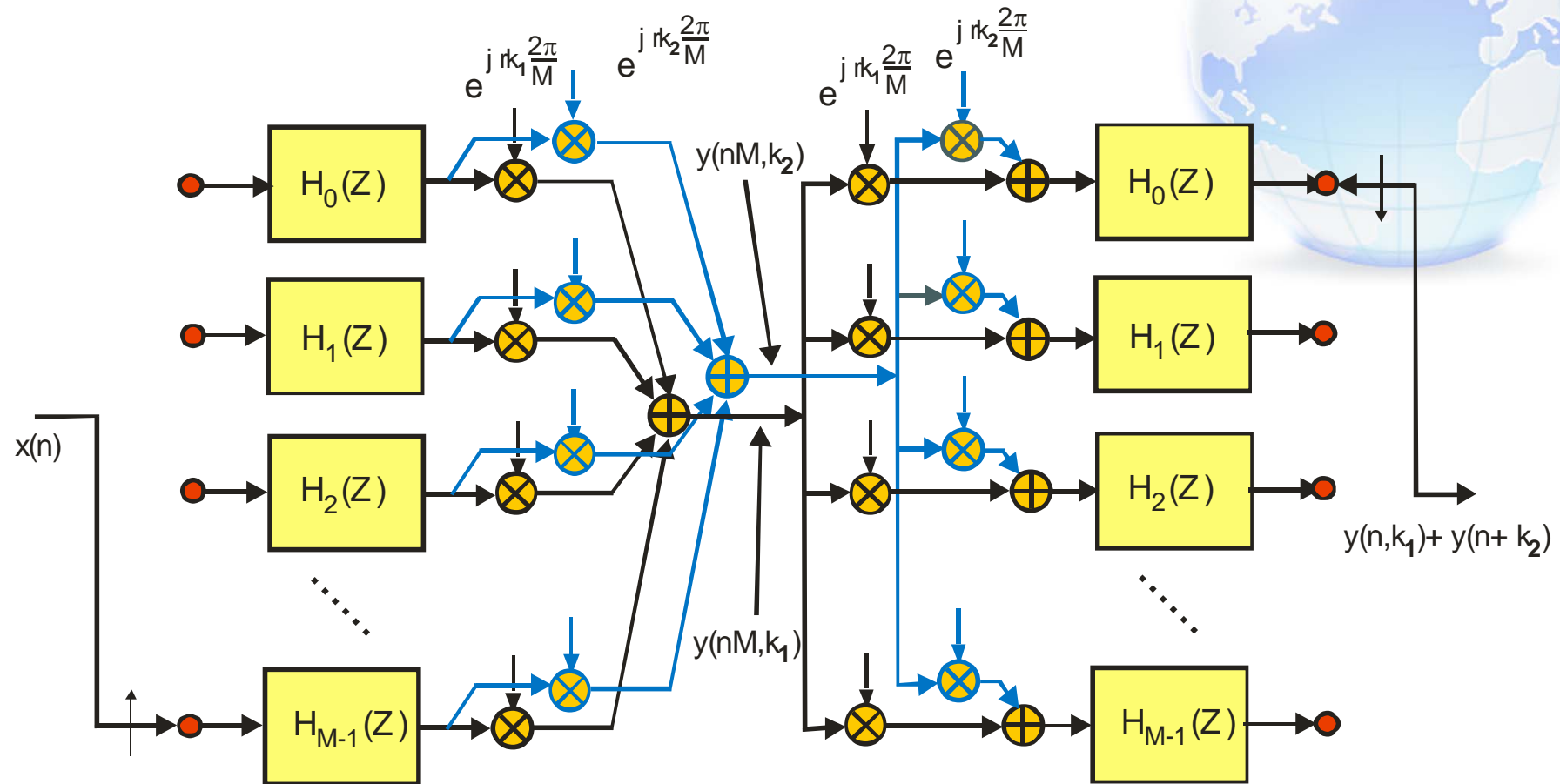




# Polyphase Partition of Band Pass Filter



# Polyphase Partition of Two Band Pass Filters



## Workload for Multiple M-Path Filters



- **1-Channel M-to-1 Down Sample**
  - **1-Filter and M Complex Phase Rotators**
- **2-Channels M-to-1 Down Sample**
  - **1-Filter and 2M Complex Phase Rotators**
- **K-Channels M-to-1 Down Sample**
  - **1-Filter and kM Complex Phase Rotators**
- **M-channels M-to-1 Down Sample (use FFT)**
  - **1-Filter and  $\lceil \log_2(M)/2 \rceil M$  Complex Phase Rotators**

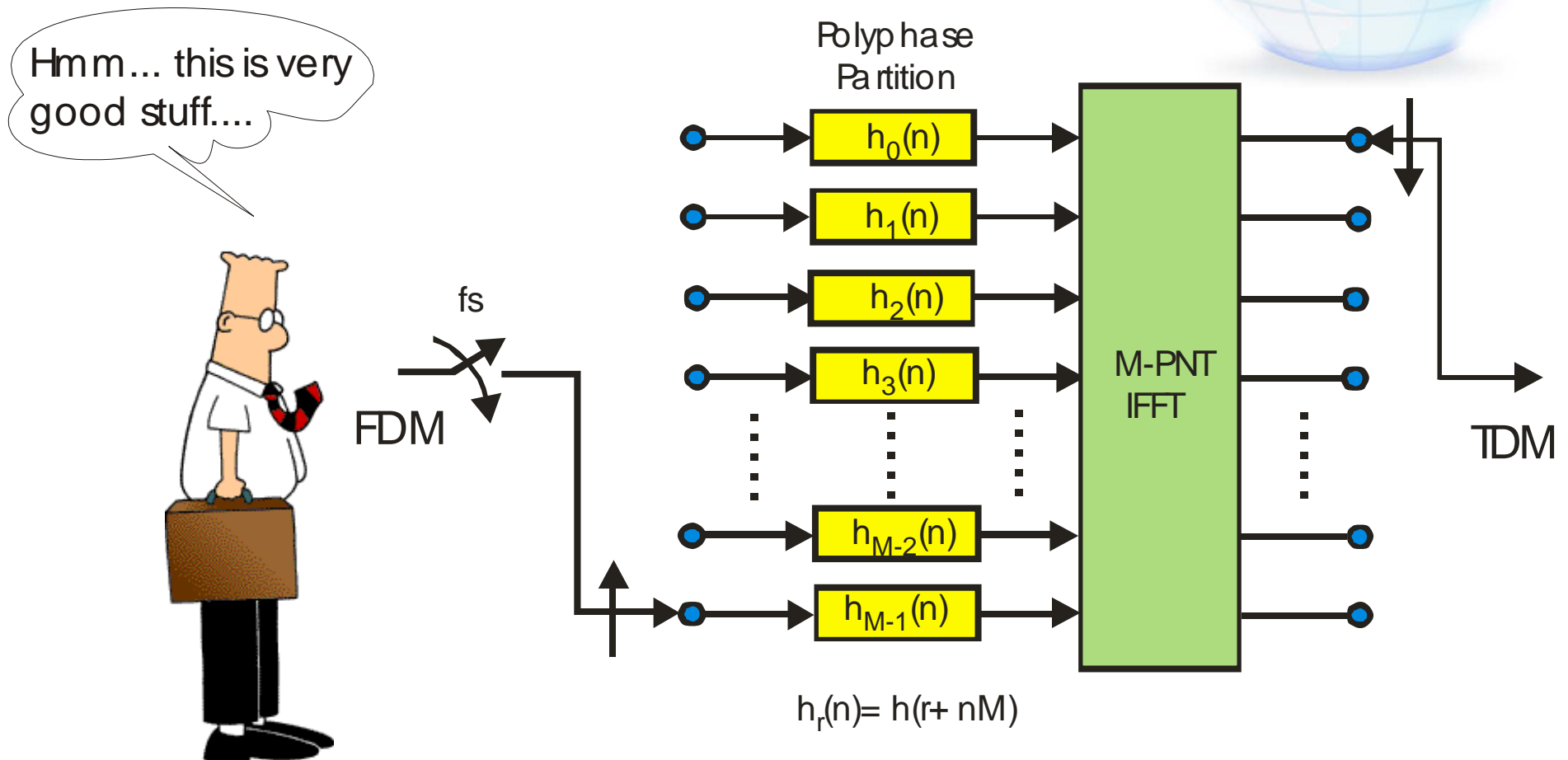
**When  $k > \log_2(M)/2$  Build all channels and discard the channels you don't need!**

**IF  $M=16$ ,  $\log_2(16)/2 = 2$ : thus if you want 2 or more, Build them all!**

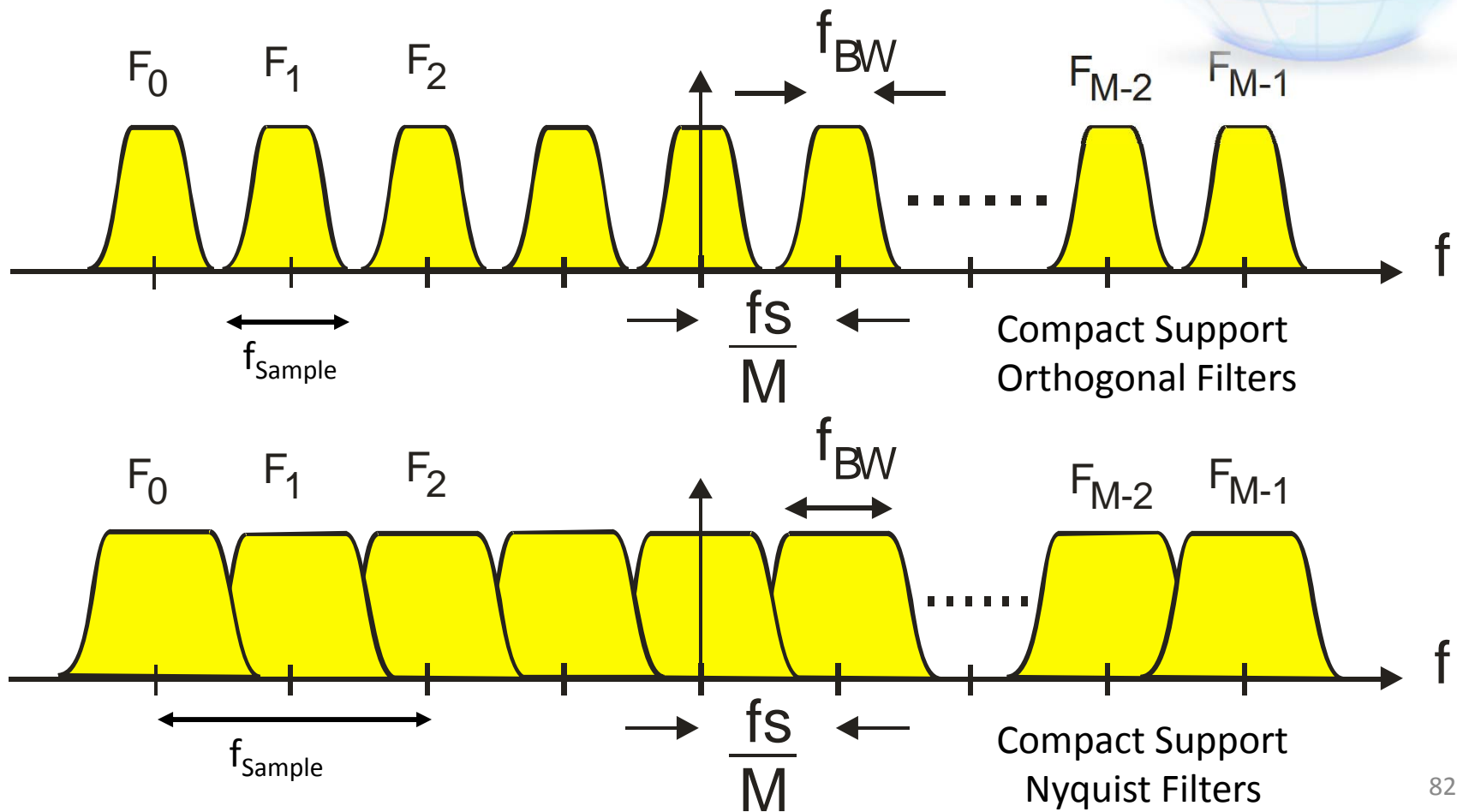
**IF  $M=128$ ,  $\log_2(128)/2 = 3.5$ : thus if you want 4 or more, Build them all!**

**IF  $M=1024$ ,  $\log_2(1024)/2 = 5$ : thus if you want 5 or more, Build them all!**

**M-Channel Channelizer: Resampled M-Path Narrowband Filter**  
**M-Channels Alias to Baseband: Phase Aligned Sums Separate Aliases:**  
**Work Performed at Low Output Rate Rather Than at High Input Rate.**  
**One Input Filter Services M-Output Channels**



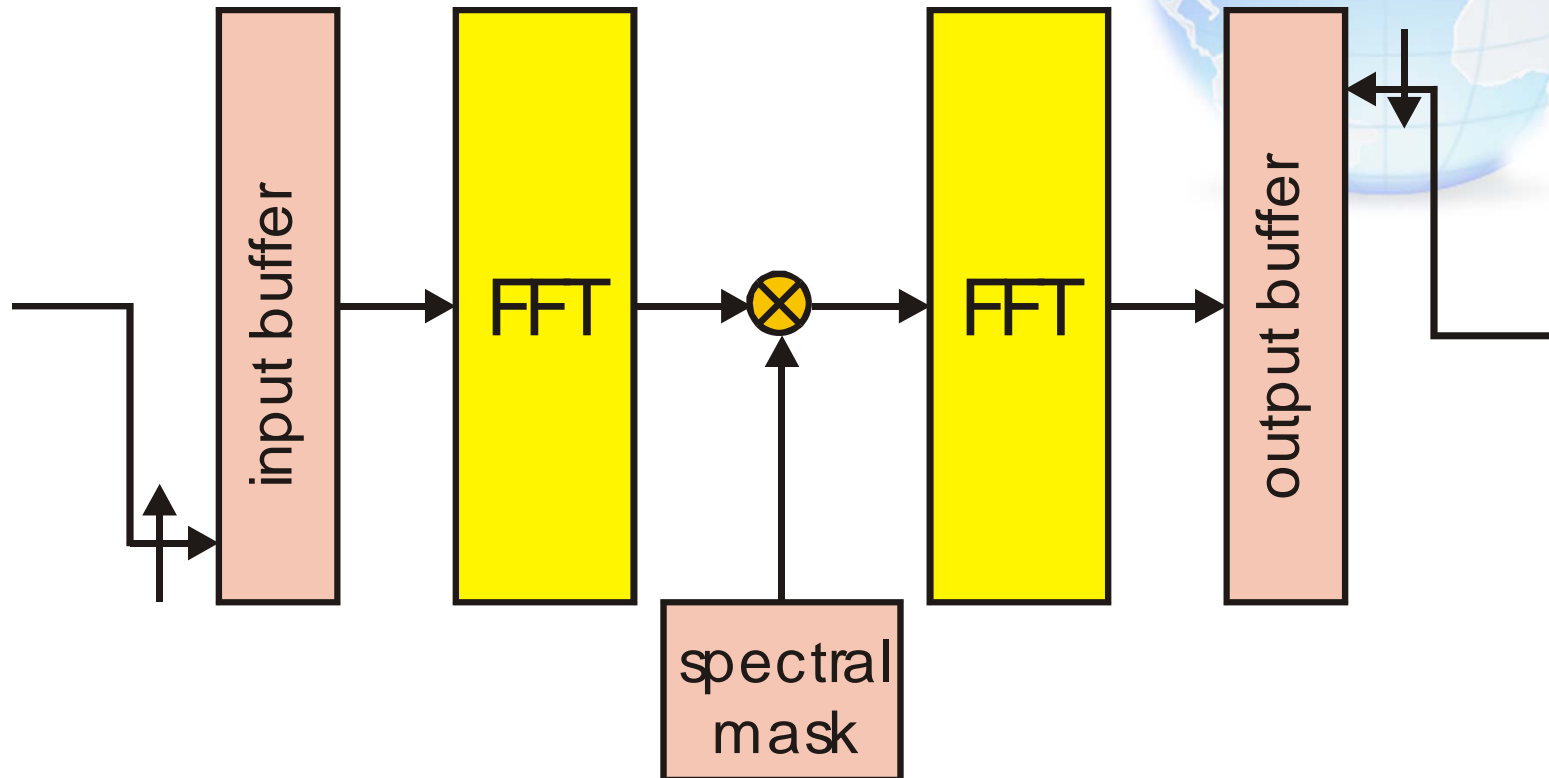
**Polyphase Channelizer:  
Bandwidth from Polyphase Filter,  
Spectral Spacing from IFFT,  
Sample Rate from Commutator**





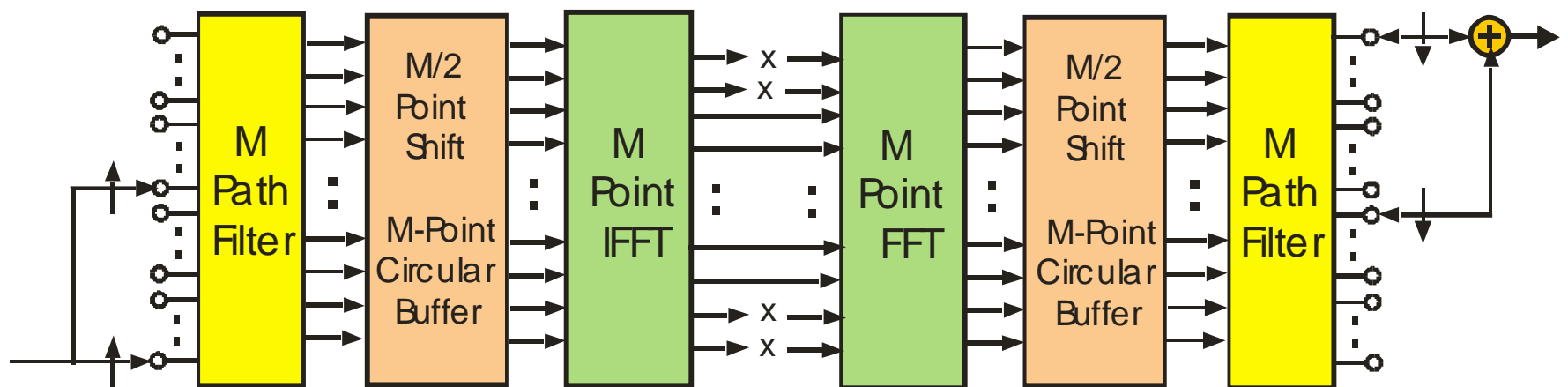
# Indirect Convolution, Fast Filtering by Spectral Product

## The Core Advantage of OFDM



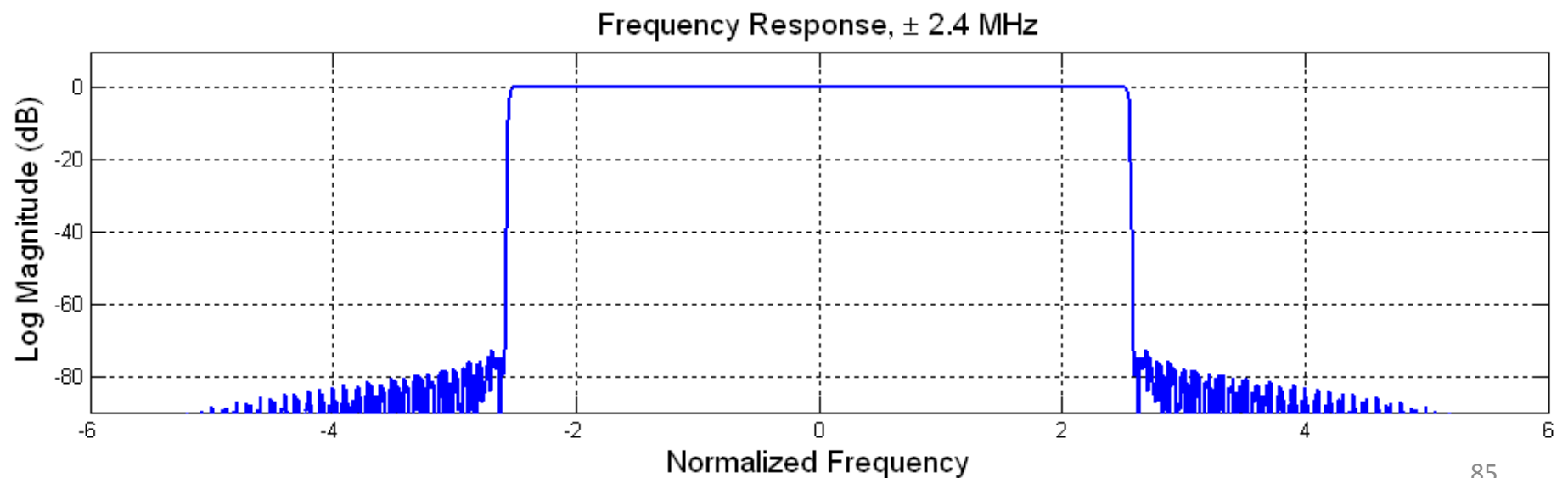
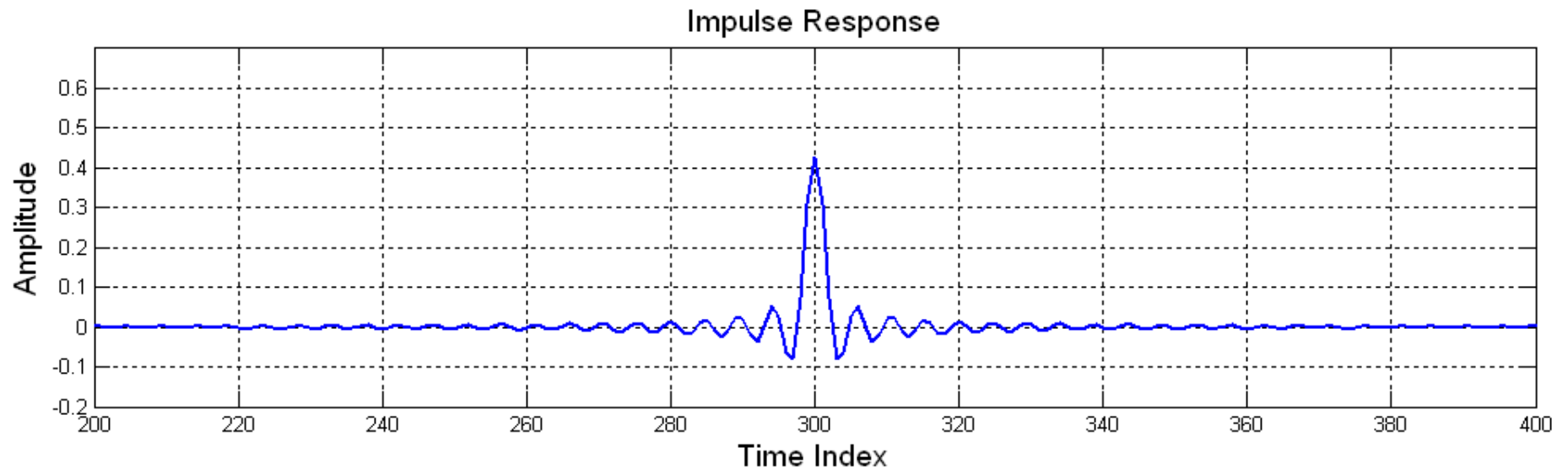
**Block Processing Related Boundary Conditions.  
Boundaries are Natural for OFDM Waveforms**

# Filtering in the Frequency Domain



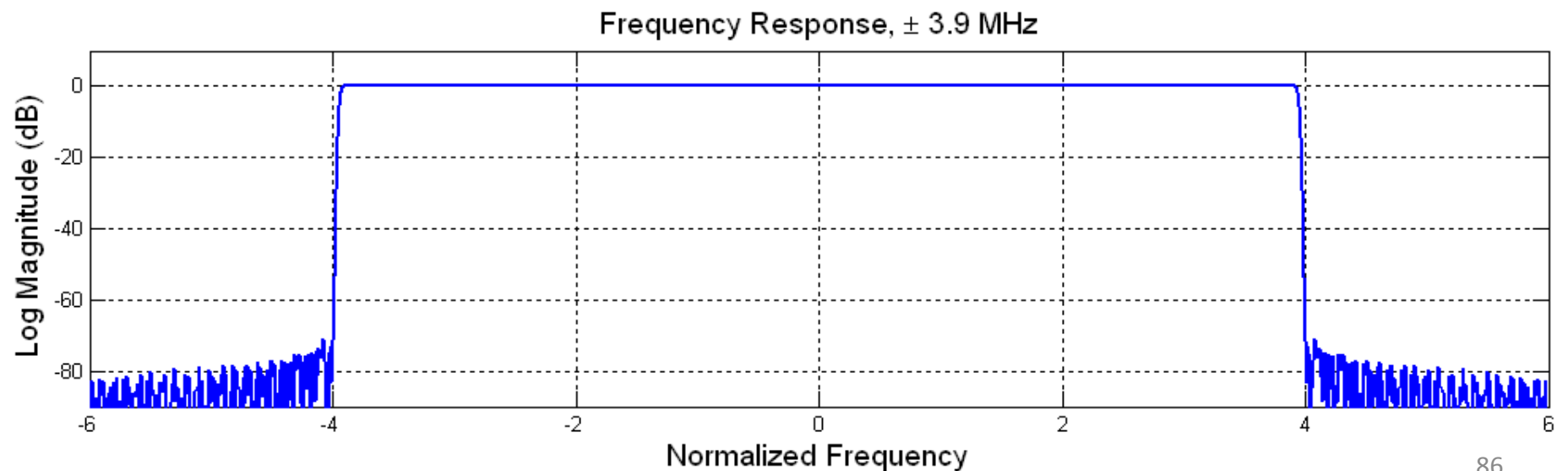
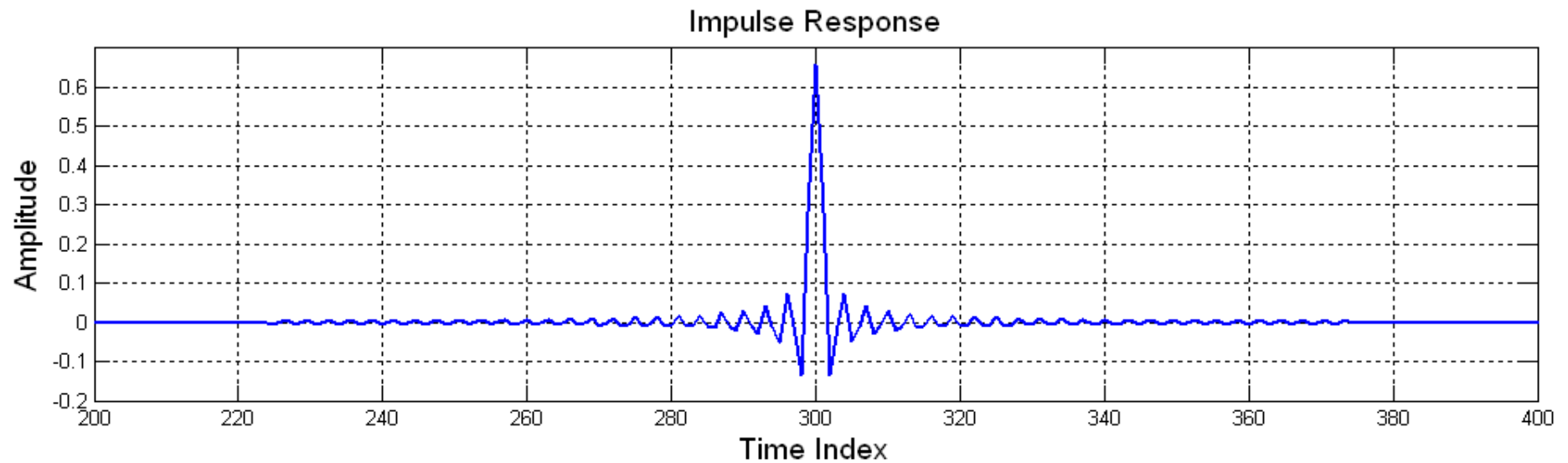
# Impulse Response and Frequency Response

## 25-Enabled Ports: 2.4 MHz Bandwidth

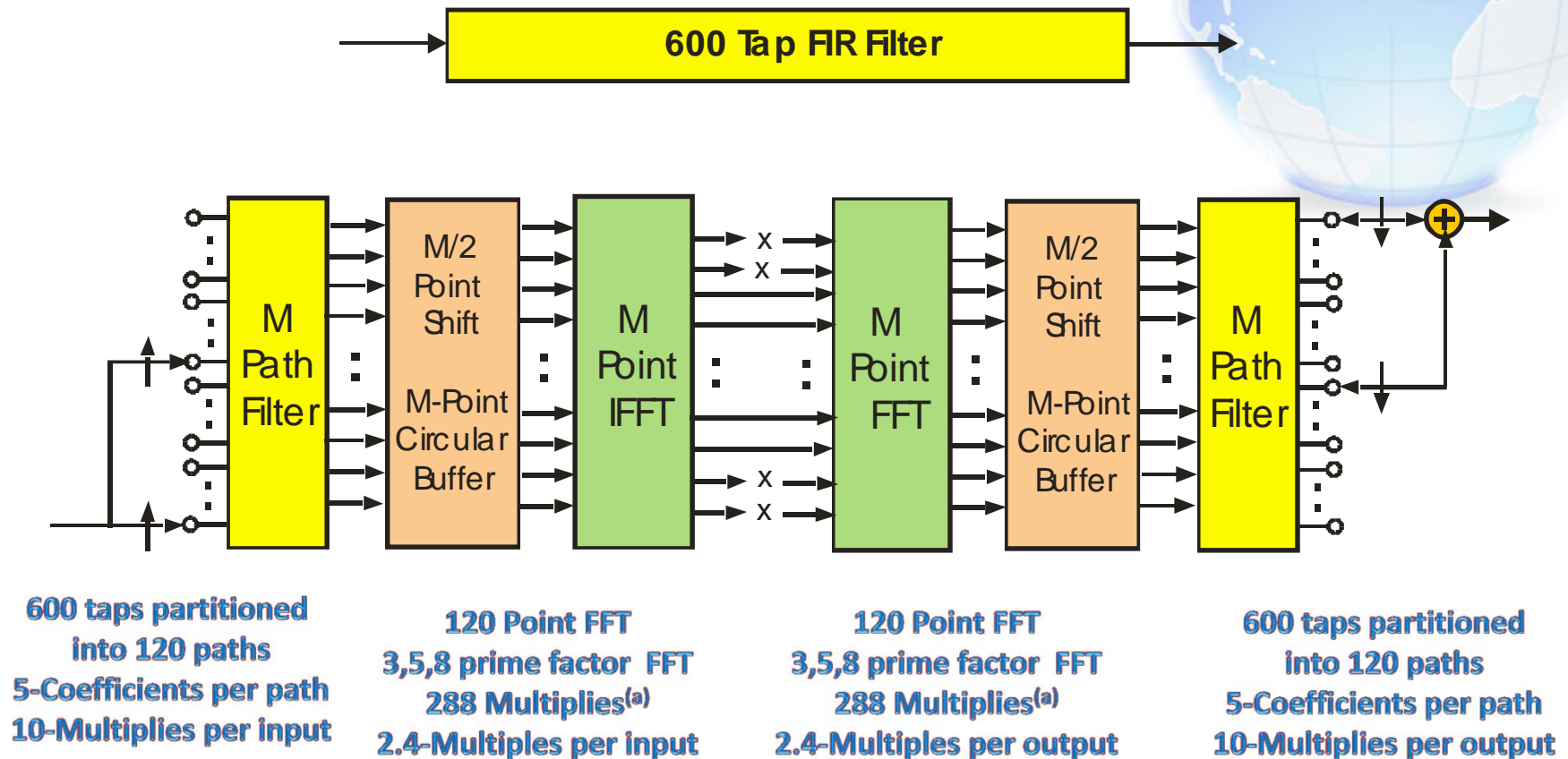


# Impulse Response and Frequency Response

## 40-Enabled Ports: 3.9 MHz Bandwidth



# Frequency Domain Filtering With Cascade M/2-to-1 Analysis and 1-to-M/2 Synthesis Channelizers



**Direct Convolution: 600 Multiplies per input-output pair**  
**Channelizer Convolution: 25 multiplies per input output pair**  
**4.16% of Computational Effort, 95.8% Saving**

<sup>(a)</sup> Complex Input Samples



## MATLAB DEMO-3

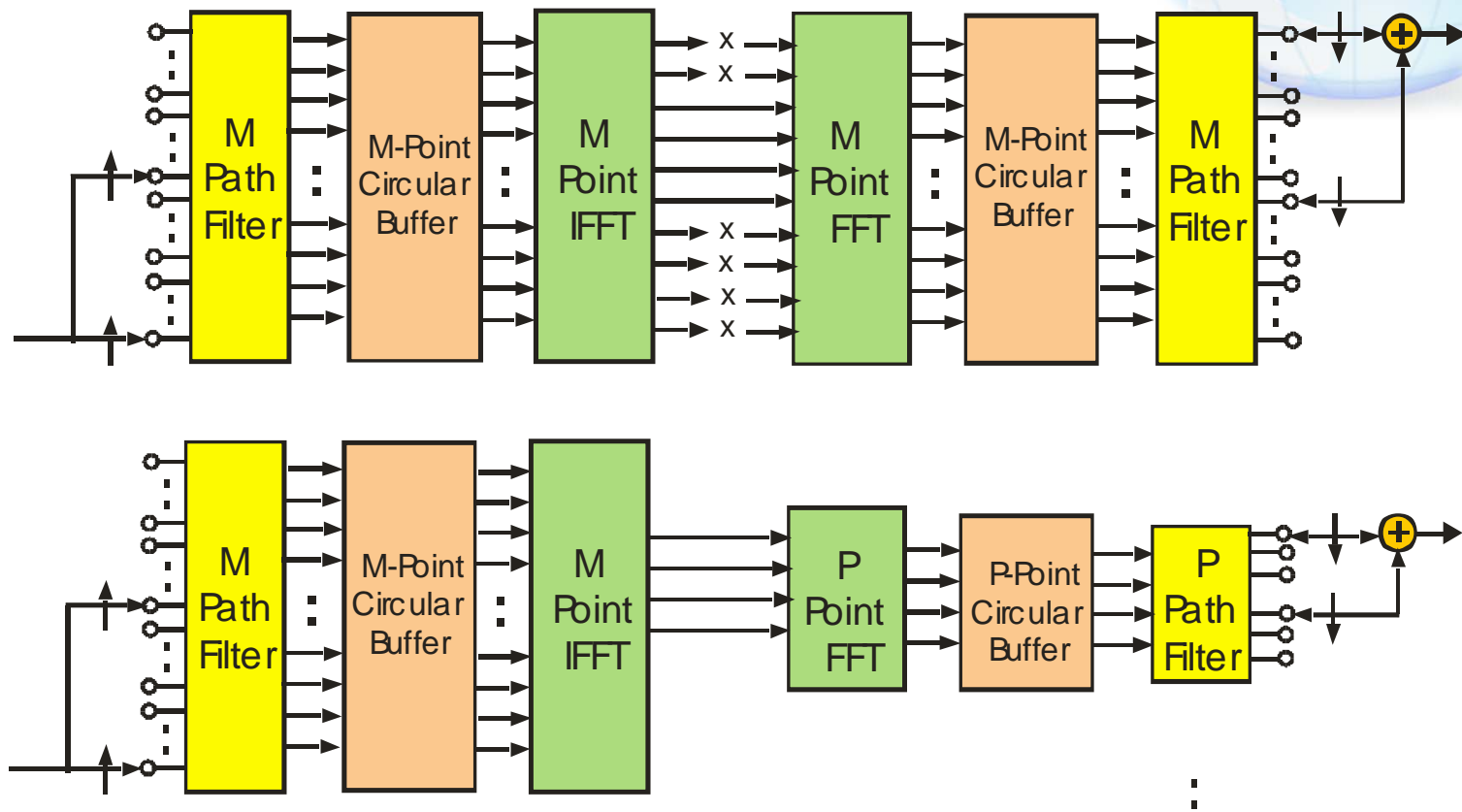
**vary\_bw\_channelizer\_120\_3a**



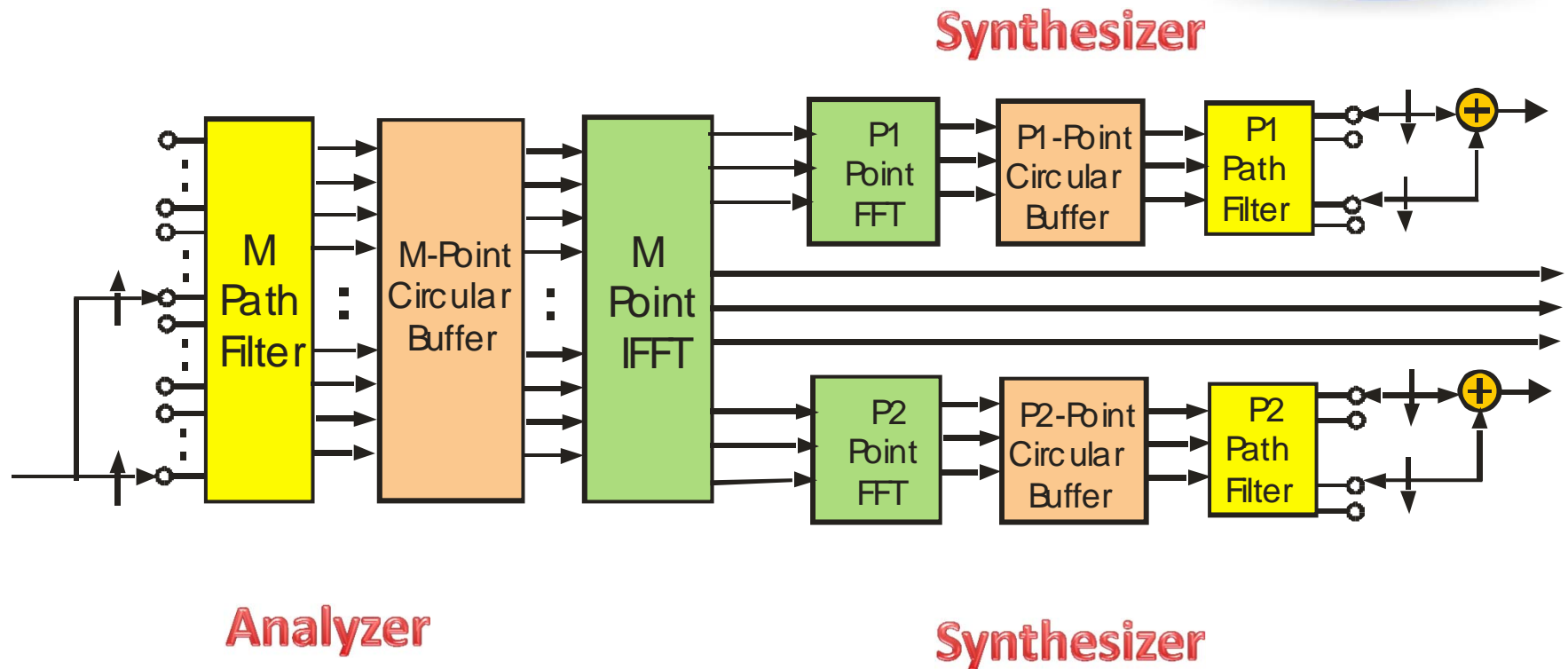
# Mixed, Arbitrary Bandwidth Channelizers

# Change Bandwidth With Mask

## Change Sample Rate With Transform

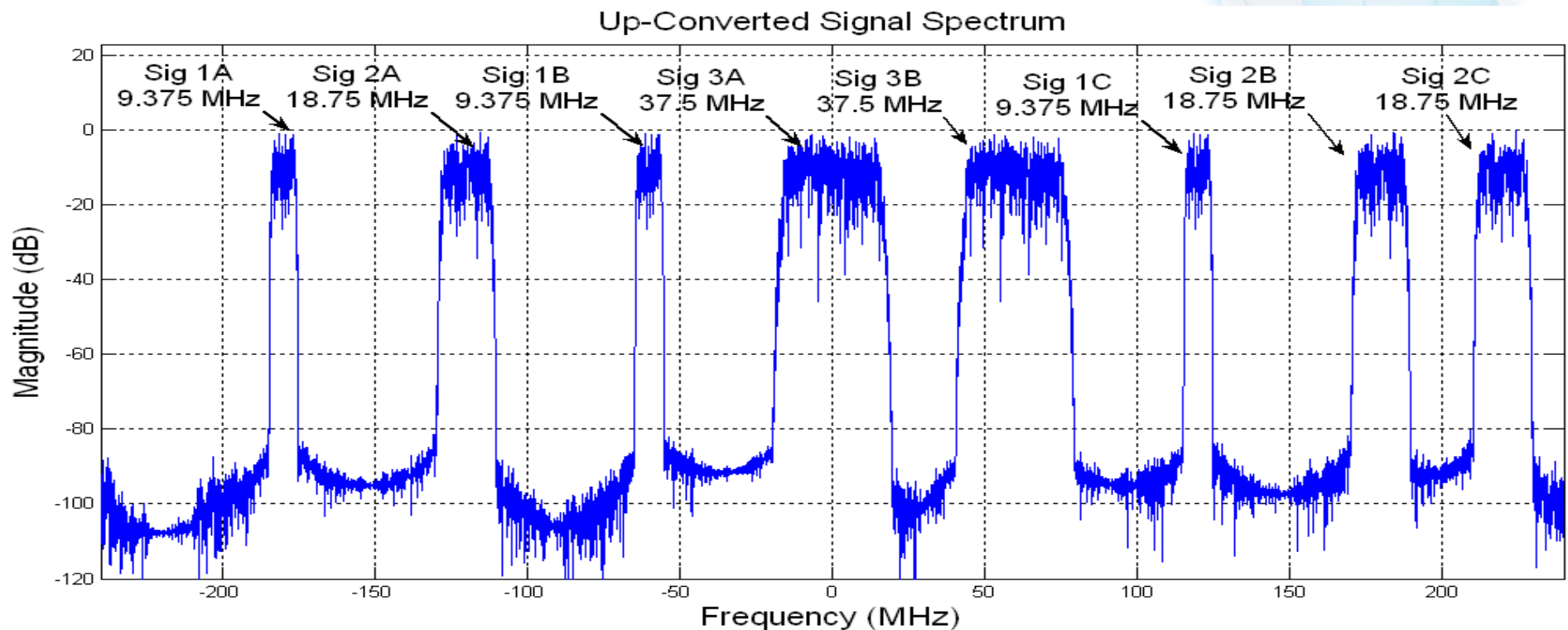


# Reassemble Decomposed Broadband Signals Using Short Synthesis Filters Formed by Multiple Channel Analysis Channelizer



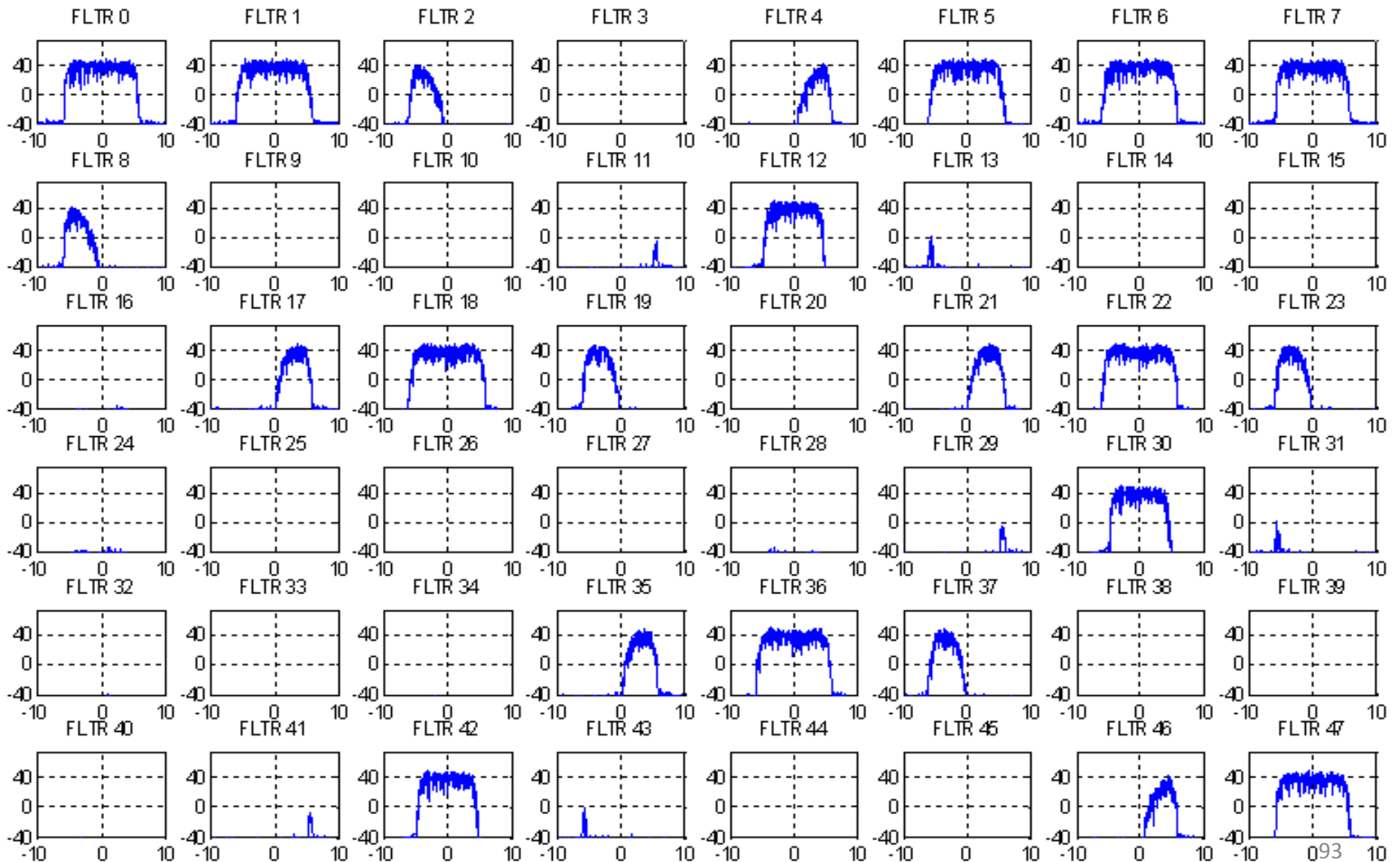
# Input Spectrum to Be Dissembled in M-Path Channelizer

## Multiple BW Channels from Single Analysis Channelizer

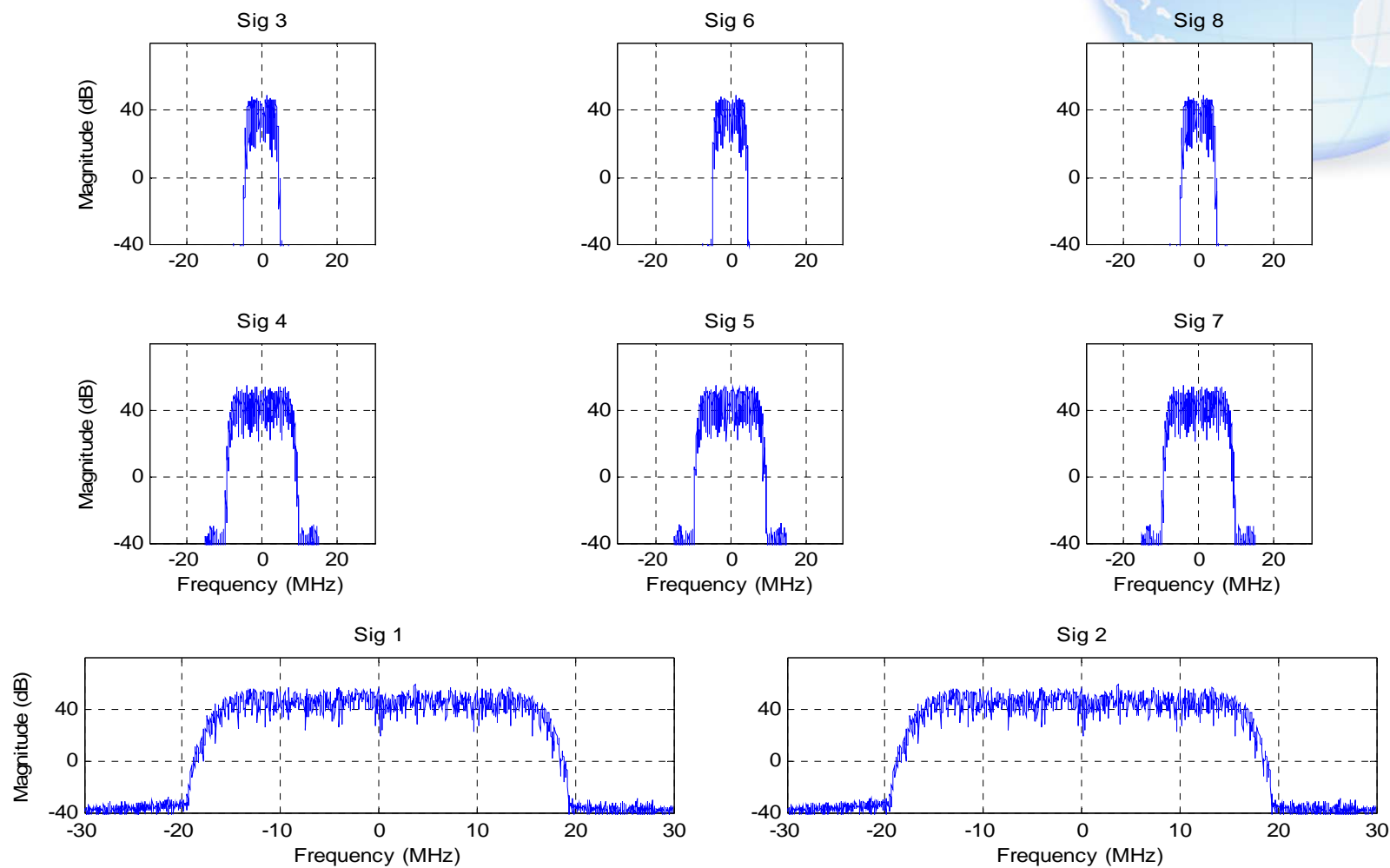
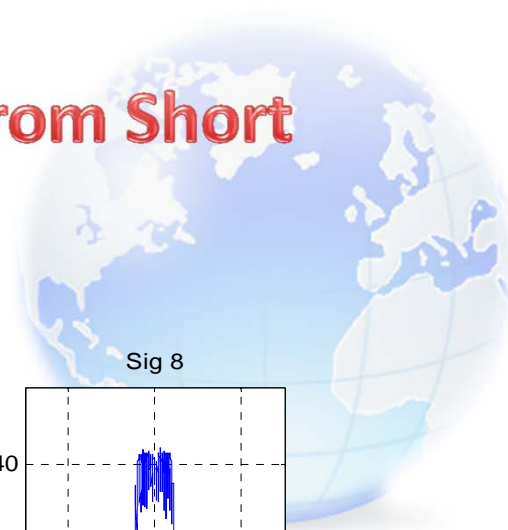




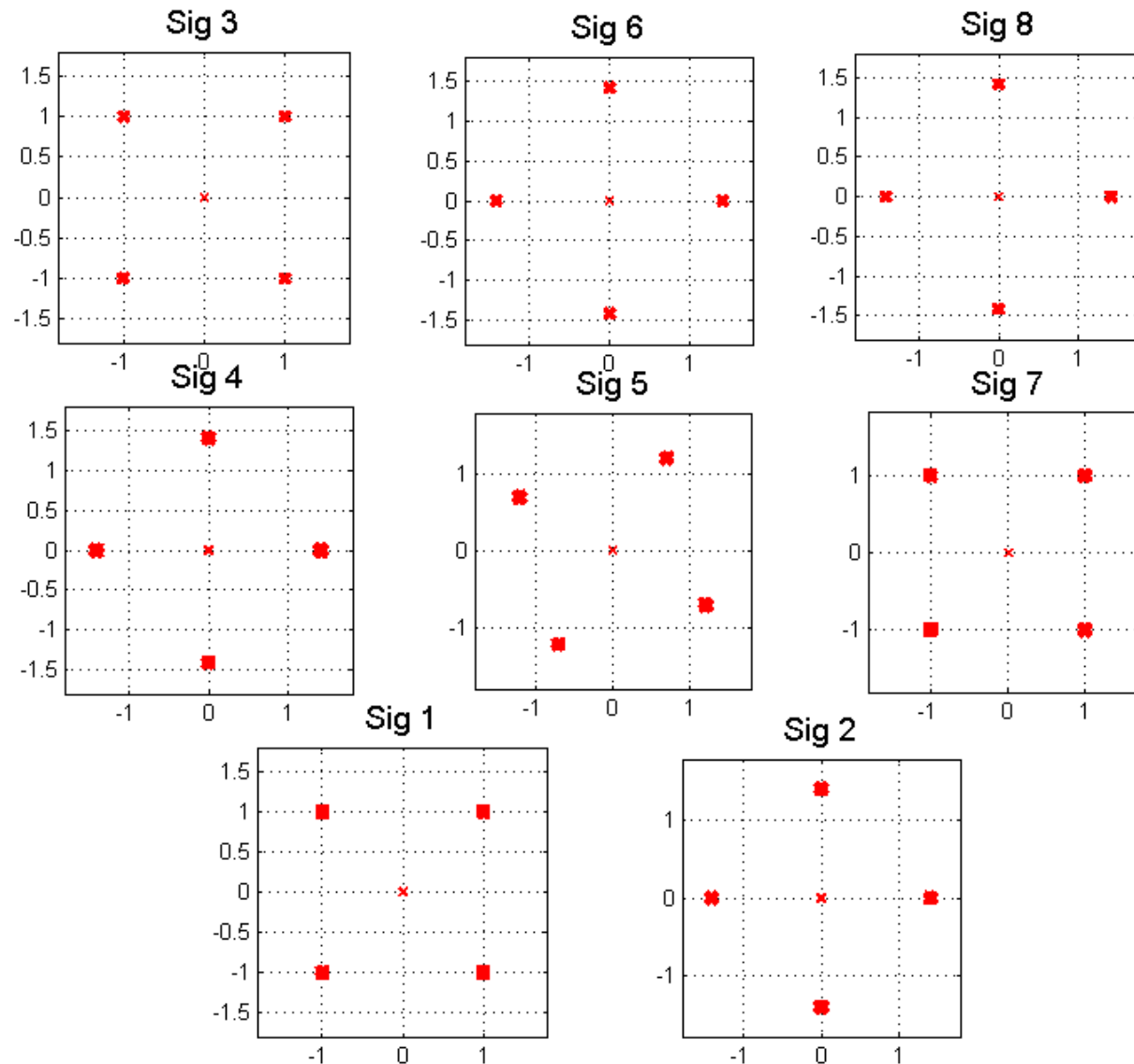
# Partitioned Spectral Components from Single Multi-Channel Analyzer



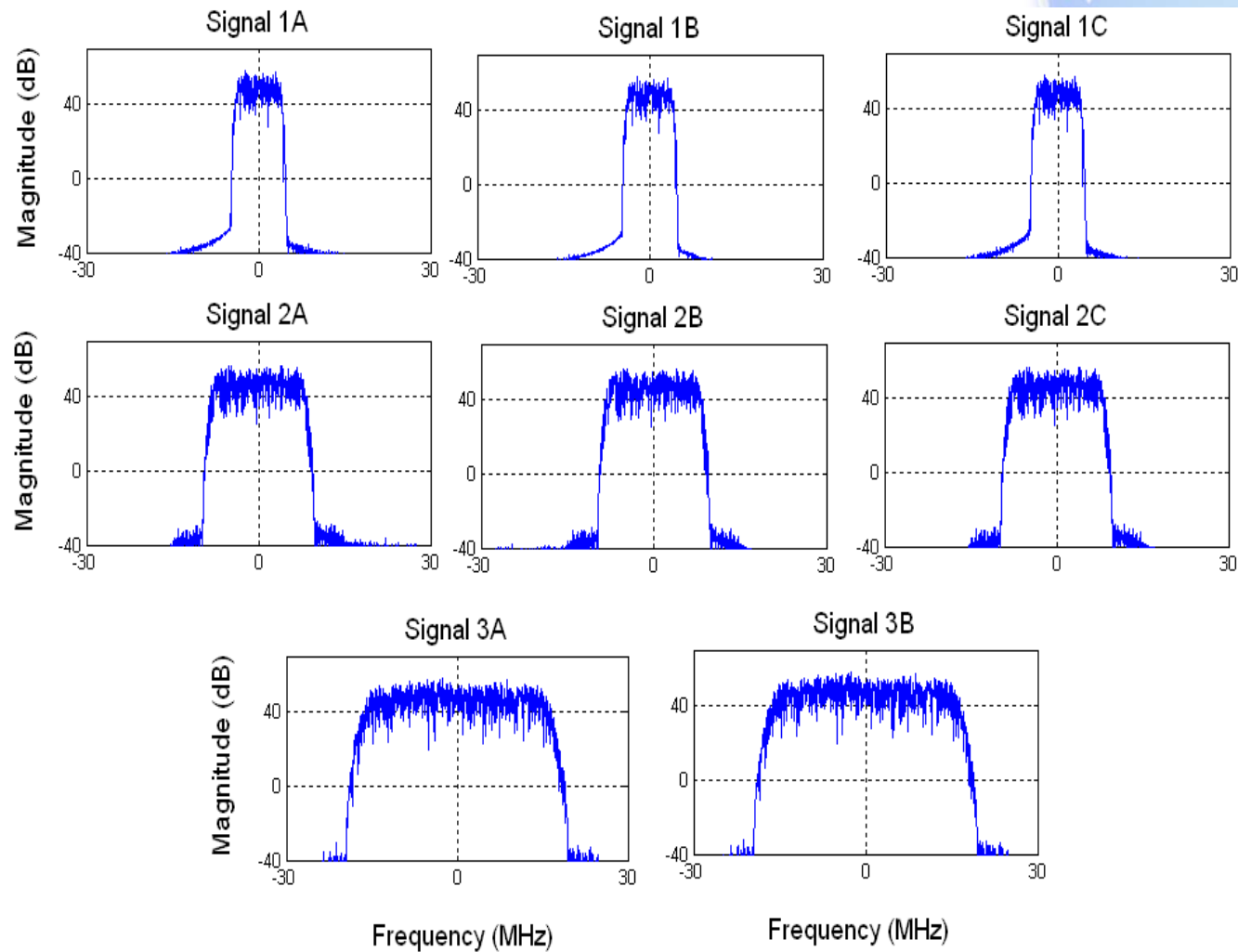
# Reassembled Wide Band Channels from Short Synthesis Channelizers



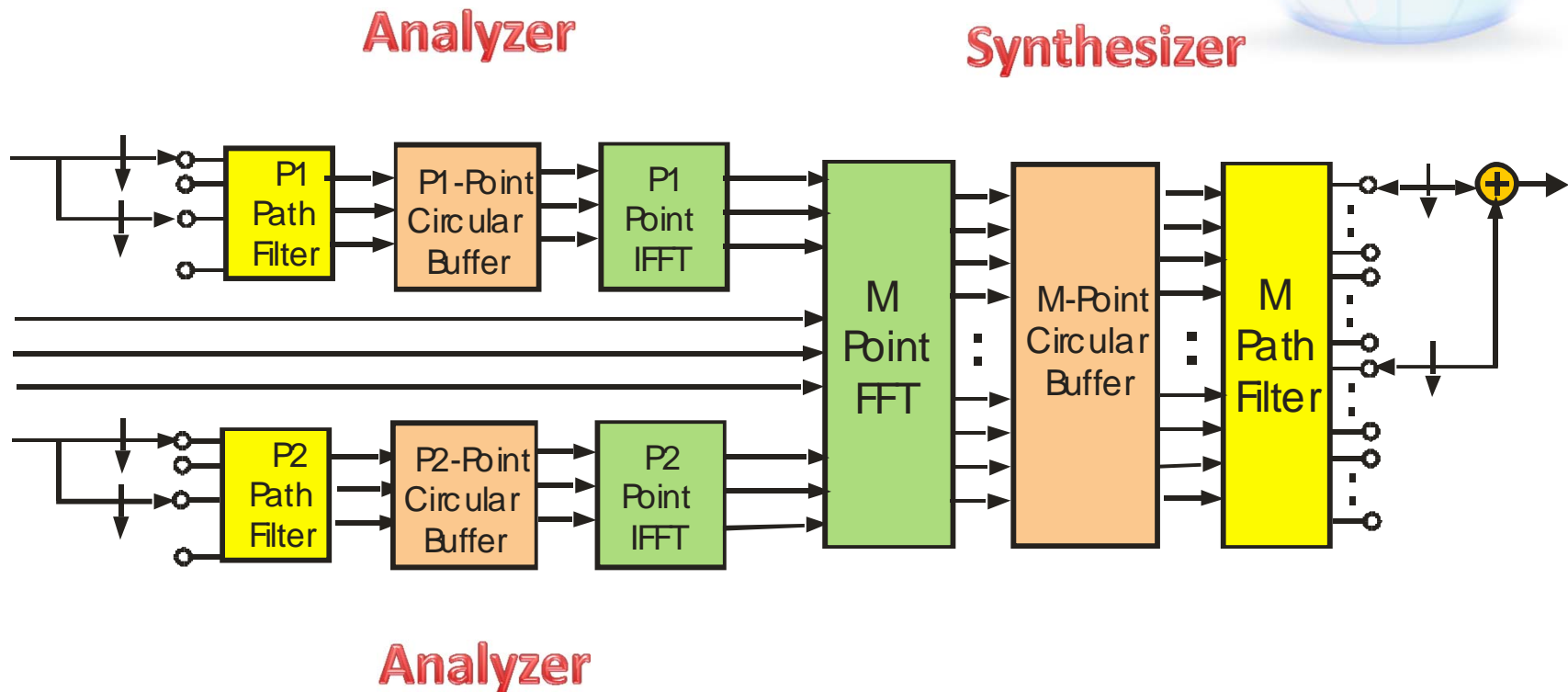
# Signal Fidelity Preserved under Multiple Sub-Channel Disassembly and Reassembly



# Mixed Bandwidth Signals Presented to Channel Synthesizer

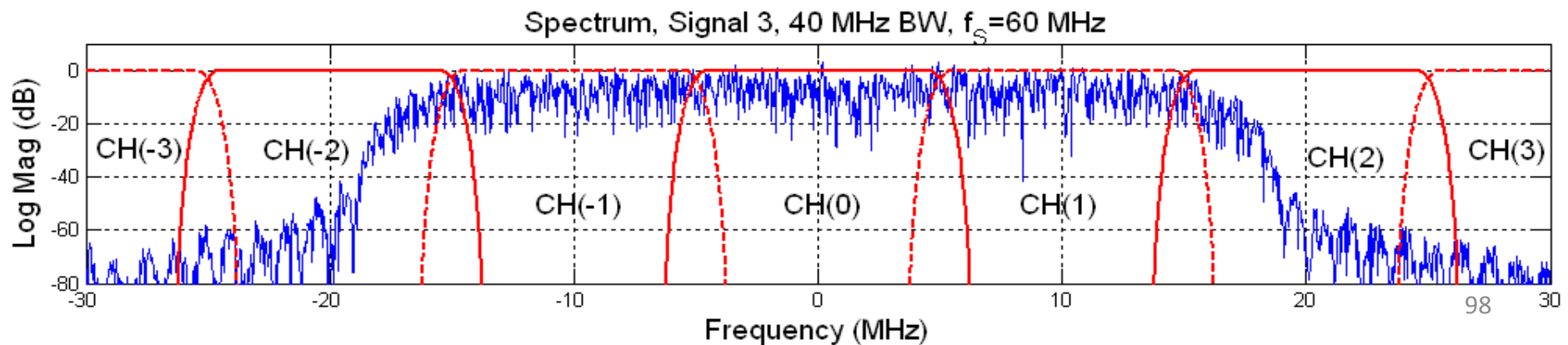
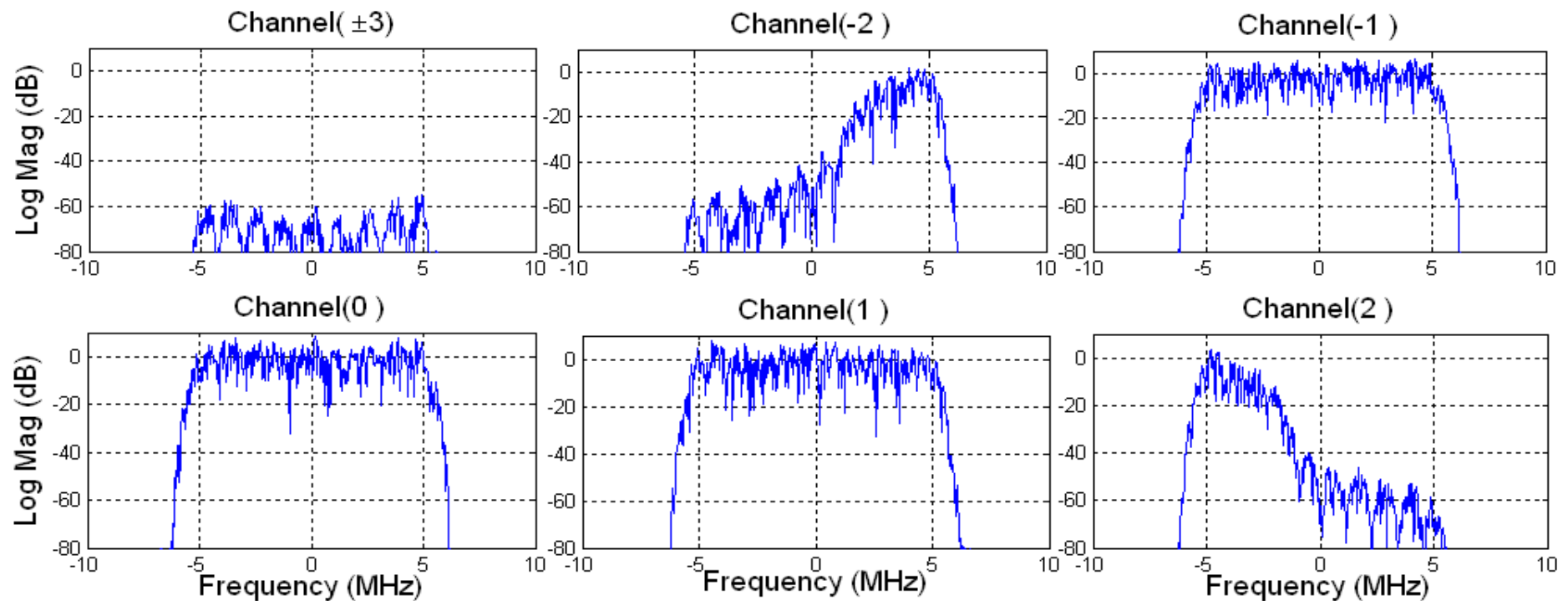


# Decompose Broadband Signals Using Short Analysis Filters and Present Components to Synthesizer

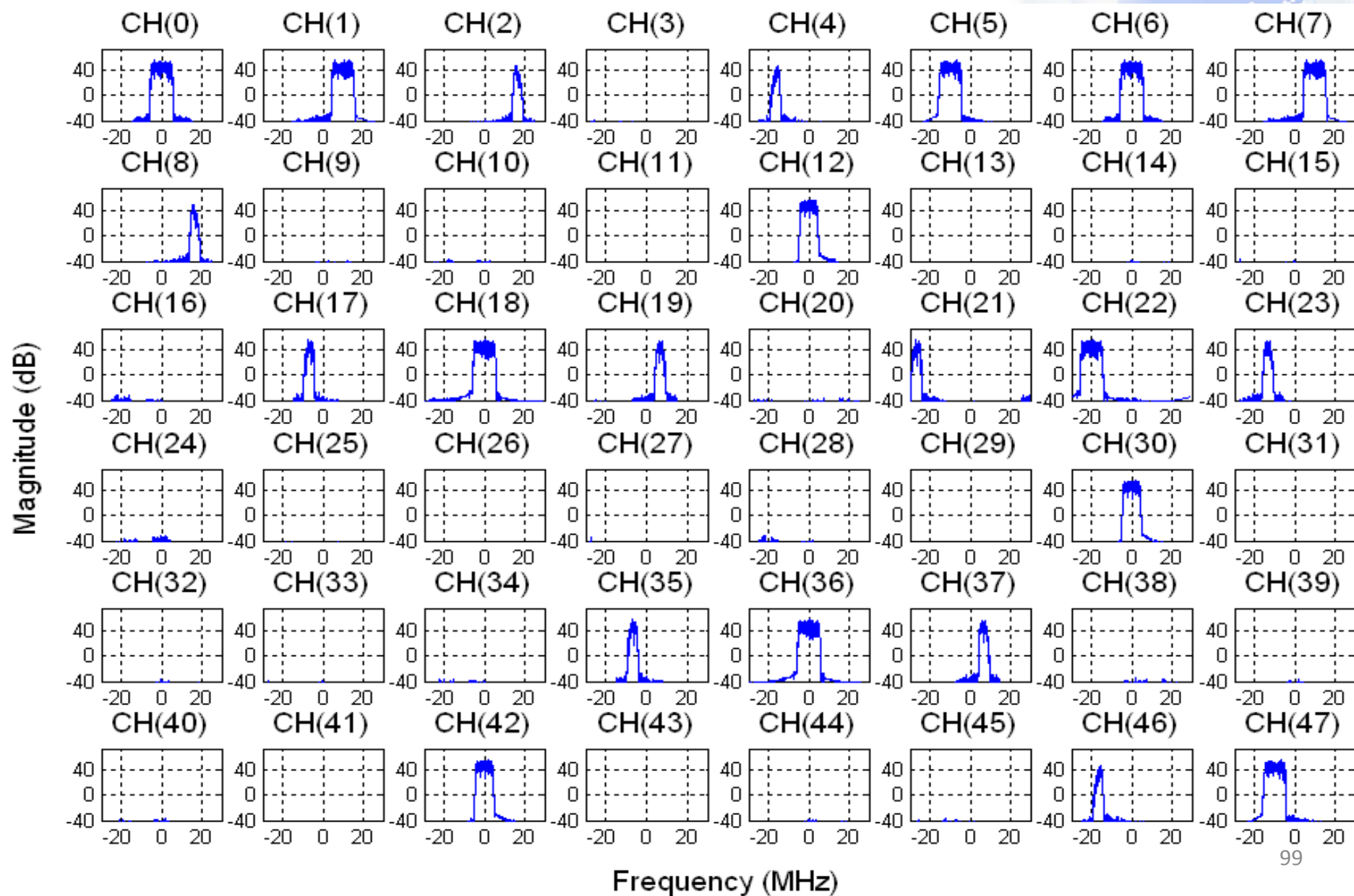




# 40-MHz Input Signal Partitioned into Five 10-MHz Sub-Channels: $f_s=20$ MHz



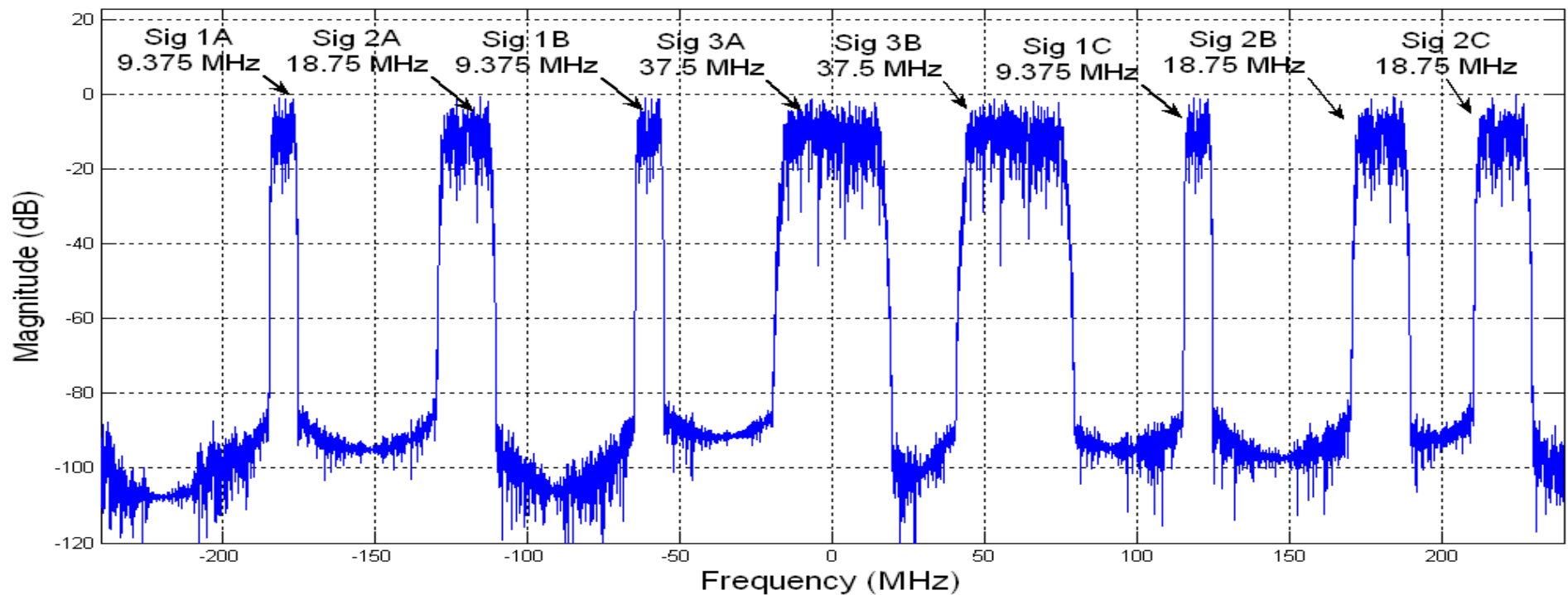
# Multiple Partitioned Input Bands Presented to Synthesizer



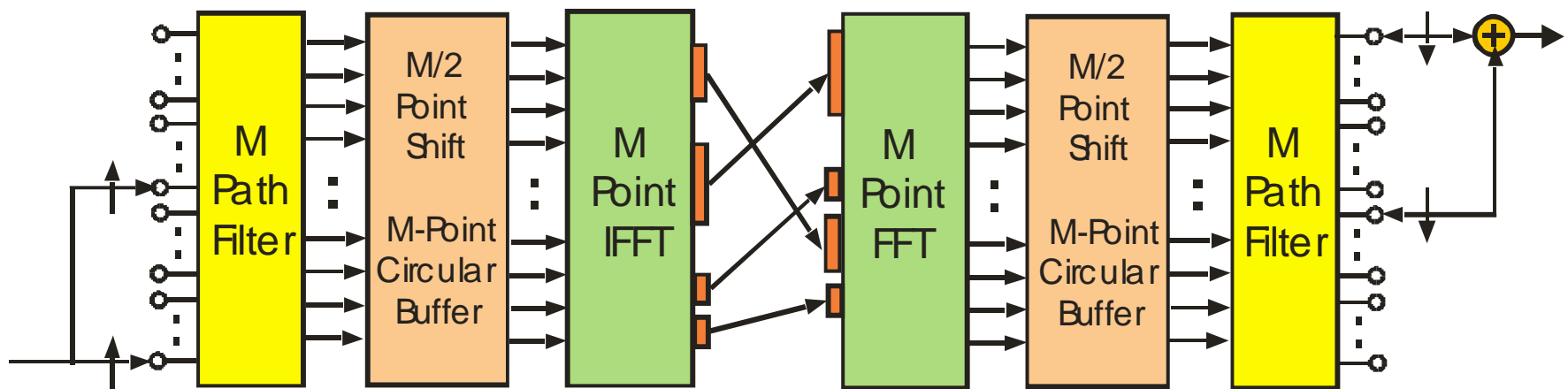
# Assembled Multiple BW Channels in Single Synthesis Channelizer



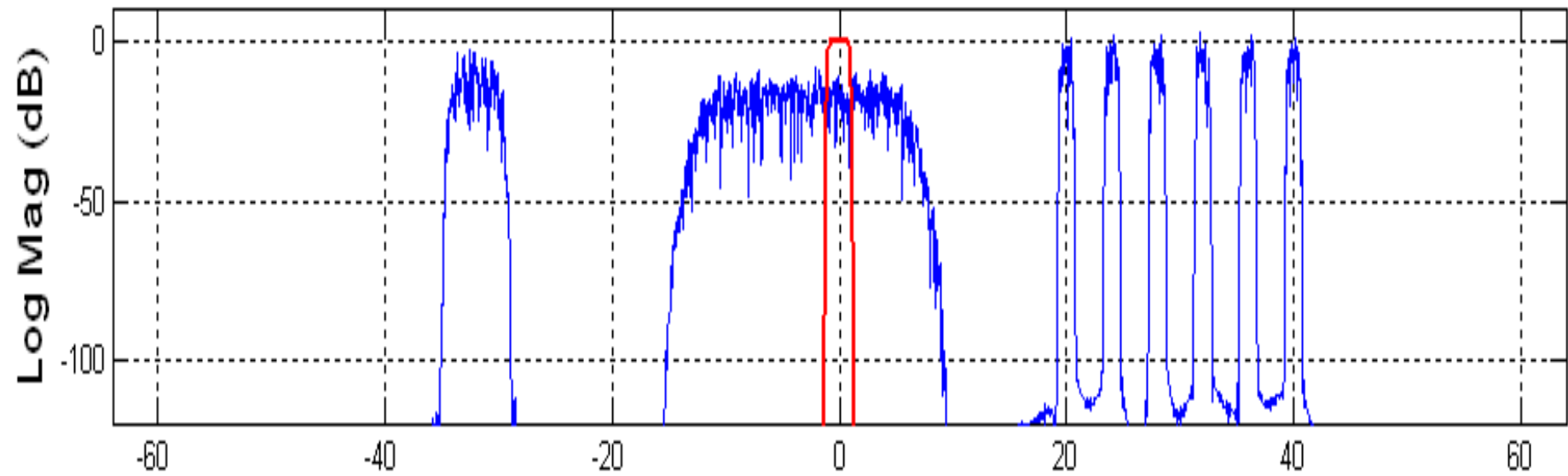
Up-Converted Signal Spectrum



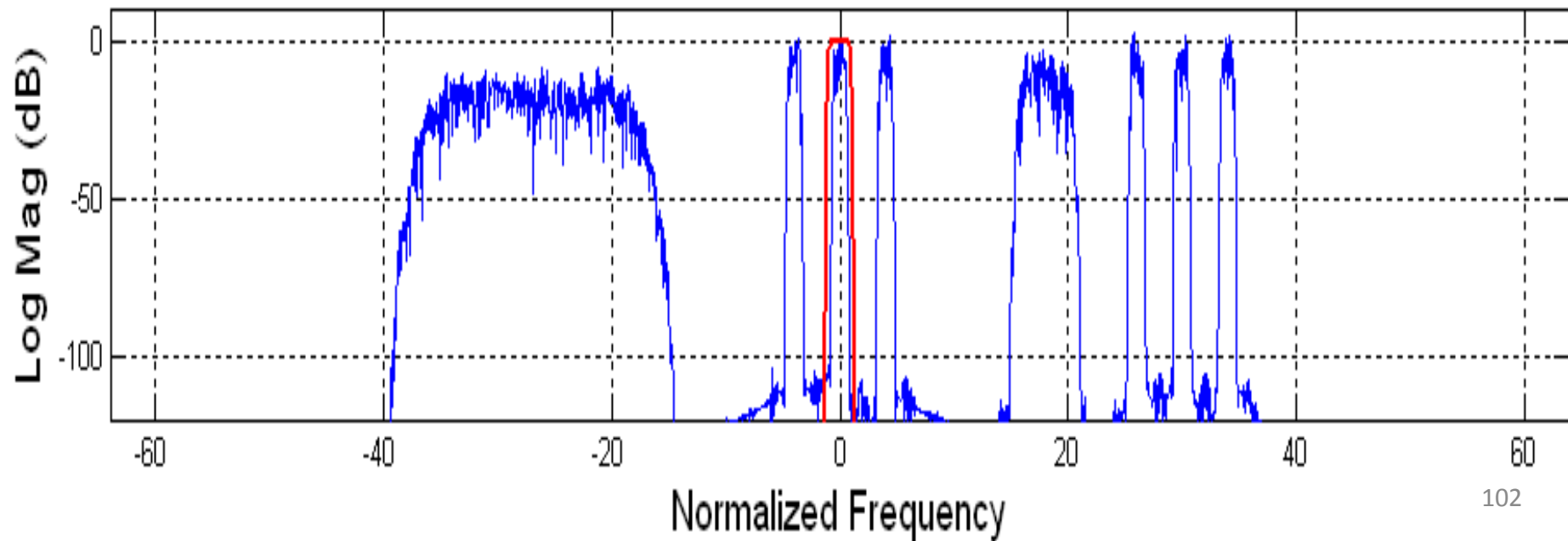
# Cascade $M/2$ -to-1 Analysis and 1-to- $M/2$ Synthesis Channelizers Frequency Domain Filtering and Spectral Shuffle



Composite Multi-Channel Input Spectrum

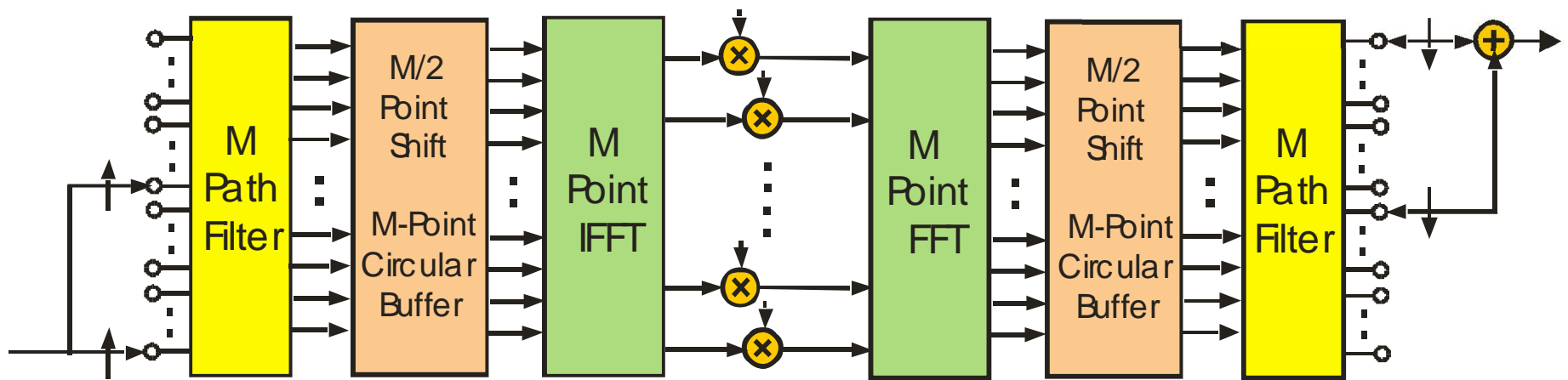


Composite Analysis, Rearranged, and Synthesized Output Spectrum





# Spectral Weights: Arbitrary Filter-Equalizer





# SOFTWARE DEFINED RADIO MAN

Is Open For Questions



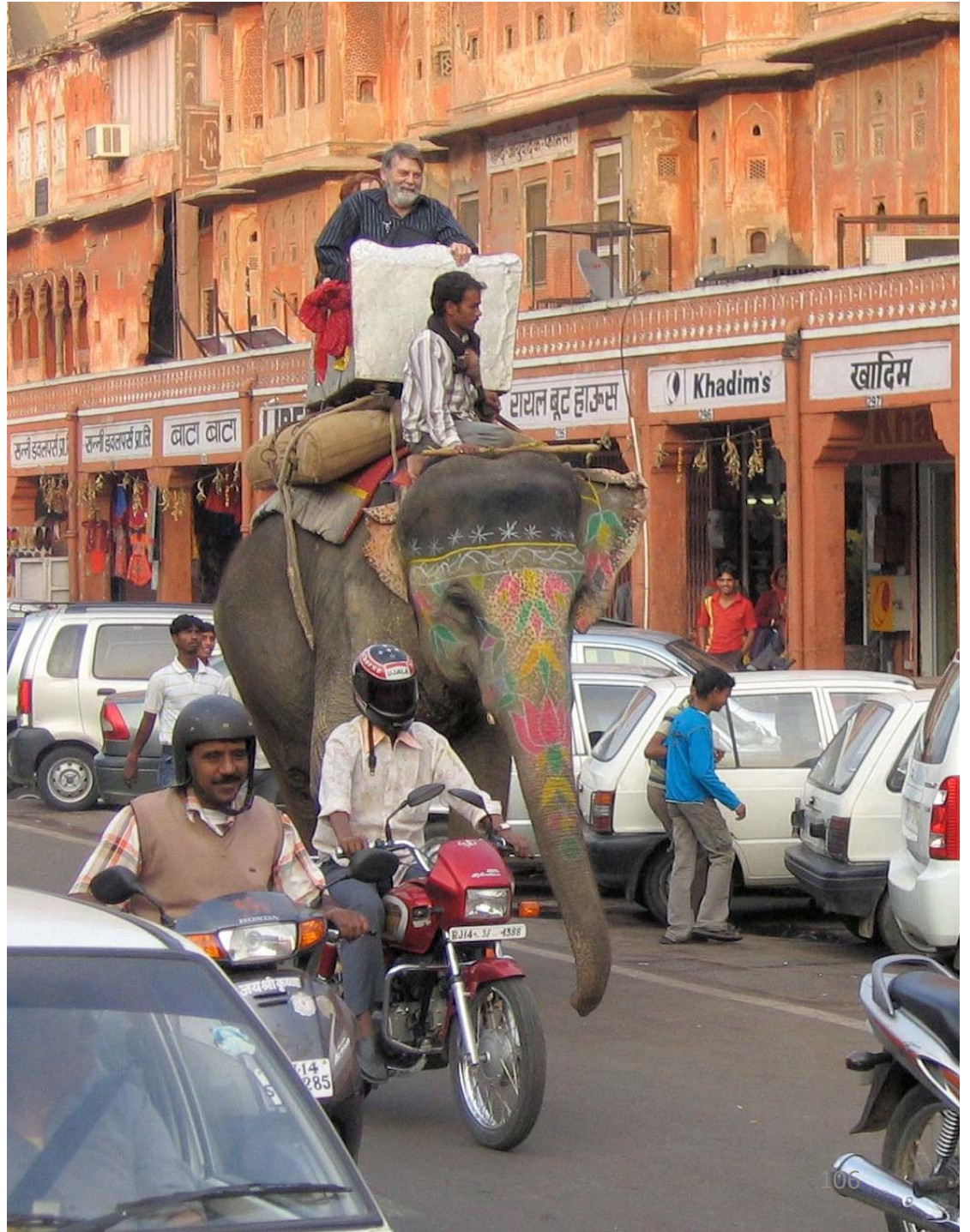
Going to work on my trusty steed, Trigger







**Going to work  
on my other  
trusty steed  
Big Girl**







**Commuting  
from  
EC&E office  
to my office  
on the  
Skateboard  
Express**





# We Now Are Really Open For Questions

